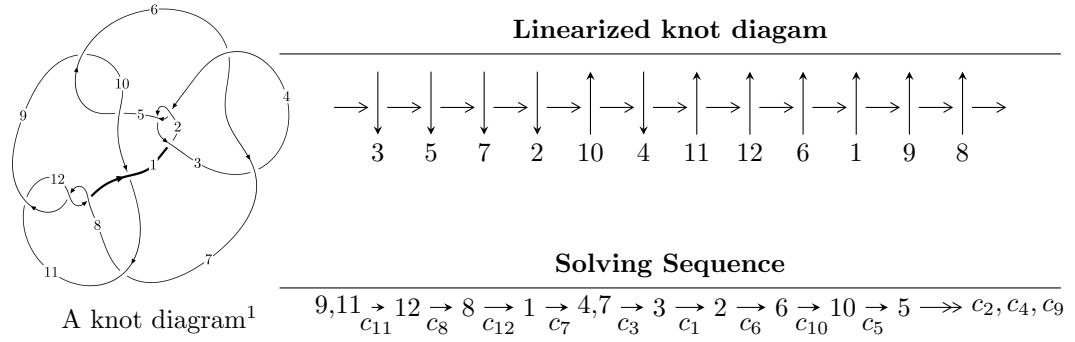


## $12a_{0051}$ ( $K12a_{0051}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle 5.08396 \times 10^{34}u^{109} + 2.87987 \times 10^{35}u^{108} + \dots + 2.07043 \times 10^{34}b + 1.00700 \times 10^{35}, \\
 &\quad - 2.40150 \times 10^{34}u^{109} - 7.91502 \times 10^{34}u^{108} + \dots + 2.07043 \times 10^{34}a - 1.21324 \times 10^{35}, \\
 &\quad u^{110} + 5u^{109} + \dots - 7u + 1 \rangle \\
 I_2^u &= \langle au - u^2 + b + a, -u^2a + a^2 + 1, u^3 - u^2 + 2u - 1 \rangle \\
 I_3^u &= \langle -u^2 + b - u - 2, 2u^2 + a + u + 4, u^3 + 2u - 1 \rangle \\
 I_4^u &= \langle -u^2 + b, -u^3 + a - u, u^4 + u^3 + 2u^2 + 2u + 1 \rangle \\
 I_5^u &= \langle u^2 + b + u, -u^2 + a - 2, u^3 - u^2 + 2u - 1 \rangle
 \end{aligned}$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 126 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 5.08 \times 10^{34}u^{109} + 2.88 \times 10^{35}u^{108} + \dots + 2.07 \times 10^{34}b + 1.01 \times 10^{35}, -2.40 \times 10^{34}u^{109} - 7.92 \times 10^{34}u^{108} + \dots + 2.07 \times 10^{34}a - 1.21 \times 10^{35}, u^{110} + 5u^{109} + \dots - 7u + 1 \rangle$$

(i) **Arc colorings**

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1.15991u^{109} + 3.82290u^{108} + \dots + 17.5984u + 5.85986 \\ -2.45551u^{109} - 13.9096u^{108} + \dots + 31.6055u - 4.86375 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^3 - 2u \\ u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1.25426u^{109} + 2.47074u^{108} + \dots + 28.5308u + 4.84333 \\ -4.21354u^{109} - 19.7876u^{108} + \dots + 21.4988u - 3.81138 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1.32122u^{109} - 5.24754u^{108} + \dots - 10.3151u - 3.64345 \\ 0.442881u^{109} + 4.21484u^{108} + \dots - 18.3658u + 2.99673 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -3.93346u^{109} - 15.5438u^{108} + \dots + 29.5005u - 0.0441834 \\ 4.97771u^{109} + 20.9442u^{108} + \dots - 6.60421u + 0.827017 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^6 - 3u^4 - 2u^2 + 1 \\ u^8 + 4u^6 + 4u^4 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1.46652u^{109} - 8.11160u^{108} + \dots + 30.3922u + 0.400062 \\ 0.0103310u^{109} + 0.286370u^{108} + \dots - 2.69149u + 0.0323288 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $1.61410u^{109} + 7.48255u^{108} + \dots - 53.0640u - 4.23776$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{110} + 53u^{109} + \cdots + 874u + 1$
$c_2, c_4$	$u^{110} - 11u^{109} + \cdots + 20u + 1$
$c_3, c_6$	$u^{110} - 4u^{109} + \cdots + 1344u - 128$
$c_5, c_9$	$u^{110} - 2u^{109} + \cdots - 1024u - 512$
$c_7$	$u^{110} - 5u^{109} + \cdots - 3176u + 292$
$c_8, c_{11}, c_{12}$	$u^{110} + 5u^{109} + \cdots - 7u + 1$
$c_{10}$	$u^{110} + 23u^{109} + \cdots - 3335609u + 61891$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{110} + 19y^{109} + \cdots - 806974y + 1$
$c_2, c_4$	$y^{110} - 53y^{109} + \cdots - 874y + 1$
$c_3, c_6$	$y^{110} + 54y^{109} + \cdots - 192512y + 16384$
$c_5, c_9$	$y^{110} + 56y^{109} + \cdots + 2228224y + 262144$
$c_7$	$y^{110} + 9y^{109} + \cdots - 11413240y + 85264$
$c_8, c_{11}, c_{12}$	$y^{110} + 101y^{109} + \cdots - 147y + 1$
$c_{10}$	$y^{110} + 41y^{109} + \cdots - 17639818908843y + 3830495881$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.087769 + 1.071150I$		
$a = -1.248980 - 0.465454I$	$2.25688 + 0.90789I$	0
$b = -1.37873 - 0.37865I$		
$u = -0.087769 - 1.071150I$		
$a = -1.248980 + 0.465454I$	$2.25688 - 0.90789I$	0
$b = -1.37873 + 0.37865I$		
$u = 0.267272 + 1.065890I$		
$a = -1.50466 - 0.67505I$	$1.22660 + 4.08841I$	0
$b = -0.984660 + 0.847043I$		
$u = 0.267272 - 1.065890I$		
$a = -1.50466 + 0.67505I$	$1.22660 - 4.08841I$	0
$b = -0.984660 - 0.847043I$		
$u = -0.467803 + 0.703618I$		
$a = 2.29074 - 0.39775I$	$-2.03455 + 9.47276I$	0
$b = -0.223957 + 0.915152I$		
$u = -0.467803 - 0.703618I$		
$a = 2.29074 + 0.39775I$	$-2.03455 - 9.47276I$	0
$b = -0.223957 - 0.915152I$		
$u = 0.326859 + 1.111260I$		
$a = 1.47565 + 0.59737I$	$-0.76167 + 9.32773I$	0
$b = 0.842871 - 0.962044I$		
$u = 0.326859 - 1.111260I$		
$a = 1.47565 - 0.59737I$	$-0.76167 - 9.32773I$	0
$b = 0.842871 + 0.962044I$		
$u = 0.044918 + 1.159940I$		
$a = 0.485785 + 0.353856I$	$-2.74728 + 0.22494I$	0
$b = 0.012116 - 1.098570I$		
$u = 0.044918 - 1.159940I$		
$a = 0.485785 - 0.353856I$	$-2.74728 - 0.22494I$	0
$b = 0.012116 + 1.098570I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.213857 + 1.147760I$	$-3.24169 + 3.96546I$	0
$a = -0.609333 - 0.547444I$		
$b = -0.276527 + 1.333880I$		
$u = 0.213857 - 1.147760I$	$-3.24169 - 3.96546I$	0
$a = -0.609333 + 0.547444I$		
$b = -0.276527 - 1.333880I$		
$u = -0.122184 + 1.171470I$	$1.13228 - 4.77677I$	0
$a = 0.937221 + 0.413575I$		
$b = 1.70265 + 0.66436I$		
$u = -0.122184 - 1.171470I$	$1.13228 + 4.77677I$	0
$a = 0.937221 - 0.413575I$		
$b = 1.70265 - 0.66436I$		
$u = -0.751985 + 0.316865I$	$-0.69158 - 13.75370I$	$0. + 9.91597I$
$a = -0.19275 - 2.67863I$		
$b = 0.28939 + 2.30634I$		
$u = -0.751985 - 0.316865I$	$-0.69158 + 13.75370I$	$0. - 9.91597I$
$a = -0.19275 + 2.67863I$		
$b = 0.28939 - 2.30634I$		
$u = -0.682778 + 0.437855I$	$-4.92429 - 1.07894I$	0
$a = 0.140125 + 0.021845I$		
$b = 0.306524 - 0.099329I$		
$u = -0.682778 - 0.437855I$	$-4.92429 + 1.07894I$	0
$a = 0.140125 - 0.021845I$		
$b = 0.306524 + 0.099329I$		
$u = -0.608747 + 0.529637I$	$-5.26321 - 3.26086I$	$0. + 8.42000I$
$a = -0.156738 + 0.093345I$		
$b = -0.147370 + 0.361143I$		
$u = -0.608747 - 0.529637I$	$-5.26321 + 3.26086I$	$0. - 8.42000I$
$a = -0.156738 - 0.093345I$		
$b = -0.147370 - 0.361143I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.133764 + 1.201670I$		
$a = 1.70456 + 1.05818I$	$-4.25280 + 2.01271I$	0
$b = 2.18770 - 1.16206I$		
$u = 0.133764 - 1.201670I$		
$a = 1.70456 - 1.05818I$	$-4.25280 - 2.01271I$	0
$b = 2.18770 + 1.16206I$		
$u = -0.393997 + 0.682907I$		
$a = -2.30080 + 0.11323I$	$0.47353 + 4.02638I$	$2.00000 - 1.65162I$
$b = 0.155381 - 0.647926I$		
$u = -0.393997 - 0.682907I$		
$a = -2.30080 - 0.11323I$	$0.47353 - 4.02638I$	$2.00000 + 1.65162I$
$b = 0.155381 + 0.647926I$		
$u = -0.728838 + 0.296790I$		
$a = 0.43006 + 2.61474I$	$1.88370 - 8.04851I$	$4.66389 + 6.64940I$
$b = -0.35716 - 2.24164I$		
$u = -0.728838 - 0.296790I$		
$a = 0.43006 - 2.61474I$	$1.88370 + 8.04851I$	$4.66389 - 6.64940I$
$b = -0.35716 + 2.24164I$		
$u = 0.777005 + 0.085415I$		
$a = -0.01227 + 2.08995I$	$2.37677 - 5.29652I$	$3.30695 + 5.27195I$
$b = -0.29493 - 1.78626I$		
$u = 0.777005 - 0.085415I$		
$a = -0.01227 - 2.08995I$	$2.37677 + 5.29652I$	$3.30695 - 5.27195I$
$b = -0.29493 + 1.78626I$		
$u = -0.702649 + 0.316627I$		
$a = 0.203452 + 0.089662I$	$-2.93391 - 7.17237I$	$0. + 7.42213I$
$b = 0.504761 + 0.070122I$		
$u = -0.702649 - 0.316627I$		
$a = 0.203452 - 0.089662I$	$-2.93391 + 7.17237I$	$0. - 7.42213I$
$b = 0.504761 - 0.070122I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.676292 + 0.325580I$		
$a = -0.92125 - 3.03516I$	$-3.81916 - 4.42307I$	$0.33207 + 6.45804I$
$b = 0.62862 + 2.30011I$		
$u = -0.676292 - 0.325580I$		
$a = -0.92125 + 3.03516I$	$-3.81916 + 4.42307I$	$0.33207 - 6.45804I$
$b = 0.62862 - 2.30011I$		
$u = 0.737560 + 0.128821I$		
$a = -0.23433 - 2.21989I$	$4.05943 - 0.32957I$	$7.05242 + 0.19707I$
$b = 0.34707 + 1.87285I$		
$u = 0.737560 - 0.128821I$		
$a = -0.23433 + 2.21989I$	$4.05943 + 0.32957I$	$7.05242 - 0.19707I$
$b = 0.34707 - 1.87285I$		
$u = 0.666718 + 0.321526I$		
$a = 1.00379 + 1.71314I$	$1.83773 + 7.20528I$	$3.32675 - 7.67477I$
$b = -0.57519 - 1.79009I$		
$u = 0.666718 - 0.321526I$		
$a = 1.00379 - 1.71314I$	$1.83773 - 7.20528I$	$3.32675 + 7.67477I$
$b = -0.57519 + 1.79009I$		
$u = -0.422080 + 0.598409I$		
$a = -0.305176 + 0.223190I$	$-4.06310 + 3.25446I$	$-2.82924 - 1.68811I$
$b = -0.003864 + 0.654541I$		
$u = -0.422080 - 0.598409I$		
$a = -0.305176 - 0.223190I$	$-4.06310 - 3.25446I$	$-2.82924 + 1.68811I$
$b = -0.003864 - 0.654541I$		
$u = 0.673412 + 0.257531I$		
$a = -0.90832 - 1.97279I$	$3.75181 + 2.12756I$	$7.14555 - 2.70279I$
$b = 0.55569 + 1.85787I$		
$u = 0.673412 - 0.257531I$		
$a = -0.90832 + 1.97279I$	$3.75181 - 2.12756I$	$7.14555 + 2.70279I$
$b = 0.55569 - 1.85787I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.633760 + 0.307440I$		
$a = -0.191099 - 0.147798I$	$-1.35364 - 2.39156I$	$1.35494 + 3.44541I$
$b = -0.453297 - 0.191626I$		
$u = -0.633760 - 0.307440I$		
$a = -0.191099 + 0.147798I$	$-1.35364 + 2.39156I$	$1.35494 - 3.44541I$
$b = -0.453297 + 0.191626I$		
$u = -0.442645 + 0.534598I$		
$a = 2.95117 + 0.09459I$	$-4.73490 + 0.63177I$	$-2.64133 - 0.41353I$
$b = -0.765044 + 0.351218I$		
$u = -0.442645 - 0.534598I$		
$a = 2.95117 - 0.09459I$	$-4.73490 - 0.63177I$	$-2.64133 + 0.41353I$
$b = -0.765044 - 0.351218I$		
$u = 0.238477 + 1.301950I$		
$a = 1.94233 - 0.22816I$	$-4.24078 + 2.59768I$	0
$b = -0.30674 - 2.02821I$		
$u = 0.238477 - 1.301950I$		
$a = 1.94233 + 0.22816I$	$-4.24078 - 2.59768I$	0
$b = -0.30674 + 2.02821I$		
$u = 0.668764 + 0.067218I$		
$a = -1.01044 - 2.15829I$	$-0.004153 - 0.660121I$	$-0.81116 + 3.72545I$
$b = 0.17342 + 1.51996I$		
$u = 0.668764 - 0.067218I$		
$a = -1.01044 + 2.15829I$	$-0.004153 + 0.660121I$	$-0.81116 - 3.72545I$
$b = 0.17342 - 1.51996I$		
$u = 0.327530 + 1.290810I$		
$a = -0.880564 - 0.599152I$	$-1.90814 - 1.31421I$	0
$b = -0.39051 + 2.00378I$		
$u = 0.327530 - 1.290810I$		
$a = -0.880564 + 0.599152I$	$-1.90814 + 1.31421I$	0
$b = -0.39051 - 2.00378I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.431721 + 0.498945I$		
$a = 1.38512 + 1.26258I$	$0.96271 - 3.52397I$	$1.82648 + 1.71517I$
$b = 0.329753 - 0.717428I$		
$u = 0.431721 - 0.498945I$		
$a = 1.38512 - 1.26258I$	$0.96271 + 3.52397I$	$1.82648 - 1.71517I$
$b = 0.329753 + 0.717428I$		
$u = -0.625020 + 0.195335I$		
$a = 1.02317 + 1.71908I$	$4.65417 - 3.79918I$	$5.60561 + 9.12001I$
$b = -0.30780 - 1.78368I$		
$u = -0.625020 - 0.195335I$		
$a = 1.02317 - 1.71908I$	$4.65417 + 3.79918I$	$5.60561 - 9.12001I$
$b = -0.30780 + 1.78368I$		
$u = 0.158715 + 1.337860I$		
$a = 0.527912 - 0.390102I$	$-3.43387 + 2.25266I$	0
$b = -0.670480 - 0.244495I$		
$u = 0.158715 - 1.337860I$		
$a = 0.527912 + 0.390102I$	$-3.43387 - 2.25266I$	0
$b = -0.670480 + 0.244495I$		
$u = 0.300858 + 1.330050I$		
$a = 1.015650 + 0.572458I$	$-0.51775 + 3.42145I$	0
$b = 0.43639 - 2.22756I$		
$u = 0.300858 - 1.330050I$		
$a = 1.015650 - 0.572458I$	$-0.51775 - 3.42145I$	0
$b = 0.43639 + 2.22756I$		
$u = 0.590275 + 0.237552I$		
$a = 1.14216 + 1.56879I$	$-0.45742 + 2.08316I$	$1.71834 - 4.71563I$
$b = 0.028965 - 0.993228I$		
$u = 0.590275 - 0.237552I$		
$a = 1.14216 - 1.56879I$	$-0.45742 - 2.08316I$	$1.71834 + 4.71563I$
$b = 0.028965 + 0.993228I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.448708 + 0.424163I$		
$a = 0.087098 - 0.355565I$	$-2.04918 - 1.01718I$	$-0.77645 + 4.39237I$
$b = -0.189088 - 0.505206I$		
$u = -0.448708 - 0.424163I$		
$a = 0.087098 + 0.355565I$	$-2.04918 + 1.01718I$	$-0.77645 - 4.39237I$
$b = -0.189088 + 0.505206I$		
$u = -0.213217 + 1.374140I$		
$a = -0.077328 + 0.925196I$	$-0.811385 - 0.560255I$	0
$b = -1.84754 - 2.39610I$		
$u = -0.213217 - 1.374140I$		
$a = -0.077328 - 0.925196I$	$-0.811385 + 0.560255I$	0
$b = -1.84754 + 2.39610I$		
$u = 0.232900 + 0.562056I$		
$a = -1.68860 - 1.12075I$	$2.28204 + 1.25980I$	$3.87420 - 3.95142I$
$b = -0.368435 + 0.504187I$		
$u = 0.232900 - 0.562056I$		
$a = -1.68860 + 1.12075I$	$2.28204 - 1.25980I$	$3.87420 + 3.95142I$
$b = -0.368435 - 0.504187I$		
$u = 0.096418 + 1.393080I$		
$a = 0.667863 + 0.044755I$	$-3.56329 + 2.49031I$	0
$b = -0.504387 - 0.413403I$		
$u = 0.096418 - 1.393080I$		
$a = 0.667863 - 0.044755I$	$-3.56329 - 2.49031I$	0
$b = -0.504387 + 0.413403I$		
$u = 0.205762 + 1.386790I$		
$a = -1.46276 - 0.03865I$	$-6.10565 + 2.87492I$	0
$b = 0.01850 + 3.00217I$		
$u = 0.205762 - 1.386790I$		
$a = -1.46276 + 0.03865I$	$-6.10565 - 2.87492I$	0
$b = 0.01850 - 3.00217I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.239877 + 1.381360I$		
$a = 0.363803 - 1.007460I$	$-0.37974 - 6.94098I$	0
$b = 1.83084 + 2.64228I$		
$u = -0.239877 - 1.381360I$		
$a = 0.363803 + 1.007460I$	$-0.37974 + 6.94098I$	0
$b = 1.83084 - 2.64228I$		
$u = 0.23220 + 1.39528I$		
$a = -1.080520 + 0.161583I$	$-5.68295 + 5.10949I$	0
$b = 0.376710 + 0.711456I$		
$u = 0.23220 - 1.39528I$		
$a = -1.080520 - 0.161583I$	$-5.68295 - 5.10949I$	0
$b = 0.376710 - 0.711456I$		
$u = -0.557111 + 0.152288I$		
$a = -1.16889 - 1.17714I$	$4.09579 + 2.24249I$	$2.09249 + 6.49191I$
$b = 0.13263 + 1.54331I$		
$u = -0.557111 - 0.152288I$		
$a = -1.16889 + 1.17714I$	$4.09579 - 2.24249I$	$2.09249 - 6.49191I$
$b = 0.13263 - 1.54331I$		
$u = 0.26322 + 1.40067I$		
$a = 1.150470 + 0.262478I$	$-1.53483 + 5.53884I$	0
$b = 0.12209 - 2.54689I$		
$u = 0.26322 - 1.40067I$		
$a = 1.150470 - 0.262478I$	$-1.53483 - 5.53884I$	0
$b = 0.12209 + 2.54689I$		
$u = -0.24822 + 1.42034I$		
$a = 0.125478 + 0.107540I$	$-6.88313 - 5.63183I$	0
$b = 0.746609 - 0.398952I$		
$u = -0.24822 - 1.42034I$		
$a = 0.125478 - 0.107540I$	$-6.88313 + 5.63183I$	0
$b = 0.746609 + 0.398952I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.17484 + 1.43130I$		
$a = 0.024046 + 0.220816I$	$-7.94217 - 3.35665I$	0
$b = 0.936174 + 0.364235I$		
$u = -0.17484 - 1.43130I$		
$a = 0.024046 - 0.220816I$	$-7.94217 + 3.35665I$	0
$b = 0.936174 - 0.364235I$		
$u = -0.10527 + 1.44541I$		
$a = 0.853980 + 0.625681I$	$-6.16042 + 2.51482I$	0
$b = -1.59490 - 0.51909I$		
$u = -0.10527 - 1.44541I$		
$a = 0.853980 - 0.625681I$	$-6.16042 - 2.51482I$	0
$b = -1.59490 + 0.51909I$		
$u = 0.16355 + 1.44140I$		
$a = -0.879236 + 0.029819I$	$-5.14995 - 1.32551I$	0
$b = 0.413235 + 0.411153I$		
$u = 0.16355 - 1.44140I$		
$a = -0.879236 - 0.029819I$	$-5.14995 + 1.32551I$	0
$b = 0.413235 - 0.411153I$		
$u = 0.25844 + 1.42833I$		
$a = -1.084660 - 0.164757I$	$-3.76654 + 10.58860I$	0
$b = 0.01462 + 2.51096I$		
$u = 0.25844 - 1.42833I$		
$a = -1.084660 + 0.164757I$	$-3.76654 - 10.58860I$	0
$b = 0.01462 - 2.51096I$		
$u = -0.28605 + 1.42369I$		
$a = 1.02941 - 1.09734I$	$-3.61534 - 11.73800I$	0
$b = 1.18408 + 3.15876I$		
$u = -0.28605 - 1.42369I$		
$a = 1.02941 + 1.09734I$	$-3.61534 + 11.73800I$	0
$b = 1.18408 - 3.15876I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.26157 + 1.42986I$	$-9.44015 - 7.84845I$	0
$a = -0.95968 + 1.43576I$		
$b = -1.58657 - 3.53860I$		
$u = -0.26157 - 1.42986I$	$-9.44015 + 7.84845I$	0
$a = -0.95968 - 1.43576I$		
$b = -1.58657 + 3.53860I$		
$u = -0.15325 + 1.44673I$		
$a = -0.921050 - 0.964047I$	$-10.99480 - 1.49755I$	0
$b = 2.34445 + 0.68813I$		
$u = -0.15325 - 1.44673I$		
$a = -0.921050 + 0.964047I$	$-10.99480 + 1.49755I$	0
$b = 2.34445 - 0.68813I$		
$u = -0.27283 + 1.42929I$	$-8.52249 - 10.72670I$	0
$a = -0.147225 - 0.080722I$		
$b = -0.629275 + 0.574116I$		
$u = -0.27283 - 1.42929I$	$-8.52249 + 10.72670I$	0
$a = -0.147225 + 0.080722I$		
$b = -0.629275 - 0.574116I$		
$u = -0.13438 + 1.44948I$		
$a = 0.060062 - 0.292373I$	$-10.49970 + 1.35653I$	0
$b = -0.956495 - 0.748806I$		
$u = -0.13438 - 1.44948I$		
$a = 0.060062 + 0.292373I$	$-10.49970 - 1.35653I$	0
$b = -0.956495 + 0.748806I$		
$u = -0.29452 + 1.43525I$	$-6.2981 - 17.5562I$	0
$a = -1.15670 + 1.04114I$		
$b = -0.94490 - 3.18553I$		
$u = -0.29452 - 1.43525I$		
$a = -1.15670 - 1.04114I$	$-6.2981 + 17.5562I$	0
$b = -0.94490 + 3.18553I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.10198 + 1.47999I$		
$a = -1.002820 - 0.545658I$	$-9.06430 + 7.73555I$	0
$b = 1.56485 + 0.12099I$		
$u = -0.10198 - 1.47999I$		
$a = -1.002820 + 0.545658I$	$-9.06430 - 7.73555I$	0
$b = 1.56485 - 0.12099I$		
$u = 0.485114 + 0.170668I$		
$a = 2.51389 + 2.67178I$	$-1.032640 + 0.255032I$	$3.20255 - 10.10229I$
$b = -1.16833 - 2.03899I$		
$u = 0.485114 - 0.170668I$		
$a = 2.51389 - 2.67178I$	$-1.032640 - 0.255032I$	$3.20255 + 10.10229I$
$b = -1.16833 + 2.03899I$		
$u = -0.24423 + 1.47467I$		
$a = -0.0983331 - 0.0071465I$	$-11.10450 - 4.45040I$	0
$b = -0.188904 + 0.429077I$		
$u = -0.24423 - 1.47467I$		
$a = -0.0983331 + 0.0071465I$	$-11.10450 + 4.45040I$	0
$b = -0.188904 - 0.429077I$		
$u = -0.19551 + 1.48517I$		
$a = 0.081909 - 0.126058I$	$-11.79450 - 6.13180I$	0
$b = -0.394609 - 0.545514I$		
$u = -0.19551 - 1.48517I$		
$a = 0.081909 + 0.126058I$	$-11.79450 + 6.13180I$	0
$b = -0.394609 + 0.545514I$		
$u = 0.480020$		
$a = -1.07071$	0.824866	12.3370
$b = 0.420132$		
$u = 0.0855909$		
$a = 7.24591$	$-1.21018$	-9.52400
$b = -0.772916$		

$$\text{II. } I_2^u = \langle au - u^2 + b + a, -u^2a + a^2 + 1, u^3 - u^2 + 2u - 1 \rangle$$

(i) Arc colorings

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ u^2 - u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ -u^2 + u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ -au + u^2 - a \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 - 1 \\ u^2 - u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2a + au - a + u \\ -au \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^2a + au - a + u \\ -2u^2 + 2u - 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ au - u^2 - a + 2u - 2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ au - u^2 - a + 2u - 2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-2u^2a + 6au + 6u^2 - 9a - 5u + 6$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_{11}$ $c_{12}$	$(u^3 - u^2 + 2u - 1)^2$
$c_2$	$(u^3 + u^2 - 1)^2$
$c_4, c_7, c_{10}$	$(u^3 - u^2 + 1)^2$
$c_5, c_9$	$u^6$
$c_6, c_8$	$(u^3 + u^2 + 2u + 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_6$ $c_8, c_{11}, c_{12}$	$(y^3 + 3y^2 + 2y - 1)^2$
$c_2, c_4, c_7$ $c_{10}$	$(y^3 - y^2 + 2y - 1)^2$
$c_5, c_9$	$y^6$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.215080 + 1.307140I$		
$a = -0.500000 - 0.424452I$	5.65624I	$-0.00556 - 4.66003I$
$b = -1.60964 + 1.73159I$		
$u = 0.215080 + 1.307140I$		
$a = -1.16236 + 0.98673I$	$-4.13758 + 2.82812I$	$-6.5820 - 15.2977I$
$b = 1.039800 + 0.882689I$		
$u = 0.215080 - 1.307140I$		
$a = -0.500000 + 0.424452I$	$-5.65624I$	$-0.00556 + 4.66003I$
$b = -1.60964 - 1.73159I$		
$u = 0.215080 - 1.307140I$		
$a = -1.16236 - 0.98673I$	$-4.13758 - 2.82812I$	$-6.5820 + 15.2977I$
$b = 1.039800 - 0.882689I$		
$u = 0.569840$		
$a = 0.162359 + 0.986732I$	4.13758 + 2.82812I	$4.08755 - 6.14773I$
$b = 0.06984 - 1.54901I$		
$u = 0.569840$		
$a = 0.162359 - 0.986732I$	4.13758 - 2.82812I	$4.08755 + 6.14773I$
$b = 0.06984 + 1.54901I$		

$$\text{III. } I_3^u = \langle -u^2 + b - u - 2, 2u^2 + a + u + 4, u^3 + 2u - 1 \rangle$$

(i) Arc colorings

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ -u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ -u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -2u^2 - u - 4 \\ u^2 + u + 2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ -u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -2u^2 - u - 4 \\ u^2 + u + 2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^2 - u - 3 \\ u^2 + 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ -u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^2 - 1 \\ u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $11u^2 + 9u + 22$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^3$
$c_3, c_6$	$u^3$
$c_4$	$(u + 1)^3$
$c_5, c_8, c_{10}$	$u^3 + 2u + 1$
$c_7$	$u^3 + 3u^2 + 5u + 2$
$c_9, c_{11}, c_{12}$	$u^3 + 2u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^3$
$c_3, c_6$	$y^3$
$c_5, c_8, c_9$ $c_{10}, c_{11}, c_{12}$	$y^3 + 4y^2 + 4y - 1$
$c_7$	$y^3 + y^2 + 13y - 4$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.22670 + 1.46771I$		
$a = 0.432268 - 0.136798I$	$-11.08570 - 5.13794I$	$-3.17092 + 5.88938I$
$b = -0.329484 + 0.802255I$		
$u = -0.22670 - 1.46771I$		
$a = 0.432268 + 0.136798I$	$-11.08570 + 5.13794I$	$-3.17092 - 5.88938I$
$b = -0.329484 - 0.802255I$		
$u = 0.453398$		
$a = -4.86454$	$-0.857735$	28.3420
$b = 2.65897$		

$$\text{IV. } I_4^u = \langle -u^2 + b, -u^3 + a - u, u^4 + u^3 + 2u^2 + 2u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u \\ u^3 + u \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^2 + 1 \\ u^3 + 2u + 1 \end{pmatrix} \\ a_4 &= \begin{pmatrix} u^3 + u \\ u^2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u^3 - 2u \\ u^3 + u \end{pmatrix} \\ a_3 &= \begin{pmatrix} u^3 + u \\ u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} u^3 + u^2 + u + 1 \\ u^3 + u^2 + 2u + 1 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -u^3 - 2u \\ u^3 + u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 2u^3 + u^2 + 3u + 3 \\ -u^3 - u^2 - u - 2 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u^2 - 1 \\ -u^3 - 2u - 1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $7u^3 + 3u^2 + 7u + 2$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^4$
$c_3, c_6$	$u^4$
$c_4$	$(u + 1)^4$
$c_5, c_8, c_{10}$	$u^4 - u^3 + 2u^2 - 2u + 1$
$c_7$	$(u^2 - u + 1)^2$
$c_9, c_{11}, c_{12}$	$u^4 + u^3 + 2u^2 + 2u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^4$
$c_3, c_6$	$y^4$
$c_5, c_8, c_9$ $c_{10}, c_{11}, c_{12}$	$y^4 + 3y^3 + 2y^2 + 1$
$c_7$	$(y^2 + y + 1)^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.621744 + 0.440597I$		
$a = -0.500000 + 0.866025I$	$-4.93480 - 2.02988I$	$-0.92268 + 4.41855I$
$b = 0.192440 - 0.547877I$		
$u = -0.621744 - 0.440597I$		
$a = -0.500000 - 0.866025I$	$-4.93480 + 2.02988I$	$-0.92268 - 4.41855I$
$b = 0.192440 + 0.547877I$		
$u = 0.121744 + 1.306620I$		
$a = -0.500000 - 0.866025I$	$-4.93480 + 2.02988I$	$-6.57732 - 5.10773I$
$b = -1.69244 + 0.31815I$		
$u = 0.121744 - 1.306620I$		
$a = -0.500000 + 0.866025I$	$-4.93480 - 2.02988I$	$-6.57732 + 5.10773I$
$b = -1.69244 - 0.31815I$		

$$\mathbf{V. } I_5^u = \langle u^2 + b + u, -u^2 + a - 2, u^3 - u^2 + 2u - 1 \rangle$$

(i) Arc colorings

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ u^2 - u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ -u^2 + u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2 + 2 \\ -u^2 - u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 - 1 \\ u^2 - u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 2u^2 - u + 3 \\ -u^2 - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 2u^2 - u + 3 \\ -2u^2 + 2u - 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ -u^2 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ -u^2 + u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-4u^2 + 3u - 4$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_{11}$ $c_{12}$	$u^3 - u^2 + 2u - 1$
$c_2$	$u^3 + u^2 - 1$
$c_4, c_7, c_{10}$	$u^3 - u^2 + 1$
$c_5, c_9$	$u^3$
$c_6, c_8$	$u^3 + u^2 + 2u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_6$ $c_8, c_{11}, c_{12}$	$y^3 + 3y^2 + 2y - 1$
$c_2, c_4, c_7$ $c_{10}$	$y^3 - y^2 + 2y - 1$
$c_5, c_9$	$y^3$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.215080 + 1.307140I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.337641 + 0.562280I$	0	$3.29468 + 1.67231I$
$b = 1.44728 - 1.86942I$		
$u = 0.215080 - 1.307140I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.337641 - 0.562280I$	0	$3.29468 - 1.67231I$
$b = 1.44728 + 1.86942I$		
$u = 0.569840$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 2.32472$	0	$-3.58940$
$b = -0.894558$		

## VI. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^7)(u^3 - u^2 + 2u - 1)^3(u^{110} + 53u^{109} + \dots + 874u + 1)$
$c_2$	$((u - 1)^7)(u^3 + u^2 - 1)^3(u^{110} - 11u^{109} + \dots + 20u + 1)$
$c_3$	$u^7(u^3 - u^2 + 2u - 1)^3(u^{110} - 4u^{109} + \dots + 1344u - 128)$
$c_4$	$((u + 1)^7)(u^3 - u^2 + 1)^3(u^{110} - 11u^{109} + \dots + 20u + 1)$
$c_5$	$u^9(u^3 + 2u + 1)(u^4 - u^3 + \dots - 2u + 1)(u^{110} - 2u^{109} + \dots - 1024u - 512)$
$c_6$	$u^7(u^3 + u^2 + 2u + 1)^3(u^{110} - 4u^{109} + \dots + 1344u - 128)$
$c_7$	$(u^2 - u + 1)^2(u^3 - u^2 + 1)^3(u^3 + 3u^2 + 5u + 2)$ $\cdot (u^{110} - 5u^{109} + \dots - 3176u + 292)$
$c_8$	$(u^3 + 2u + 1)(u^3 + u^2 + 2u + 1)^3(u^4 - u^3 + 2u^2 - 2u + 1)$ $\cdot (u^{110} + 5u^{109} + \dots - 7u + 1)$
$c_9$	$u^9(u^3 + 2u - 1)(u^4 + u^3 + \dots + 2u + 1)(u^{110} - 2u^{109} + \dots - 1024u - 512)$
$c_{10}$	$(u^3 + 2u + 1)(u^3 - u^2 + 1)^3(u^4 - u^3 + 2u^2 - 2u + 1)$ $\cdot (u^{110} + 23u^{109} + \dots - 3335609u + 61891)$
$c_{11}, c_{12}$	$(u^3 + 2u - 1)(u^3 - u^2 + 2u - 1)^3(u^4 + u^3 + 2u^2 + 2u + 1)$ $\cdot (u^{110} + 5u^{109} + \dots - 7u + 1)$

## VII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y - 1)^7)(y^3 + 3y^2 + 2y - 1)^3(y^{110} + 19y^{109} + \dots - 806974y + 1)$
$c_2, c_4$	$((y - 1)^7)(y^3 - y^2 + 2y - 1)^3(y^{110} - 53y^{109} + \dots - 874y + 1)$
$c_3, c_6$	$y^7(y^3 + 3y^2 + 2y - 1)^3(y^{110} + 54y^{109} + \dots - 192512y + 16384)$
$c_5, c_9$	$y^9(y^3 + 4y^2 + 4y - 1)(y^4 + 3y^3 + 2y^2 + 1)$ $\cdot (y^{110} + 56y^{109} + \dots + 2228224y + 262144)$
$c_7$	$(y^2 + y + 1)^2(y^3 - y^2 + 2y - 1)^3(y^3 + y^2 + 13y - 4)$ $\cdot (y^{110} + 9y^{109} + \dots - 11413240y + 85264)$
$c_8, c_{11}, c_{12}$	$(y^3 + 3y^2 + 2y - 1)^3(y^3 + 4y^2 + 4y - 1)(y^4 + 3y^3 + 2y^2 + 1)$ $\cdot (y^{110} + 101y^{109} + \dots - 147y + 1)$
$c_{10}$	$(y^3 - y^2 + 2y - 1)^3(y^3 + 4y^2 + 4y - 1)(y^4 + 3y^3 + 2y^2 + 1)$ $\cdot (y^{110} + 41y^{109} + \dots - 17639818908843y + 3830495881)$