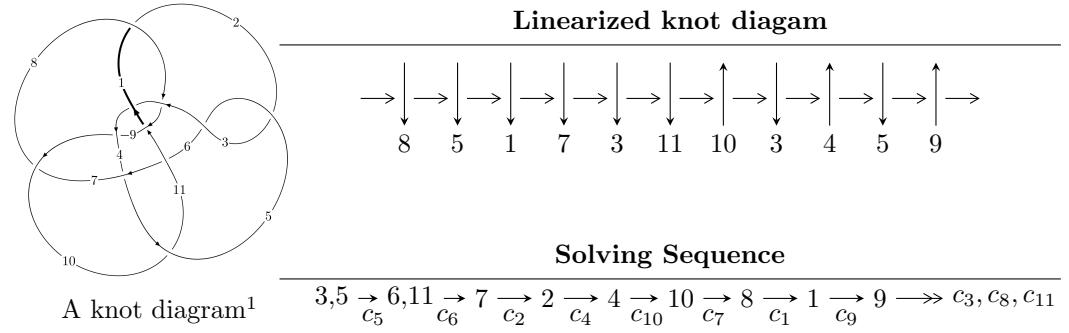


## $11n_{178}$ ( $K11n_{178}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle 1.44183 \times 10^{20} u^{19} - 4.62808 \times 10^{20} u^{18} + \dots + 4.02960 \times 10^{22} b + 1.32550 \times 10^{22}, \\
 &\quad 5.38510 \times 10^{21} u^{19} - 1.93058 \times 10^{22} u^{18} + \dots + 5.64145 \times 10^{23} a - 1.58764 \times 10^{23}, u^{20} - 3u^{19} + \dots + 50u + \dots \rangle \\
 I_2^u &= \langle 8.27426 \times 10^{22} au^{24} + 2.16729 \times 10^{23} u^{24} + \dots - 8.08063 \times 10^{23} a - 2.16180 \times 10^{24}, \\
 &\quad 1.10607 \times 10^{23} au^{24} - 4.35547 \times 10^{23} u^{24} + \dots - 2.26434 \times 10^{24} a + 5.35326 \times 10^{24}, u^{25} + 2u^{24} + \dots - 18u + \dots \rangle \\
 I_3^u &= \langle -498u^9 a + 411u^9 + \dots - 538a - 71, 33u^9 a - 50u^9 + \dots + 36a + 14, \\
 &\quad u^{10} + u^9 + u^8 - u^7 - 7u^6 - 6u^5 - 4u^4 - u^3 + 4u^2 - 1 \rangle \\
 I_4^u &= \langle b + u, a - u + 1, u^3 + u + 1 \rangle
 \end{aligned}$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 93 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 1.44 \times 10^{20} u^{19} - 4.63 \times 10^{20} u^{18} + \dots + 4.03 \times 10^{22} b + 1.33 \times 10^{22}, \ 5.39 \times 10^{21} u^{19} - 1.93 \times 10^{22} u^{18} + \dots + 5.64 \times 10^{23} a - 1.59 \times 10^{23}, \ u^{20} - 3u^{19} + \dots + 50u + 28 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.00954560u^{19} + 0.0342214u^{18} + \dots - 2.04736u + 0.281424 \\ -0.00357808u^{19} + 0.0114852u^{18} + \dots - 1.57985u - 0.328941 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.00788039u^{19} - 0.0328040u^{18} + \dots - 0.518617u + 0.751134 \\ 0.00598606u^{19} - 0.0182745u^{18} + \dots + 0.965413u - 0.0154483 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.0104192u^{19} + 0.0403606u^{18} + \dots - 0.479468u + 0.453996 \\ 0.00910287u^{19} - 0.0324780u^{18} + \dots + 0.974959u + 0.291739 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.0131237u^{19} + 0.0457066u^{18} + \dots - 3.62721u - 0.0475176 \\ -0.00357808u^{19} + 0.0114852u^{18} + \dots - 1.57985u - 0.328941 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.0117479u^{19} + 0.0388218u^{18} + \dots - 2.47010u + 0.992450 \\ -0.00558459u^{19} + 0.0212055u^{18} + \dots - 0.758704u - 0.267277 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.000551726u^{19} + 0.00433088u^{18} + \dots + 2.81102u + 0.992999 \\ -0.00916278u^{19} + 0.0352104u^{18} + \dots + 0.357114u - 0.220651 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.0117479u^{19} + 0.0388218u^{18} + \dots - 2.47010u + 0.992450 \\ -0.00633555u^{19} + 0.0263534u^{18} + \dots - 0.608667u - 0.367463 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.0117479u^{19} + 0.0388218u^{18} + \dots - 2.47010u + 0.992450 \\ -0.00633555u^{19} + 0.0263534u^{18} + \dots - 0.608667u - 0.367463 \end{pmatrix}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = -\frac{2008394464227286266247}{48150419926932042591458}u^{19} + \frac{6462622260672532812482}{20148019962096448350151}u^{18} + \dots -$$

$$-\frac{13344332465178993232190}{20148019962096448350151}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_6$	$u^{20} - 5u^{19} + \cdots + 24u - 8$
$c_2, c_5$	$u^{20} - 3u^{19} + \cdots + 50u + 28$
$c_3, c_4$	$u^{20} - u^{19} + \cdots - 3u^2 + 1$
$c_7, c_{11}$	$u^{20} - 2u^{19} + \cdots - 5u - 1$
$c_8, c_{10}$	$u^{20} + 9u^{18} + \cdots + 5u - 1$
$c_9$	$u^{20} + 5u^{19} + \cdots + 192u + 32$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$y^{20} + 19y^{19} + \cdots + 384y + 64$
$c_2, c_5$	$y^{20} + 11y^{19} + \cdots + 6180y + 784$
$c_3, c_4$	$y^{20} - 3y^{19} + \cdots - 6y + 1$
$c_7, c_{11}$	$y^{20} + 24y^{18} + \cdots - 79y + 1$
$c_8, c_{10}$	$y^{20} + 18y^{19} + \cdots + 13y + 1$
$c_9$	$y^{20} + y^{19} + \cdots - 14336y + 1024$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.860797 + 0.516146I$	$-0.02958 - 4.97799I$	$-5.29605 + 5.59335I$
$a = -0.749789 - 0.590643I$		
$b = -0.155130 - 0.305377I$		
$u = 0.860797 - 0.516146I$	$-0.02958 + 4.97799I$	$-5.29605 - 5.59335I$
$a = -0.749789 + 0.590643I$		
$b = -0.155130 + 0.305377I$		
$u = -0.837495$		
$a = 1.44067$	$-4.10423$	$8.28190$
$b = -0.563826$		
$u = -0.127511 + 1.189810I$	$5.89336 + 2.36950I$	$5.34088 - 5.91566I$
$a = -0.55333 - 1.51288I$		
$b = -0.265516 + 1.136880I$		
$u = -0.127511 - 1.189810I$	$5.89336 - 2.36950I$	$5.34088 + 5.91566I$
$a = -0.55333 + 1.51288I$		
$b = -0.265516 - 1.136880I$		
$u = -1.206690 + 0.010929I$	$-1.50701 - 0.96018I$	$-11.18870 + 6.49006I$
$a = 0.309849 - 0.484836I$		
$b = 0.275436 - 1.241550I$		
$u = -1.206690 - 0.010929I$	$-1.50701 + 0.96018I$	$-11.18870 - 6.49006I$
$a = 0.309849 + 0.484836I$		
$b = 0.275436 + 1.241550I$		
$u = -0.044384 + 1.389540I$	$3.02537 + 1.86293I$	$-7.79633 - 3.80746I$
$a = -0.092328 - 1.185210I$		
$b = -0.230707 + 0.577747I$		
$u = -0.044384 - 1.389540I$	$3.02537 - 1.86293I$	$-7.79633 + 3.80746I$
$a = -0.092328 + 1.185210I$		
$b = -0.230707 - 0.577747I$		
$u = -0.495317$		
$a = 0.784881$	$-0.861131$	$-11.6540$
$b = 0.562448$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.008487 + 0.397854I$		
$a = 0.665300 - 0.862267I$	$1.66626 + 1.83421I$	$-0.60394 - 1.52765I$
$b = -0.433094 - 0.565353I$		
$u = -0.008487 - 0.397854I$		
$a = 0.665300 + 0.862267I$	$1.66626 - 1.83421I$	$-0.60394 + 1.52765I$
$b = -0.433094 + 0.565353I$		
$u = 1.70479 + 0.08565I$		
$a = 0.138055 - 0.057007I$	$2.91415 - 8.59875I$	$-1.50122 + 6.80502I$
$b = 0.519057 + 1.305600I$		
$u = 1.70479 - 0.08565I$		
$a = 0.138055 + 0.057007I$	$2.91415 + 8.59875I$	$-1.50122 - 6.80502I$
$b = 0.519057 - 1.305600I$		
$u = -0.47740 + 1.67811I$		
$a = 0.103149 + 1.154610I$	$4.37107 + 7.54282I$	$-5.65623 - 11.11643I$
$b = 1.18053 - 1.97776I$		
$u = -0.47740 - 1.67811I$		
$a = 0.103149 - 1.154610I$	$4.37107 - 7.54282I$	$-5.65623 + 11.11643I$
$b = 1.18053 + 1.97776I$		
$u = 0.68219 + 1.68930I$		
$a = -0.198906 + 1.142030I$	$8.5745 - 16.9983I$	$-2.67254 + 8.37996I$
$b = -1.17479 - 1.40102I$		
$u = 0.68219 - 1.68930I$		
$a = -0.198906 - 1.142030I$	$8.5745 + 16.9983I$	$-2.67254 - 8.37996I$
$b = -1.17479 + 1.40102I$		
$u = 0.78311 + 1.71850I$		
$a = 0.300944 - 0.712043I$	$8.00588 - 0.27607I$	$1.56028 - 0.31134I$
$b = 0.284896 + 1.301190I$		
$u = 0.78311 - 1.71850I$		
$a = 0.300944 + 0.712043I$	$8.00588 + 0.27607I$	$1.56028 + 0.31134I$
$b = 0.284896 - 1.301190I$		

$$\text{II. } I_2^u = \langle 8.27 \times 10^{22} au^{24} + 2.17 \times 10^{23} u^{24} + \dots - 8.08 \times 10^{23} a - 2.16 \times 10^{24}, 1.11 \times 10^{23} au^{24} - 4.36 \times 10^{23} u^{24} + \dots - 2.26 \times 10^{24} a + 5.35 \times 10^{24}, u^{25} + 2u^{24} + \dots - 18u + 5 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_3 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} a \\ -0.715728au^{24} - 1.87471u^{24} + \dots + 6.98979a + 18.6997 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 2.87565au^{24} - 3.09074u^{24} + \dots - 30.7439a + 31.3997 \\ 0.805852au^{24} + 1.72660u^{24} + \dots - 8.29141a - 17.8506 \end{pmatrix} \\ a_2 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 0.715728au^{24} + 1.87471u^{24} + \dots - 5.98979a - 18.6997 \\ -0.387518au^{24} - 1.63688u^{24} + \dots + 3.57864a + 19.9274 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -0.715728au^{24} - 1.87471u^{24} + \dots + 7.98979a + 18.6997 \\ -0.715728au^{24} - 1.87471u^{24} + \dots + 6.98979a + 18.6997 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -1.39796au^{24} - 5.76946u^{24} + \dots + 13.0810a + 58.4354 \\ 0.379318u^{24} + 0.946149u^{23} + \dots - 2.74341u - 5.54920 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -1.65828au^{24} + 2.07471u^{24} + \dots + 16.7481a - 22.2997 \\ -1.25756au^{24} + 3.83734u^{24} + \dots + 14.3782a - 42.0842 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -1.39796au^{24} - 5.76946u^{24} + \dots + 13.0810a + 58.4354 \\ -0.387518au^{24} - 0.813602u^{24} + \dots + 3.57864a + 7.89146 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -1.39796au^{24} - 5.76946u^{24} + \dots + 13.0810a + 58.4354 \\ -0.387518au^{24} - 0.813602u^{24} + \dots + 3.57864a + 7.89146 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -\frac{1156952596349356967504}{1993212416684380527497}u^{24} - \frac{3249366973641059899377}{1993212416684380527497}u^{23} + \dots - \frac{66879505468638485855810}{1993212416684380527497}u + \frac{10075785679097148312488}{1993212416684380527497}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_6$	$u^{50} + 5u^{49} + \cdots + 337800u + 93608$
$c_2, c_5$	$(u^{25} + 2u^{24} + \cdots - 18u + 5)^2$
$c_3, c_4$	$u^{50} - 4u^{49} + \cdots + 5u - 1$
$c_7, c_{11}$	$u^{50} - u^{49} + \cdots + 22u - 1$
$c_8, c_{10}$	$u^{50} + 3u^{48} + \cdots - 10342u - 3931$
$c_9$	$(u^{25} - u^{24} + \cdots - 18u + 31)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$y^{50} + 13y^{49} + \cdots + 42553508800y + 8762457664$
$c_2, c_5$	$(y^{25} + 24y^{24} + \cdots - 336y - 25)^2$
$c_3, c_4$	$y^{50} + 18y^{48} + \cdots + 143y + 1$
$c_7, c_{11}$	$y^{50} - 21y^{49} + \cdots + 244y + 1$
$c_8, c_{10}$	$y^{50} + 6y^{49} + \cdots + 33112428y + 15452761$
$c_9$	$(y^{25} - 17y^{24} + \cdots + 12662y - 961)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.140650 + 0.267150I$		
$a = 1.084710 + 0.611862I$	$-1.03856 + 1.14326I$	$-10.5893 + 12.6521I$
$b = 1.49229 + 0.92382I$		
$u = -1.140650 + 0.267150I$		
$a = 0.113359 + 0.355439I$	$-1.03856 + 1.14326I$	$-10.5893 + 12.6521I$
$b = 0.633787 + 0.654814I$		
$u = -1.140650 - 0.267150I$		
$a = 1.084710 - 0.611862I$	$-1.03856 - 1.14326I$	$-10.5893 - 12.6521I$
$b = 1.49229 - 0.92382I$		
$u = -1.140650 - 0.267150I$		
$a = 0.113359 - 0.355439I$	$-1.03856 - 1.14326I$	$-10.5893 - 12.6521I$
$b = 0.633787 - 0.654814I$		
$u = -0.163146 + 1.252380I$		
$a = -0.356875 - 0.754522I$	$2.89680 + 2.76831I$	$-5.67436 - 1.24863I$
$b = -0.959590 + 0.451959I$		
$u = -0.163146 + 1.252380I$		
$a = 0.223215 - 1.350440I$	$2.89680 + 2.76831I$	$-5.67436 - 1.24863I$
$b = -0.670798 + 0.653559I$		
$u = -0.163146 - 1.252380I$		
$a = -0.356875 + 0.754522I$	$2.89680 - 2.76831I$	$-5.67436 + 1.24863I$
$b = -0.959590 - 0.451959I$		
$u = -0.163146 - 1.252380I$		
$a = 0.223215 + 1.350440I$	$2.89680 - 2.76831I$	$-5.67436 + 1.24863I$
$b = -0.670798 - 0.653559I$		
$u = 0.434385 + 1.315760I$		
$a = -0.676723 + 0.897603I$	$6.24414 - 3.55600I$	$4.03991 + 3.49531I$
$b = -0.451415 - 0.840386I$		
$u = 0.434385 + 1.315760I$		
$a = 0.14272 - 1.58350I$	$6.24414 - 3.55600I$	$4.03991 + 3.49531I$
$b = 1.25444 + 1.50173I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.434385 - 1.315760I$		
$a = -0.676723 - 0.897603I$	$6.24414 + 3.55600I$	$4.03991 - 3.49531I$
$b = -0.451415 + 0.840386I$		
$u = 0.434385 - 1.315760I$		
$a = 0.14272 + 1.58350I$	$6.24414 + 3.55600I$	$4.03991 - 3.49531I$
$b = 1.25444 - 1.50173I$		
$u = 0.15084 + 1.44113I$		
$a = -0.365971 - 1.348100I$	$6.70056 - 6.60168I$	$4.95046 + 12.30292I$
$b = 1.12800 + 1.43516I$		
$u = 0.15084 + 1.44113I$		
$a = 0.23756 + 1.60715I$	$6.70056 - 6.60168I$	$4.95046 + 12.30292I$
$b = -0.035729 - 0.763533I$		
$u = 0.15084 - 1.44113I$		
$a = -0.365971 + 1.348100I$	$6.70056 + 6.60168I$	$4.95046 - 12.30292I$
$b = 1.12800 - 1.43516I$		
$u = 0.15084 - 1.44113I$		
$a = 0.23756 - 1.60715I$	$6.70056 + 6.60168I$	$4.95046 - 12.30292I$
$b = -0.035729 + 0.763533I$		
$u = -0.148436 + 0.506372I$		
$a = 0.388829 + 0.383713I$	$-2.53372 + 0.16719I$	$-3.64574 - 0.21536I$
$b = 1.118110 - 0.274856I$		
$u = -0.148436 + 0.506372I$		
$a = 3.02455 + 0.27470I$	$-2.53372 + 0.16719I$	$-3.64574 - 0.21536I$
$b = -0.251824 - 0.797330I$		
$u = -0.148436 - 0.506372I$		
$a = 0.388829 - 0.383713I$	$-2.53372 - 0.16719I$	$-3.64574 + 0.21536I$
$b = 1.118110 + 0.274856I$		
$u = -0.148436 - 0.506372I$		
$a = 3.02455 - 0.27470I$	$-2.53372 - 0.16719I$	$-3.64574 + 0.21536I$
$b = -0.251824 + 0.797330I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.475339$		
$a = 0.528924 + 0.781882I$	2.81112	0.202280
$b = -0.430675 + 0.809478I$		
$u = 0.475339$		
$a = 0.528924 - 0.781882I$	2.81112	0.202280
$b = -0.430675 - 0.809478I$		
$u = -1.53222$		
$a = 0.078790 + 0.191294I$	3.05217	0.159530
$b = 0.568791 - 1.033300I$		
$u = -1.53222$		
$a = 0.078790 - 0.191294I$	3.05217	0.159530
$b = 0.568791 + 1.033300I$		
$u = 0.466383 + 0.024974I$		
$a = 0.624833 - 0.860638I$	1.53850 - 4.51240I	-4.65188 + 7.14304I
$b = -0.840463 - 0.646691I$		
$u = 0.466383 + 0.024974I$		
$a = 1.42335 - 2.52636I$	1.53850 - 4.51240I	-4.65188 + 7.14304I
$b = 0.735817 + 0.431578I$		
$u = 0.466383 - 0.024974I$		
$a = 0.624833 + 0.860638I$	1.53850 + 4.51240I	-4.65188 - 7.14304I
$b = -0.840463 + 0.646691I$		
$u = 0.466383 - 0.024974I$		
$a = 1.42335 + 2.52636I$	1.53850 + 4.51240I	-4.65188 - 7.14304I
$b = 0.735817 - 0.431578I$		
$u = 1.54406$		
$a = -0.230436$	-6.61075	-51.2600
$b = 0.365605$		
$u = 1.54406$		
$a = -1.77941$	-6.61075	-51.2600
$b = -1.23498$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.18525 + 1.56503I$		
$a = -0.482316 - 0.856149I$	$3.52121 - 5.29385I$	$-3.74916 + 8.30350I$
$b = 0.583599 + 0.895127I$		
$u = -0.18525 + 1.56503I$		
$a = 0.672798 - 0.276435I$	$3.52121 - 5.29385I$	$-3.74916 + 8.30350I$
$b = 1.161330 + 0.309043I$		
$u = -0.18525 - 1.56503I$		
$a = -0.482316 + 0.856149I$	$3.52121 + 5.29385I$	$-3.74916 - 8.30350I$
$b = 0.583599 - 0.895127I$		
$u = -0.18525 - 1.56503I$		
$a = 0.672798 + 0.276435I$	$3.52121 + 5.29385I$	$-3.74916 - 8.30350I$
$b = 1.161330 - 0.309043I$		
$u = 0.003969 + 0.337154I$		
$a = 0.650002 + 0.785649I$	$-0.56308 + 6.78110I$	$3.38343 - 3.19298I$
$b = -1.171020 + 0.504584I$		
$u = 0.003969 + 0.337154I$		
$a = 7.17919 - 1.72929I$	$-0.56308 + 6.78110I$	$3.38343 - 3.19298I$
$b = -0.074163 + 0.750946I$		
$u = 0.003969 - 0.337154I$		
$a = 0.650002 - 0.785649I$	$-0.56308 - 6.78110I$	$3.38343 + 3.19298I$
$b = -1.171020 - 0.504584I$		
$u = 0.003969 - 0.337154I$		
$a = 7.17919 + 1.72929I$	$-0.56308 - 6.78110I$	$3.38343 + 3.19298I$
$b = -0.074163 - 0.750946I$		
$u = 0.19448 + 1.65842I$		
$a = 0.422264 - 0.836955I$	$7.41514 + 1.27639I$	$2.55128 - 0.67478I$
$b = -1.43214 + 1.44496I$		
$u = 0.19448 + 1.65842I$		
$a = -0.325781 + 0.877177I$	$7.41514 + 1.27639I$	$2.55128 - 0.67478I$
$b = -0.010779 - 1.084000I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.19448 - 1.65842I$		
$a = 0.422264 + 0.836955I$	$7.41514 - 1.27639I$	$2.55128 + 0.67478I$
$b = -1.43214 - 1.44496I$		
$u = 0.19448 - 1.65842I$		
$a = -0.325781 - 0.877177I$	$7.41514 - 1.27639I$	$2.55128 + 0.67478I$
$b = -0.010779 + 1.084000I$		
$u = -0.08719 + 1.73481I$		
$a = 0.436377 + 0.874340I$	$7.66608 + 6.24371I$	$4.09267 - 6.21663I$
$b = -1.81263 - 1.76872I$		
$u = -0.08719 + 1.73481I$		
$a = -0.211132 + 1.015010I$	$7.66608 + 6.24371I$	$4.09267 - 6.21663I$
$b = 0.62955 - 1.66105I$		
$u = -0.08719 - 1.73481I$		
$a = 0.436377 - 0.874340I$	$7.66608 - 6.24371I$	$4.09267 + 6.21663I$
$b = -1.81263 + 1.76872I$		
$u = -0.08719 - 1.73481I$		
$a = -0.211132 - 1.015010I$	$7.66608 - 6.24371I$	$4.09267 + 6.21663I$
$b = 0.62955 + 1.66105I$		
$u = -0.76896 + 1.70316I$		
$a = -0.267227 - 1.109740I$	$8.00509 + 8.45240I$	$0. - 6.49999I$
$b = -1.14143 + 1.30331I$		
$u = -0.76896 + 1.70316I$		
$a = 0.259474 + 0.720363I$	$8.00509 + 8.45240I$	$0. - 6.49999I$
$b = 0.411624 - 1.049270I$		
$u = -0.76896 - 1.70316I$		
$a = -0.267227 + 1.109740I$	$8.00509 - 8.45240I$	$0. + 6.49999I$
$b = -1.14143 - 1.30331I$		
$u = -0.76896 - 1.70316I$		
$a = 0.259474 - 0.720363I$	$8.00509 - 8.45240I$	$0. + 6.49999I$
$b = 0.411624 + 1.049270I$		

$$\text{III. } I_3^u = \langle -498u^9a + 411u^9 + \cdots - 538a - 71, 33u^9a - 50u^9 + \cdots + 36a + 14, u^{10} + u^9 + \cdots + 4u^2 - 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_3 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} a \\ 0.256305au^9 - 0.211529u^9 + \cdots + 0.276891a + 0.0365414 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -0.202265au^9 + 0.388574u^9 + \cdots + 1.23932a + 1.61657 \\ -0.128667au^9 - 0.533196u^9 + \cdots - 0.0386001a + 0.440041 \end{pmatrix} \\ a_2 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 0.256305au^9 - 0.211529u^9 + \cdots - 0.723109a + 0.0365414 \\ 0.145651au^9 + 1.11889u^9 + \cdots - 0.256305a + 0.935666 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0.256305au^9 - 0.211529u^9 + \cdots + 1.27689a + 0.0365414 \\ 0.256305au^9 - 0.211529u^9 + \cdots + 0.276891a + 0.0365414 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -0.276891au^9 + 0.446217u^9 + \cdots - 0.283067a - 0.566135 \\ -0.793103u^9 - 1.10345u^8 + \cdots - 1.24138u - 1.13793 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 0.0386001au^9 + 0.594442u^9 + \cdots + 0.511580a - 0.321668 \\ -0.325785au^9 - 0.513639u^9 + \cdots + 0.202265a - 0.354092 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -0.276891au^9 + 0.446217u^9 + \cdots - 0.283067a - 0.566135 \\ 0.145651au^9 - 0.501801u^9 + \cdots - 0.256305a - 1.65054 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -0.276891au^9 + 0.446217u^9 + \cdots - 0.283067a - 0.566135 \\ 0.145651au^9 - 0.501801u^9 + \cdots - 0.256305a - 1.65054 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes**

$$= -\frac{70}{29}u^9 - \frac{139}{29}u^8 - \frac{166}{29}u^7 + 2u^6 + \frac{490}{29}u^5 + \frac{1077}{29}u^4 + \frac{738}{29}u^3 + \frac{413}{29}u^2 - \frac{44}{29}u - \frac{485}{29}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{20} - 4u^{19} + \cdots + 24u + 8$
$c_2$	$(u^{10} - u^9 + u^8 + u^7 - 7u^6 + 6u^5 - 4u^4 + u^3 + 4u^2 - 1)^2$
$c_3$	$u^{20} + 7u^{19} + \cdots - u - 1$
$c_4$	$u^{20} - 7u^{19} + \cdots + u - 1$
$c_5$	$(u^{10} + u^9 + u^8 - u^7 - 7u^6 - 6u^5 - 4u^4 - u^3 + 4u^2 - 1)^2$
$c_6$	$u^{20} + 4u^{19} + \cdots - 24u + 8$
$c_7$	$u^{20} + 6u^{19} + \cdots + 8u + 1$
$c_8$	$u^{20} + u^{19} + \cdots - 4u - 1$
$c_9$	$u^{20} - 4u^{18} + \cdots + 146u^2 - 31$
$c_{10}$	$u^{20} - u^{19} + \cdots + 4u - 1$
$c_{11}$	$u^{20} - 6u^{19} + \cdots - 8u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$y^{20} - 10y^{19} + \cdots + 832y + 64$
$c_2, c_5$	$(y^{10} + y^9 - 11y^8 - 11y^7 + 39y^6 + 24y^5 - 54y^4 - 19y^3 + 24y^2 - 8y + 1)^2$
$c_3, c_4$	$y^{20} - 9y^{19} + \cdots + 7y + 1$
$c_7, c_{11}$	$y^{20} - 2y^{19} + \cdots - 14y + 1$
$c_8, c_{10}$	$y^{20} - y^{19} + \cdots - 22y + 1$
$c_9$	$(y^{10} - 4y^9 + \cdots + 146y - 31)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.162027 + 1.093500I$		
$a = -0.593689 + 0.666269I$	$3.13638 - 3.94572I$	$-1.58269 + 5.47828I$
$b = -0.965025 - 0.562961I$		
$u = -0.162027 + 1.093500I$		
$a = 0.91912 + 1.26340I$	$3.13638 - 3.94572I$	$-1.58269 + 5.47828I$
$b = -0.554998 - 0.469577I$		
$u = -0.162027 - 1.093500I$		
$a = -0.593689 - 0.666269I$	$3.13638 + 3.94572I$	$-1.58269 - 5.47828I$
$b = -0.965025 + 0.562961I$		
$u = -0.162027 - 1.093500I$		
$a = 0.91912 - 1.26340I$	$3.13638 + 3.94572I$	$-1.58269 - 5.47828I$
$b = -0.554998 + 0.469577I$		
$u = -1.184430 + 0.161063I$		
$a = -1.044950 - 0.712567I$	$-0.91356 + 1.34180I$	$8.0489 - 15.8298I$
$b = -1.47068 - 1.35942I$		
$u = -1.184430 + 0.161063I$		
$a = 0.266174 + 0.351567I$	$-0.91356 + 1.34180I$	$8.0489 - 15.8298I$
$b = 0.614102 + 0.689658I$		
$u = -1.184430 - 0.161063I$		
$a = -1.044950 + 0.712567I$	$-0.91356 - 1.34180I$	$8.0489 + 15.8298I$
$b = -1.47068 + 1.35942I$		
$u = -1.184430 - 0.161063I$		
$a = 0.266174 - 0.351567I$	$-0.91356 - 1.34180I$	$8.0489 + 15.8298I$
$b = 0.614102 - 0.689658I$		
$u = 0.493258 + 0.211168I$		
$a = 0.030687 + 0.614200I$	$-0.98335 - 6.94564I$	$-13.6667 + 10.0962I$
$b = -1.053900 - 0.481170I$		
$u = 0.493258 + 0.211168I$		
$a = 1.07089 + 4.10487I$	$-0.98335 - 6.94564I$	$-13.6667 + 10.0962I$
$b = 0.278877 + 0.531389I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.493258 - 0.211168I$		
$a = 0.030687 - 0.614200I$	$-0.98335 + 6.94564I$	$-13.6667 - 10.0962I$
$b = -1.053900 + 0.481170I$		
$u = 0.493258 - 0.211168I$		
$a = 1.07089 - 4.10487I$	$-0.98335 + 6.94564I$	$-13.6667 - 10.0962I$
$b = 0.278877 - 0.531389I$		
$u = -0.510374$		
$a = -0.34052 + 1.84999I$	$-3.56392$	$-13.6180$
$b = 0.789530 + 0.525018I$		
$u = -0.510374$		
$a = -0.34052 - 1.84999I$	$-3.56392$	$-13.6180$
$b = 0.789530 - 0.525018I$		
$u = -0.19822 + 1.54173I$		
$a = -0.059083 - 1.131320I$	$6.26864 + 5.98904I$	$-2.92384 - 3.18632I$
$b = 0.371545 + 1.039520I$		
$u = -0.19822 + 1.54173I$		
$a = -0.222760 + 1.238820I$	$6.26864 + 5.98904I$	$-2.92384 - 3.18632I$
$b = 0.96108 - 1.49878I$		
$u = -0.19822 - 1.54173I$		
$a = -0.059083 + 1.131320I$	$6.26864 - 5.98904I$	$-2.92384 + 3.18632I$
$b = 0.371545 - 1.039520I$		
$u = -0.19822 - 1.54173I$		
$a = -0.222760 - 1.238820I$	$6.26864 - 5.98904I$	$-2.92384 + 3.18632I$
$b = 0.96108 + 1.49878I$		
$u = 1.61322$		
$a = 1.68819$	$-6.51752$	$34.8670$
$b = 1.26726$		
$u = 1.61322$		
$a = 0.260087$	$-6.51752$	$34.8670$
$b = -0.208312$		

$$\text{IV. } I_4^u = \langle b + u, a - u + 1, u^3 + u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_3 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u - 1 \\ -u \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u^2 - 1 \\ u^2 + 1 \end{pmatrix} \\ a_2 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} u^2 - u + 2 \\ -u^2 + u - 1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -1 \\ -u \end{pmatrix} \\ a_8 &= \begin{pmatrix} -1 \\ u^2 - u \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u^2 + u - 1 \\ 1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -1 \\ -u \end{pmatrix} \\ a_9 &= \begin{pmatrix} -1 \\ -u \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-8u^2 + 4u - 11$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$u^3 + u^2 + 1$
$c_2, c_8$	$u^3 + u - 1$
$c_4, c_6$	$u^3 - u^2 - 1$
$c_5, c_{10}$	$u^3 + u + 1$
$c_7$	$u^3 + 2u^2 + u - 1$
$c_9$	$u^3$
$c_{11}$	$u^3 - 2u^2 + u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_6$	$y^3 - y^2 - 2y - 1$
$c_2, c_5, c_8$ $c_{10}$	$y^3 + 2y^2 + y - 1$
$c_7, c_{11}$	$y^3 - 2y^2 + 5y - 1$
$c_9$	$y^3$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.341164 + 1.161540I$		
$a = -0.658836 + 1.161540I$	$5.50124 - 1.58317I$	$0.22694 - 1.69425I$
$b = -0.341164 - 1.161540I$		
$u = 0.341164 - 1.161540I$		
$a = -0.658836 - 1.161540I$	$5.50124 + 1.58317I$	$0.22694 + 1.69425I$
$b = -0.341164 + 1.161540I$		
$u = -0.682328$		
$a = -1.68233$	$-4.42273$	$-17.4540$
$b = 0.682328$		

## V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^3 + u^2 + 1)(u^{20} - 5u^{19} + \dots + 24u - 8)(u^{20} - 4u^{19} + \dots + 24u + 8)$ $\cdot (u^{50} + 5u^{49} + \dots + 337800u + 93608)$
$c_2$	$(u^3 + u - 1)(u^{10} - u^9 + u^8 + u^7 - 7u^6 + 6u^5 - 4u^4 + u^3 + 4u^2 - 1)^2$ $\cdot (u^{20} - 3u^{19} + \dots + 50u + 28)(u^{25} + 2u^{24} + \dots - 18u + 5)^2$
$c_3$	$(u^3 + u^2 + 1)(u^{20} - u^{19} + \dots - 3u^2 + 1)(u^{20} + 7u^{19} + \dots - u - 1)$ $\cdot (u^{50} - 4u^{49} + \dots + 5u - 1)$
$c_4$	$(u^3 - u^2 - 1)(u^{20} - 7u^{19} + \dots + u - 1)(u^{20} - u^{19} + \dots - 3u^2 + 1)$ $\cdot (u^{50} - 4u^{49} + \dots + 5u - 1)$
$c_5$	$(u^3 + u + 1)(u^{10} + u^9 + u^8 - u^7 - 7u^6 - 6u^5 - 4u^4 - u^3 + 4u^2 - 1)^2$ $\cdot (u^{20} - 3u^{19} + \dots + 50u + 28)(u^{25} + 2u^{24} + \dots - 18u + 5)^2$
$c_6$	$(u^3 - u^2 - 1)(u^{20} - 5u^{19} + \dots + 24u - 8)(u^{20} + 4u^{19} + \dots - 24u + 8)$ $\cdot (u^{50} + 5u^{49} + \dots + 337800u + 93608)$
$c_7$	$(u^3 + 2u^2 + u - 1)(u^{20} - 2u^{19} + \dots - 5u - 1)(u^{20} + 6u^{19} + \dots + 8u + 1)$ $\cdot (u^{50} - u^{49} + \dots + 22u - 1)$
$c_8$	$(u^3 + u - 1)(u^{20} + 9u^{18} + \dots + 5u - 1)(u^{20} + u^{19} + \dots - 4u - 1)$ $\cdot (u^{50} + 3u^{48} + \dots - 10342u - 3931)$
$c_9$	$u^3(u^{20} - 4u^{18} + \dots + 146u^2 - 31)(u^{20} + 5u^{19} + \dots + 192u + 32)$ $\cdot (u^{25} - u^{24} + \dots - 18u + 31)^2$
$c_{10}$	$(u^3 + u + 1)(u^{20} + 9u^{18} + \dots + 5u - 1)(u^{20} - u^{19} + \dots + 4u - 1)$ $\cdot (u^{50} + 3u^{48} + \dots - 10342u - 3931)$
$c_{11}$	$(u^3 - 2u^2 + u + 1)(u^{20} - 6u^{19} + \dots - 8u + 1)(u^{20} - 2u^{19} + \dots - 5u - 1)$ $\cdot (u^{50} - u^{49} + \dots + 22u - 1)$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$(y^3 - y^2 - 2y - 1)(y^{20} - 10y^{19} + \dots + 832y + 64)$ $\cdot (y^{20} + 19y^{19} + \dots + 384y + 64)$ $\cdot (y^{50} + 13y^{49} + \dots + 42553508800y + 8762457664)$
$c_2, c_5$	$(y^3 + 2y^2 + y - 1)$ $\cdot (y^{10} + y^9 - 11y^8 - 11y^7 + 39y^6 + 24y^5 - 54y^4 - 19y^3 + 24y^2 - 8y + 1)^2$ $\cdot (y^{20} + 11y^{19} + \dots + 6180y + 784)(y^{25} + 24y^{24} + \dots - 336y - 25)^2$
$c_3, c_4$	$(y^3 - y^2 - 2y - 1)(y^{20} - 9y^{19} + \dots + 7y + 1)(y^{20} - 3y^{19} + \dots - 6y + 1)$ $\cdot (y^{50} + 18y^{48} + \dots + 143y + 1)$
$c_7, c_{11}$	$(y^3 - 2y^2 + 5y - 1)(y^{20} + 24y^{18} + \dots - 79y + 1)$ $\cdot (y^{20} - 2y^{19} + \dots - 14y + 1)(y^{50} - 21y^{49} + \dots + 244y + 1)$
$c_8, c_{10}$	$(y^3 + 2y^2 + y - 1)(y^{20} - y^{19} + \dots - 22y + 1)$ $\cdot (y^{20} + 18y^{19} + \dots + 13y + 1)$ $\cdot (y^{50} + 6y^{49} + \dots + 33112428y + 15452761)$
$c_9$	$y^3(y^{10} - 4y^9 + \dots + 146y - 31)^2(y^{20} + y^{19} + \dots - 14336y + 1024)$ $\cdot (y^{25} - 17y^{24} + \dots + 12662y - 961)^2$