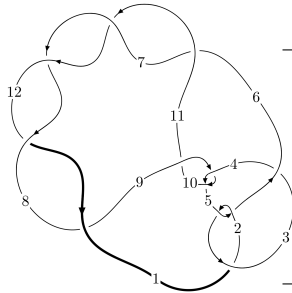
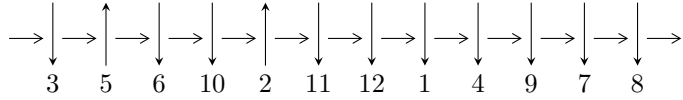


12a<sub>0034</sub> (K12a<sub>0034</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$7,12 \xrightarrow{c_7} 8 \xrightarrow{c_{12}} 1,3 \xrightarrow{c_1} 2 \xrightarrow{c_8} 9 \xrightarrow{c_{11}} 11 \xrightarrow{c_6} 6 \xrightarrow{c_3} 4 \xrightarrow{c_5} 5 \xrightarrow{c_{10}} 10 \rightsquigarrow c_2, c_4, c_9$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -11u^{60} + 15u^{59} + \dots + 2b + 7, -8u^{60} + 9u^{59} + \dots + 2a + 7, u^{61} - 3u^{60} + \dots + u + 1 \rangle$$

$$I_2^u = \langle au + b - a, a^2 + au + a + u + 2, u^2 + u - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 65 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\langle -11u^{60} + 15u^{59} + \dots + 2b + 7, -8u^{60} + 9u^{59} + \dots + 2a + 7, u^{61} - 3u^{60} + \dots + u + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 4u^{60} - \frac{9}{2}u^{59} + \dots - 6u - \frac{7}{2} \\ \frac{11}{2}u^{60} - \frac{15}{2}u^{59} + \dots - \frac{11}{2}u - \frac{7}{2} \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -\frac{1}{2}u^{59} + u^{58} + \dots + 6u - \frac{1}{2} \\ -\frac{1}{2}u^{60} + \frac{1}{2}u^{59} + \dots + \frac{5}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} \frac{19}{2}u^{60} - 12u^{59} + \dots - \frac{21}{2}u - 6 \\ \frac{27}{2}u^{60} - 18u^{59} + \dots - \frac{25}{2}u - 8 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -\frac{7}{2}u^{60} + 5u^{59} + \dots + \frac{5}{2}u + 2 \\ -\frac{15}{2}u^{60} + 10u^{59} + \dots + \frac{15}{2}u + 4 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^7 + 4u^5 - 4u^3 + 2u \\ -u^9 + 5u^7 - 7u^5 + 2u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = -\frac{5}{2}u^{60} + 95u^{58} + \dots - \frac{29}{2}u - 5$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{61} + 29u^{60} + \dots + 23u - 1$
$c_2, c_5$	$u^{61} + 3u^{60} + \dots + 9u + 1$
$c_3$	$u^{61} - 3u^{60} + \dots - 129u + 241$
$c_4, c_9$	$u^{61} + u^{60} + \dots - 48u - 16$
$c_6, c_7, c_8$ $c_{11}, c_{12}$	$u^{61} + 3u^{60} + \dots + u - 1$
$c_{10}$	$u^{61} + 25u^{60} + \dots + 2432u + 256$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{61} + 9y^{60} + \dots + 707y - 1$
$c_2, c_5$	$y^{61} + 29y^{60} + \dots + 23y - 1$
$c_3$	$y^{61} - 11y^{60} + \dots + 2638239y - 58081$
$c_4, c_9$	$y^{61} - 25y^{60} + \dots + 2432y - 256$
$c_6, c_7, c_8$ $c_{11}, c_{12}$	$y^{61} - 79y^{60} + \dots + 19y - 1$
$c_{10}$	$y^{61} + 15y^{60} + \dots + 2564096y - 65536$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.941549 + 0.362904I$ $a = -0.926027 - 0.288989I$ $b = 0.684803 + 0.361766I$	$-1.57693 + 6.68347I$	0
$u = -0.941549 - 0.362904I$ $a = -0.926027 + 0.288989I$ $b = 0.684803 - 0.361766I$	$-1.57693 - 6.68347I$	0
$u = -0.962161 + 0.388897I$ $a = 1.091940 + 0.880454I$ $b = -0.891980 - 0.179165I$	$-3.85828 + 11.82190I$	0
$u = -0.962161 - 0.388897I$ $a = 1.091940 - 0.880454I$ $b = -0.891980 + 0.179165I$	$-3.85828 - 11.82190I$	0
$u = -0.991302 + 0.313503I$ $a = -0.066752 + 0.371102I$ $b = -0.789116 - 0.780549I$	$-6.39349 + 4.01306I$	0
$u = -0.991302 - 0.313503I$ $a = -0.066752 - 0.371102I$ $b = -0.789116 + 0.780549I$	$-6.39349 - 4.01306I$	0
$u = 0.907581 + 0.284646I$ $a = -1.43188 + 0.77881I$ $b = 1.194390 - 0.037845I$	$-1.92448 - 5.85744I$	0
$u = 0.907581 - 0.284646I$ $a = -1.43188 - 0.77881I$ $b = 1.194390 + 0.037845I$	$-1.92448 + 5.85744I$	0
$u = -1.06207$ $a = -0.867883$ $b = 0.339270$	$-5.58398$	0
$u = 0.916155 + 0.124387I$ $a = -0.395310 + 0.861467I$ $b = 0.790911 - 1.053260I$	$-3.56819 + 0.84716I$	$-15.9906 + 0.I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.916155 - 0.124387I$ $a = -0.395310 - 0.861467I$ $b = 0.790911 + 1.053260I$	$-3.56819 - 0.84716I$	$-15.9906 + 0.I$
$u = -0.858548 + 0.285771I$ $a = -0.240294 + 1.130700I$ $b = 0.426613 + 0.684373I$	$-0.14613 + 4.14771I$	$-8.00000 - 7.53022I$
$u = -0.858548 - 0.285771I$ $a = -0.240294 - 1.130700I$ $b = 0.426613 - 0.684373I$	$-0.14613 - 4.14771I$	$-8.00000 + 7.53022I$
$u = 0.833612 + 0.279640I$ $a = 1.133180 - 0.204262I$ $b = -0.769914 + 0.142240I$	$0.014847 - 1.230250I$	$-8.00000 + 2.00002I$
$u = 0.833612 - 0.279640I$ $a = 1.133180 + 0.204262I$ $b = -0.769914 - 0.142240I$	$0.014847 + 1.230250I$	$-8.00000 - 2.00002I$
$u = -1.138410 + 0.086480I$ $a = 0.760786 + 0.178531I$ $b = -0.780459 + 0.648714I$	$-8.82704 + 3.92280I$	0
$u = -1.138410 - 0.086480I$ $a = 0.760786 - 0.178531I$ $b = -0.780459 - 0.648714I$	$-8.82704 - 3.92280I$	0
$u = -0.819047 + 0.217033I$ $a = -0.57338 - 1.48189I$ $b = -0.544215 - 0.744173I$	$-1.09072 - 0.91618I$	$-13.20392 - 2.90788I$
$u = -0.819047 - 0.217033I$ $a = -0.57338 + 1.48189I$ $b = -0.544215 + 0.744173I$	$-1.09072 + 0.91618I$	$-13.20392 + 2.90788I$
$u = 0.651545 + 0.456443I$ $a = 0.43685 - 1.47583I$ $b = 0.607385 - 0.419645I$	$-2.01345 + 4.76879I$	$-12.80458 - 3.25405I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.651545 - 0.456443I$		
$a = 0.43685 + 1.47583I$	$-2.01345 - 4.76879I$	$-12.80458 + 3.25405I$
$b = 0.607385 + 0.419645I$		
$u = 0.672132 + 0.371659I$		
$a = 0.204778 + 0.807835I$	$0.006977 + 0.191932I$	$-9.14973 + 0.93355I$
$b = -0.503235 + 0.231907I$		
$u = 0.672132 - 0.371659I$		
$a = 0.204778 - 0.807835I$	$0.006977 - 0.191932I$	$-9.14973 - 0.93355I$
$b = -0.503235 - 0.231907I$		
$u = 0.486313 + 0.449825I$		
$a = 1.064050 + 0.128423I$	$-3.44842 - 2.18500I$	$-15.5614 + 4.6731I$
$b = 0.750517 + 0.088709I$		
$u = 0.486313 - 0.449825I$		
$a = 1.064050 - 0.128423I$	$-3.44842 + 2.18500I$	$-15.5614 - 4.6731I$
$b = 0.750517 - 0.088709I$		
$u = 0.142006 + 0.624563I$		
$a = 0.949731 - 0.841604I$	$-0.47167 - 8.39775I$	$-9.16009 + 8.05408I$
$b = 1.063740 + 0.386697I$		
$u = 0.142006 - 0.624563I$		
$a = 0.949731 + 0.841604I$	$-0.47167 + 8.39775I$	$-9.16009 - 8.05408I$
$b = 1.063740 - 0.386697I$		
$u = 0.119463 + 0.584881I$		
$a = -0.402048 + 0.694739I$	$1.67223 - 3.47107I$	$-5.43201 + 4.12123I$
$b = -0.574572 - 0.527063I$		
$u = 0.119463 - 0.584881I$		
$a = -0.402048 - 0.694739I$	$1.67223 + 3.47107I$	$-5.43201 - 4.12123I$
$b = -0.574572 + 0.527063I$		
$u = 0.222473 + 0.540240I$		
$a = 0.01204 - 1.43662I$	$-2.65865 - 1.12584I$	$-12.84225 + 3.10905I$
$b = 0.230433 - 0.262534I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.222473 - 0.540240I$ $a = 0.01204 + 1.43662I$ $b = 0.230433 + 0.262534I$	$-2.65865 + 1.12584I$	$-12.84225 - 3.10905I$
$u = 0.011799 + 0.502580I$ $a = 0.736143 + 0.780204I$ $b = 0.443073 - 0.686495I$	$2.47447 - 1.45390I$	$-2.95032 + 3.27697I$
$u = 0.011799 - 0.502580I$ $a = 0.736143 - 0.780204I$ $b = 0.443073 + 0.686495I$	$2.47447 + 1.45390I$	$-2.95032 - 3.27697I$
$u = -0.071181 + 0.471890I$ $a = -1.39302 - 1.27147I$ $b = -0.971413 + 0.506703I$	$1.06320 + 3.26175I$	$-5.16927 - 3.30010I$
$u = -0.071181 - 0.471890I$ $a = -1.39302 + 1.27147I$ $b = -0.971413 - 0.506703I$	$1.06320 - 3.26175I$	$-5.16927 + 3.30010I$
$u = 0.441573$ $a = 0.291655$ $b = -0.318830$	$-0.703516$	$-13.9150$
$u = -1.57089 + 0.05487I$ $a = -0.108181 - 0.454338I$ $b = -0.73199 - 1.31069I$	$-9.35339 - 3.05356I$	0
$u = -1.57089 - 0.05487I$ $a = -0.108181 + 0.454338I$ $b = -0.73199 + 1.31069I$	$-9.35339 + 3.05356I$	0
$u = -1.62164 + 0.05572I$ $a = -0.661023 + 0.422089I$ $b = -1.01599 + 1.16132I$	$-7.88099 + 1.12428I$	0
$u = -1.62164 - 0.05572I$ $a = -0.661023 - 0.422089I$ $b = -1.01599 - 1.16132I$	$-7.88099 - 1.12428I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.67660 + 0.06327I$ $a = -2.46813 - 0.26761I$ $b = -4.28495 - 0.21565I$	$-8.84015 + 2.47805I$	0
$u = -1.67660 - 0.06327I$ $a = -2.46813 + 0.26761I$ $b = -4.28495 + 0.21565I$	$-8.84015 - 2.47805I$	0
$u = 1.67898 + 0.05115I$ $a = 0.276936 - 0.341290I$ $b = 0.80641 - 1.34802I$	$-9.96853 - 0.06844I$	0
$u = 1.67898 - 0.05115I$ $a = 0.276936 + 0.341290I$ $b = 0.80641 + 1.34802I$	$-9.96853 + 0.06844I$	0
$u = 1.68198 + 0.06781I$ $a = 0.485407 + 0.293294I$ $b = 0.76562 + 1.24151I$	$-9.10899 - 5.46550I$	0
$u = 1.68198 - 0.06781I$ $a = 0.485407 - 0.293294I$ $b = 0.76562 - 1.24151I$	$-9.10899 + 5.46550I$	0
$u = -1.69350 + 0.07169I$ $a = 3.58656 + 0.38893I$ $b = 6.19427 + 0.54411I$	$-11.11280 + 7.23397I$	0
$u = -1.69350 - 0.07169I$ $a = 3.58656 - 0.38893I$ $b = 6.19427 - 0.54411I$	$-11.11280 - 7.23397I$	0
$u = -1.69643 + 0.03492I$ $a = 2.03123 + 2.16248I$ $b = 3.41894 + 3.43232I$	$-12.85740 - 0.20377I$	0
$u = -1.69643 - 0.03492I$ $a = 2.03123 - 2.16248I$ $b = 3.41894 - 3.43232I$	$-12.85740 + 0.20377I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.69964 + 0.09553I$ $a = 2.24617 - 0.46709I$ $b = 4.02268 - 0.47212I$	$-10.86090 - 8.49023I$	0
$u = 1.69964 - 0.09553I$ $a = 2.24617 + 0.46709I$ $b = 4.02268 + 0.47212I$	$-10.86090 + 8.49023I$	0
$u = 1.70503 + 0.10421I$ $a = -2.95201 + 0.71525I$ $b = -5.24696 + 1.06747I$	$-13.2248 - 13.7857I$	0
$u = 1.70503 - 0.10421I$ $a = -2.95201 - 0.71525I$ $b = -5.24696 - 1.06747I$	$-13.2248 + 13.7857I$	0
$u = 1.71354 + 0.08181I$ $a = -1.37523 + 1.51380I$ $b = -2.28865 + 2.24136I$	$-15.9607 - 5.5984I$	0
$u = 1.71354 - 0.08181I$ $a = -1.37523 - 1.51380I$ $b = -2.28865 - 2.24136I$	$-15.9607 + 5.5984I$	0
$u = 1.72573$ $a = 2.16104$ $b = 3.90890$	$-15.5407$	0
$u = 1.73947 + 0.01560I$ $a = -2.65245 - 0.84909I$ $b = -4.61334 - 1.29091I$	$-19.1104 - 4.2965I$	0
$u = 1.73947 - 0.01560I$ $a = -2.65245 + 0.84909I$ $b = -4.61334 + 1.29091I$	$-19.1104 + 4.2965I$	0
$u = -0.193073 + 0.125473I$ $a = -0.16246 - 3.64433I$ $b = -0.357674 - 0.618866I$	$-0.31183 - 1.80289I$	$-2.01842 + 2.61178I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.193073 - 0.125473I$		
$a = -0.16246 + 3.64433I$	$-0.31183 + 1.80289I$	$-2.01842 - 2.61178I$
$b = -0.357674 + 0.618866I$		

$$\text{II. } I_2^u = \langle au + b - a, a^2 + au + a + u + 2, u^2 + u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ -au + a \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a + 1 \\ -au + a + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} au \\ au \end{pmatrix}$$

$$a_5 = \begin{pmatrix} au \\ au \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-3au - 2a - u - 16$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_5$	$(u^2 - u + 1)^2$
$c_2$	$(u^2 + u + 1)^2$
$c_4, c_9, c_{10}$	$u^4$
$c_6, c_7, c_8$	$(u^2 + u - 1)^2$
$c_{11}, c_{12}$	$(u^2 - u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_5$	$(y^2 + y + 1)^2$
$c_4, c_9, c_{10}$	$y^4$
$c_6, c_7, c_8$ $c_{11}, c_{12}$	$(y^2 - 3y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.618034$ $a = -0.80902 + 1.40126I$ $b = -0.309017 + 0.535233I$	$-0.98696 + 2.02988I$	$-13.5000 - 5.4006I$
$u = 0.618034$ $a = -0.80902 - 1.40126I$ $b = -0.309017 - 0.535233I$	$-0.98696 - 2.02988I$	$-13.5000 + 5.4006I$
$u = -1.61803$ $a = 0.309017 + 0.535233I$ $b = 0.80902 + 1.40126I$	$-8.88264 - 2.02988I$	$-13.50000 + 1.52761I$
$u = -1.61803$ $a = 0.309017 - 0.535233I$ $b = 0.80902 - 1.40126I$	$-8.88264 + 2.02988I$	$-13.50000 - 1.52761I$

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^2 - u + 1)^2)(u^{61} + 29u^{60} + \dots + 23u - 1)$
$c_2$	$((u^2 + u + 1)^2)(u^{61} + 3u^{60} + \dots + 9u + 1)$
$c_3$	$((u^2 - u + 1)^2)(u^{61} - 3u^{60} + \dots - 129u + 241)$
$c_4, c_9$	$u^4(u^{61} + u^{60} + \dots - 48u - 16)$
$c_5$	$((u^2 - u + 1)^2)(u^{61} + 3u^{60} + \dots + 9u + 1)$
$c_6, c_7, c_8$	$((u^2 + u - 1)^2)(u^{61} + 3u^{60} + \dots + u - 1)$
$c_{10}$	$u^4(u^{61} + 25u^{60} + \dots + 2432u + 256)$
$c_{11}, c_{12}$	$((u^2 - u - 1)^2)(u^{61} + 3u^{60} + \dots + u - 1)$



#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y^2 + y + 1)^2)(y^{61} + 9y^{60} + \dots + 707y - 1)$
$c_2, c_5$	$((y^2 + y + 1)^2)(y^{61} + 29y^{60} + \dots + 23y - 1)$
$c_3$	$((y^2 + y + 1)^2)(y^{61} - 11y^{60} + \dots + 2638239y - 58081)$
$c_4, c_9$	$y^4(y^{61} - 25y^{60} + \dots + 2432y - 256)$
$c_6, c_7, c_8$ $c_{11}, c_{12}$	$((y^2 - 3y + 1)^2)(y^{61} - 79y^{60} + \dots + 19y - 1)$
$c_{10}$	$y^4(y^{61} + 15y^{60} + \dots + 2564096y - 65536)$