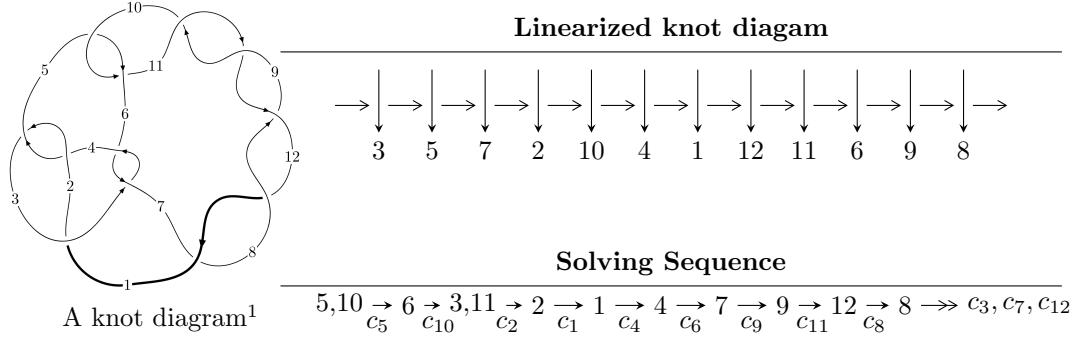


$12a_{0056}$  ( $K12a_{0056}$ )



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -u^{48} - u^{47} + \dots + b + 1, u^{45} - 4u^{43} + \dots + a - 5u, u^{49} + 2u^{48} + \dots + u - 1 \rangle$$

$$I_2^u = \langle b + 1, u^4 - u^2 + a + u + 2, u^5 - u^4 + u^2 + u - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 54 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle -u^{48} - u^{47} + \cdots + b + 1, \ u^{45} - 4u^{43} + \cdots + a - 5u, \ u^{49} + 2u^{48} + \cdots + u - 1 \rangle^{\text{I.}}$$

(i) **Arc colorings**

$$\begin{aligned} a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u^{45} + 4u^{43} + \cdots - 22u^3 + 5u \\ u^{48} + u^{47} + \cdots + 4u^2 - 1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix} \\ a_2 &= \begin{pmatrix} u^{48} + u^{47} + \cdots + 5u - 1 \\ u^{48} + u^{47} + \cdots + 4u^2 - 1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^9 + 3u^5 + u \\ u^{11} - u^9 + 4u^7 - 3u^5 + 3u^3 - u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 2u^{48} + 2u^{47} + \cdots + 6u - 1 \\ u^{48} + u^{47} + \cdots + u - 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} u^{11} + 4u^7 + 3u^3 \\ u^{13} - u^{11} + 5u^9 - 4u^7 + 6u^5 - 3u^3 + u \end{pmatrix} \\ a_9 &= \begin{pmatrix} u^3 \\ u^5 - u^3 + u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -u^5 - u \\ -u^7 + u^5 - 2u^3 + u \end{pmatrix} \\ a_8 &= \begin{pmatrix} u^7 + 2u^3 \\ u^9 - u^7 + 3u^5 - 2u^3 + u \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** =  $-1$

(iii) **Cusp Shapes** =  $6u^{48} + 5u^{47} + \cdots + 9u - 20$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{49} + 20u^{48} + \cdots + 79u + 1$
$c_2, c_4$	$u^{49} - 6u^{48} + \cdots - u + 1$
$c_3, c_6$	$u^{49} - u^{48} + \cdots + 64u + 32$
$c_5, c_{10}$	$u^{49} - 2u^{48} + \cdots + u + 1$
$c_7, c_8, c_9$ $c_{11}, c_{12}$	$u^{49} + 8u^{48} + \cdots + 13u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{49} + 24y^{48} + \cdots + 2991y - 1$
$c_2, c_4$	$y^{49} - 20y^{48} + \cdots + 79y - 1$
$c_3, c_6$	$y^{49} + 33y^{48} + \cdots - 9728y - 1024$
$c_5, c_{10}$	$y^{49} - 8y^{48} + \cdots + 13y - 1$
$c_7, c_8, c_9$ $c_{11}, c_{12}$	$y^{49} + 68y^{48} + \cdots - 67y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.760736 + 0.719246I$	$3.14913 + 0.38825I$	$-7.13985 + 0.I$
$a = 1.12247 + 1.09140I$		
$b = -0.784658 - 0.558197I$		
$u = -0.760736 - 0.719246I$	$3.14913 - 0.38825I$	$-7.13985 + 0.I$
$a = 1.12247 - 1.09140I$		
$b = -0.784658 + 0.558197I$		
$u = 0.796734 + 0.681722I$	$1.51702 - 2.54299I$	$-6.23264 + 3.96997I$
$a = -0.291180 + 1.036890I$		
$b = -1.281700 + 0.033312I$		
$u = 0.796734 - 0.681722I$	$1.51702 + 2.54299I$	$-6.23264 - 3.96997I$
$a = -0.291180 - 1.036890I$		
$b = -1.281700 - 0.033312I$		
$u = -0.892137 + 0.327379I$	$0.43580 + 6.91892I$	$-11.9536 - 9.3736I$
$a = 2.17207 + 1.31935I$		
$b = 1.005090 - 0.623169I$		
$u = -0.892137 - 0.327379I$	$0.43580 - 6.91892I$	$-11.9536 + 9.3736I$
$a = 2.17207 - 1.31935I$		
$b = 1.005090 + 0.623169I$		
$u = -0.844082 + 0.428322I$	$1.59253 + 2.02971I$	$-8.12894 - 3.92342I$
$a = -0.187763 + 0.837953I$		
$b = 0.617924 + 0.579853I$		
$u = -0.844082 - 0.428322I$	$1.59253 - 2.02971I$	$-8.12894 + 3.92342I$
$a = -0.187763 - 0.837953I$		
$b = 0.617924 - 0.579853I$		
$u = 0.693592 + 0.795699I$	$7.01029 + 5.24368I$	$-5.42899 - 3.02603I$
$a = -0.527393 + 1.026490I$		
$b = 1.070340 - 0.723216I$		
$u = 0.693592 - 0.795699I$	$7.01029 - 5.24368I$	$-5.42899 + 3.02603I$
$a = -0.527393 - 1.026490I$		
$b = 1.070340 + 0.723216I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.842140 + 0.687789I$		
$a = -0.05555 - 2.42181I$	$2.88211 + 4.83632I$	$-8.23420 - 6.42667I$
$b = -0.868271 + 0.553100I$		
$u = -0.842140 - 0.687789I$		
$a = -0.05555 + 2.42181I$	$2.88211 - 4.83632I$	$-8.23420 + 6.42667I$
$b = -0.868271 - 0.553100I$		
$u = 0.749509 + 0.792916I$		
$a = -0.060126 - 1.378320I$	$8.45422 - 0.68674I$	$-3.54074 + 1.96318I$
$b = 0.588767 + 0.880625I$		
$u = 0.749509 - 0.792916I$		
$a = -0.060126 + 1.378320I$	$8.45422 + 0.68674I$	$-3.54074 - 1.96318I$
$b = 0.588767 - 0.880625I$		
$u = -0.737633 + 0.516972I$		
$a = 0.414474 + 0.300895I$	$1.34830 + 2.00478I$	$-4.48597 - 4.55079I$
$b = 0.346209 + 0.168150I$		
$u = -0.737633 - 0.516972I$		
$a = 0.414474 - 0.300895I$	$1.34830 - 2.00478I$	$-4.48597 + 4.55079I$
$b = 0.346209 - 0.168150I$		
$u = 0.880418 + 0.058419I$		
$a = 1.79760 - 0.81935I$	$-0.98474 + 2.22735I$	$-14.5110 - 2.6928I$
$b = 0.877222 - 0.561628I$		
$u = 0.880418 - 0.058419I$		
$a = 1.79760 + 0.81935I$	$-0.98474 - 2.22735I$	$-14.5110 + 2.6928I$
$b = 0.877222 + 0.561628I$		
$u = 0.892884 + 0.720049I$		
$a = -1.122640 + 0.355505I$	$7.97137 - 4.88104I$	$-4.58899 + 4.14916I$
$b = 0.517458 - 0.877459I$		
$u = 0.892884 - 0.720049I$		
$a = -1.122640 - 0.355505I$	$7.97137 + 4.88104I$	$-4.58899 - 4.14916I$
$b = 0.517458 + 0.877459I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.922095 + 0.682387I$		
$a = 0.94618 - 2.27074I$	$6.24237 - 10.68800I$	$-7.37912 + 8.93754I$
$b = 1.097470 + 0.693580I$		
$u = 0.922095 - 0.682387I$		
$a = 0.94618 + 2.27074I$	$6.24237 + 10.68800I$	$-7.37912 - 8.93754I$
$b = 1.097470 - 0.693580I$		
$u = 0.740442 + 0.287353I$		
$a = -1.50962 + 2.57763I$	$-2.14769 - 2.41886I$	$-15.9646 + 6.9978I$
$b = -0.946359 - 0.333388I$		
$u = 0.740442 - 0.287353I$		
$a = -1.50962 - 2.57763I$	$-2.14769 + 2.41886I$	$-15.9646 - 6.9978I$
$b = -0.946359 + 0.333388I$		
$u = -0.359412 + 0.611149I$		
$a = -0.165040 + 1.109630I$	$3.14714 + 1.64287I$	$-3.84623 - 3.06683I$
$b = 0.758551 - 0.696515I$		
$u = -0.359412 - 0.611149I$		
$a = -0.165040 - 1.109630I$	$3.14714 - 1.64287I$	$-3.84623 + 3.06683I$
$b = 0.758551 + 0.696515I$		
$u = 0.931772 + 0.895572I$		
$a = 0.237488 - 0.406711I$	$9.96355 - 3.30520I$	0
$b = 0.694049 - 0.014591I$		
$u = 0.931772 - 0.895572I$		
$a = 0.237488 + 0.406711I$	$9.96355 + 3.30520I$	0
$b = 0.694049 + 0.014591I$		
$u = -0.682651 + 0.184302I$		
$a = -2.50646 - 0.45724I$	$-2.69048 + 0.60292I$	$-15.3689 - 9.6396I$
$b = -1.096840 - 0.143397I$		
$u = -0.682651 - 0.184302I$		
$a = -2.50646 + 0.45724I$	$-2.69048 - 0.60292I$	$-15.3689 + 9.6396I$
$b = -1.096840 + 0.143397I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.948044 + 0.926579I$		
$a = 0.195056 - 0.777042I$	$11.83110 + 3.40658I$	0
$b = -1.395190 - 0.006072I$		
$u = -0.948044 - 0.926579I$		
$a = 0.195056 + 0.777042I$	$11.83110 - 3.40658I$	0
$b = -1.395190 + 0.006072I$		
$u = 0.942403 + 0.933530I$		
$a = 1.03952 - 1.20944I$	$13.54070 - 0.72694I$	0
$b = -0.855209 + 0.703197I$		
$u = 0.942403 - 0.933530I$		
$a = 1.03952 + 1.20944I$	$13.54070 + 0.72694I$	0
$b = -0.855209 - 0.703197I$		
$u = -0.927792 + 0.948411I$		
$a = -0.633748 - 1.030830I$	$17.4053 - 6.0517I$	0
$b = 1.155820 + 0.749430I$		
$u = -0.927792 - 0.948411I$		
$a = -0.633748 + 1.030830I$	$17.4053 + 6.0517I$	0
$b = 1.155820 - 0.749430I$		
$u = 0.956706 + 0.925364I$		
$a = 0.22666 + 2.17249I$	$13.4933 - 6.1049I$	0
$b = -0.870319 - 0.699281I$		
$u = 0.956706 - 0.925364I$		
$a = 0.22666 - 2.17249I$	$13.4933 + 6.1049I$	0
$b = -0.870319 + 0.699281I$		
$u = -0.939680 + 0.946771I$		
$a = -0.07120 + 1.53829I$	$19.3115 + 0.3590I$	0
$b = 0.540687 - 1.020080I$		
$u = -0.939680 - 0.946771I$		
$a = -0.07120 - 1.53829I$	$19.3115 - 0.3590I$	0
$b = 0.540687 + 1.020080I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.975390 + 0.920268I$		
$a = 0.26091 + 2.26210I$	$17.2463 + 12.9142I$	0
$b = 1.161320 - 0.741973I$		
$u = -0.975390 - 0.920268I$		
$a = 0.26091 - 2.26210I$	$17.2463 - 12.9142I$	0
$b = 1.161320 + 0.741973I$		
$u = -0.968824 + 0.929241I$		
$a = -1.16534 - 0.91357I$	$19.2138 + 6.5292I$	0
$b = 0.526652 + 1.020740I$		
$u = -0.968824 - 0.929241I$		
$a = -1.16534 + 0.91357I$	$19.2138 - 6.5292I$	0
$b = 0.526652 - 1.020740I$		
$u = -0.222542 + 0.611946I$		
$a = -0.356092 - 1.021050I$	$2.61636 - 3.65615I$	$-4.75819 + 3.34819I$
$b = 0.934438 + 0.678142I$		
$u = -0.222542 - 0.611946I$		
$a = -0.356092 + 1.021050I$	$2.61636 + 3.65615I$	$-4.75819 - 3.34819I$
$b = 0.934438 - 0.678142I$		
$u = 0.560438$		
$a = 0.882793$	$-0.730326$	-14.0240
$b = -0.134956$		
$u = 0.314290 + 0.268544I$		
$a = 1.79832 - 0.55498I$	$-0.980654 + 0.106245I$	$-9.70626 + 1.04735I$
$b = -0.725982 + 0.146511I$		
$u = 0.314290 - 0.268544I$		
$a = 1.79832 + 0.55498I$	$-0.980654 - 0.106245I$	$-9.70626 - 1.04735I$
$b = -0.725982 - 0.146511I$		

$$\text{II. } I_2^u = \langle b + 1, u^4 - u^2 + a + u + 2, u^5 - u^4 + u^2 + u - 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^4 + u^2 - u - 2 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^4 + u^2 - u - 3 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^4 + u^2 - u - 2 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^3 \\ u^4 - u^3 - u^2 + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^4 + u^2 - 1 \\ u^4 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-u^3 + 3u^2 - u - 14$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^5$
$c_3, c_6$	$u^5$
$c_4$	$(u + 1)^5$
$c_5$	$u^5 - u^4 + u^2 + u - 1$
$c_7, c_8, c_9$	$u^5 - u^4 + 4u^3 - 3u^2 + 3u - 1$
$c_{10}$	$u^5 + u^4 - u^2 + u + 1$
$c_{11}, c_{12}$	$u^5 + u^4 + 4u^3 + 3u^2 + 3u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^5$
$c_3, c_6$	$y^5$
$c_5, c_{10}$	$y^5 - y^4 + 4y^3 - 3y^2 + 3y - 1$
$c_7, c_8, c_9$ $c_{11}, c_{12}$	$y^5 + 7y^4 + 16y^3 + 13y^2 + 3y - 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.758138 + 0.584034I$		
$a = -0.278580 - 1.055720I$	$0.17487 + 2.21397I$	$-12.88087 - 4.04855I$
$b = -1.00000$		
$u = -0.758138 - 0.584034I$		
$a = -0.278580 + 1.055720I$	$0.17487 - 2.21397I$	$-12.88087 + 4.04855I$
$b = -1.00000$		
$u = 0.935538 + 0.903908I$		
$a = -0.020316 + 0.590570I$	$9.31336 - 3.33174I$	$-13.28666 + 2.53508I$
$b = -1.00000$		
$u = 0.935538 - 0.903908I$		
$a = -0.020316 - 0.590570I$	$9.31336 + 3.33174I$	$-13.28666 - 2.53508I$
$b = -1.00000$		
$u = 0.645200$		
$a = -2.40221$	$-2.52712$	$-13.6650$
$b = -1.00000$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^5)(u^{49} + 20u^{48} + \dots + 79u + 1)$
$c_2$	$((u - 1)^5)(u^{49} - 6u^{48} + \dots - u + 1)$
$c_3, c_6$	$u^5(u^{49} - u^{48} + \dots + 64u + 32)$
$c_4$	$((u + 1)^5)(u^{49} - 6u^{48} + \dots - u + 1)$
$c_5$	$(u^5 - u^4 + u^2 + u - 1)(u^{49} - 2u^{48} + \dots + u + 1)$
$c_7, c_8, c_9$	$(u^5 - u^4 + 4u^3 - 3u^2 + 3u - 1)(u^{49} + 8u^{48} + \dots + 13u + 1)$
$c_{10}$	$(u^5 + u^4 - u^2 + u + 1)(u^{49} - 2u^{48} + \dots + u + 1)$
$c_{11}, c_{12}$	$(u^5 + u^4 + 4u^3 + 3u^2 + 3u + 1)(u^{49} + 8u^{48} + \dots + 13u + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y - 1)^5)(y^{49} + 24y^{48} + \dots + 2991y - 1)$
$c_2, c_4$	$((y - 1)^5)(y^{49} - 20y^{48} + \dots + 79y - 1)$
$c_3, c_6$	$y^5(y^{49} + 33y^{48} + \dots - 9728y - 1024)$
$c_5, c_{10}$	$(y^5 - y^4 + 4y^3 - 3y^2 + 3y - 1)(y^{49} - 8y^{48} + \dots + 13y - 1)$
$c_7, c_8, c_9$ $c_{11}, c_{12}$	$(y^5 + 7y^4 + 16y^3 + 13y^2 + 3y - 1)(y^{49} + 68y^{48} + \dots - 67y - 1)$