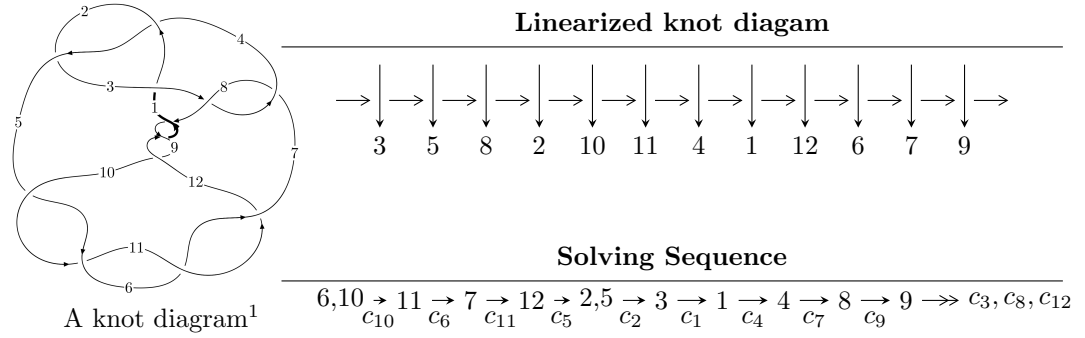


12a<sub>0096</sub> (K12a<sub>0096</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -u^{59} + 31u^{57} + \dots - 4u^2 + b, -u^{62} - u^{61} + \dots + a - 1, u^{63} + 2u^{62} + \dots + 2u - 1 \rangle$$

$$I_2^u = \langle u^4 - 2u^2 + b + 2u, -u^5 + 3u^3 + a + 1, u^6 + u^5 - 3u^4 - 2u^3 + 2u^2 - u - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 69 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\langle -u^{59} + 31u^{57} + \dots - 4u^2 + b, -u^{62} - u^{61} + \dots + a - 1, u^{63} + 2u^{62} + \dots + 2u - 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^{62} + u^{61} + \dots + 2u + 1 \\ u^{59} - 31u^{57} + \dots - 3u^3 + 4u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 2u^{62} + u^{61} + \dots - 4u^2 + 5u \\ u^{62} - 33u^{60} + \dots + 3u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^{10} + 5u^8 - 8u^6 + 5u^4 - 3u^2 + 1 \\ -u^{12} + 6u^{10} - 12u^8 + 8u^6 - u^4 + 2u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^{61} - 32u^{59} + \dots + u + 1 \\ -u^{62} + 33u^{60} + \dots - 2u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^{14} - 7u^{12} + 18u^{10} - 21u^8 + 14u^6 - 10u^4 + 4u^2 - 1 \\ u^{16} - 8u^{14} + 24u^{12} - 32u^{10} + 18u^8 - 8u^6 + 8u^4 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^6 + 3u^4 - 2u^2 + 1 \\ -u^8 + 4u^6 - 4u^4 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-u^{61} - u^{60} + \dots + 2u - 18$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{63} + 27u^{62} + \dots + 95u + 1$
$c_2, c_4$	$u^{63} - 7u^{62} + \dots + u + 1$
$c_3, c_7$	$u^{63} + u^{62} + \dots + 192u + 64$
$c_5, c_6, c_{10}$ $c_{11}$	$u^{63} - 2u^{62} + \dots + 2u + 1$
$c_8, c_9, c_{12}$	$u^{63} - 8u^{62} + \dots + 6u + 7$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{63} + 25y^{62} + \dots + 5299y - 1$
$c_2, c_4$	$y^{63} - 27y^{62} + \dots + 95y - 1$
$c_3, c_7$	$y^{63} + 39y^{62} + \dots - 40960y - 4096$
$c_5, c_6, c_{10}$ $c_{11}$	$y^{63} - 68y^{62} + \dots + 14y - 1$
$c_8, c_9, c_{12}$	$y^{63} + 64y^{62} + \dots - 2246y - 49$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.552072 + 0.648887I$ $a = 0.477044 + 0.191255I$ $b = 1.98574 - 0.28222I$	$8.36290 - 11.10910I$	$-8.86571 + 8.37495I$
$u = 0.552072 - 0.648887I$ $a = 0.477044 - 0.191255I$ $b = 1.98574 + 0.28222I$	$8.36290 + 11.10910I$	$-8.86571 - 8.37495I$
$u = 0.533877 + 0.656255I$ $a = -0.086296 + 0.604333I$ $b = -0.591871 - 0.592997I$	$10.28220 - 4.95595I$	$-6.40227 + 3.95794I$
$u = 0.533877 - 0.656255I$ $a = -0.086296 - 0.604333I$ $b = -0.591871 + 0.592997I$	$10.28220 + 4.95595I$	$-6.40227 - 3.95794I$
$u = -0.518166 + 0.638255I$ $a = 0.239548 + 0.425049I$ $b = 1.50926 + 0.75312I$	$4.80189 + 4.67051I$	$-9.56411 - 5.84070I$
$u = -0.518166 - 0.638255I$ $a = 0.239548 - 0.425049I$ $b = 1.50926 - 0.75312I$	$4.80189 - 4.67051I$	$-9.56411 + 5.84070I$
$u = 0.475260 + 0.668900I$ $a = -0.500436 - 0.356756I$ $b = 0.840809 - 0.212539I$	$10.45670 + 0.49427I$	$-5.93156 + 2.06629I$
$u = 0.475260 - 0.668900I$ $a = -0.500436 + 0.356756I$ $b = 0.840809 + 0.212539I$	$10.45670 - 0.49427I$	$-5.93156 - 2.06629I$
$u = 0.453215 + 0.669802I$ $a = -0.35281 + 1.85601I$ $b = -0.317027 + 0.198250I$	$8.65681 + 6.66761I$	$-8.01120 - 2.46984I$
$u = 0.453215 - 0.669802I$ $a = -0.35281 - 1.85601I$ $b = -0.317027 - 0.198250I$	$8.65681 - 6.66761I$	$-8.01120 + 2.46984I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.500444 + 0.632445I$ $a = -0.016435 - 1.256630I$ $b = -1.040210 + 0.063749I$	$3.24652 - 2.14201I$	$-8.59063 + 3.32182I$
$u = 0.500444 - 0.632445I$ $a = -0.016435 + 1.256630I$ $b = -1.040210 - 0.063749I$	$3.24652 + 2.14201I$	$-8.59063 - 3.32182I$
$u = -0.484205 + 0.643677I$ $a = -0.75821 - 1.21698I$ $b = -0.773190 + 0.091630I$	$4.90236 - 0.33637I$	$-9.15743 - 0.38817I$
$u = -0.484205 - 0.643677I$ $a = -0.75821 + 1.21698I$ $b = -0.773190 - 0.091630I$	$4.90236 + 0.33637I$	$-9.15743 + 0.38817I$
$u = -0.657206 + 0.383548I$ $a = -0.498372 + 0.026703I$ $b = -2.07884 + 0.04909I$	$0.73856 + 7.23469I$	$-12.7532 - 9.6424I$
$u = -0.657206 - 0.383548I$ $a = -0.498372 - 0.026703I$ $b = -2.07884 - 0.04909I$	$0.73856 - 7.23469I$	$-12.7532 + 9.6424I$
$u = 0.750394 + 0.085615I$ $a = 0.447881 + 0.312629I$ $b = 1.52225 - 0.54267I$	$-0.91500 + 2.18703I$	$-15.1580 - 2.5589I$
$u = 0.750394 - 0.085615I$ $a = 0.447881 - 0.312629I$ $b = 1.52225 + 0.54267I$	$-0.91500 - 2.18703I$	$-15.1580 + 2.5589I$
$u = -0.495914 + 0.538413I$ $a = -0.181479 + 0.681833I$ $b = -0.586391 + 0.071931I$	$2.22957 + 1.86380I$	$-4.96531 - 3.49525I$
$u = -0.495914 - 0.538413I$ $a = -0.181479 - 0.681833I$ $b = -0.586391 - 0.071931I$	$2.22957 - 1.86380I$	$-4.96531 + 3.49525I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.572206 + 0.430292I$ $a = -0.149585 + 0.569347I$ $b = -0.199905 - 0.583366I$	$2.16114 + 2.24871I$	$-8.78086 - 4.77265I$
$u = -0.572206 - 0.430292I$ $a = -0.149585 - 0.569347I$ $b = -0.199905 + 0.583366I$	$2.16114 - 2.24871I$	$-8.78086 + 4.77265I$
$u = 0.539929 + 0.300101I$ $a = -0.044166 + 0.631034I$ $b = -1.65764 + 0.85420I$	$-1.85220 - 2.46880I$	$-16.2123 + 7.6233I$
$u = 0.539929 - 0.300101I$ $a = -0.044166 - 0.631034I$ $b = -1.65764 - 0.85420I$	$-1.85220 + 2.46880I$	$-16.2123 - 7.6233I$
$u = 1.398670 + 0.035211I$ $a = 0.815049 - 0.521609I$ $b = 1.42294 - 0.01679I$	$-1.87097 - 2.75507I$	0
$u = 1.398670 - 0.035211I$ $a = 0.815049 + 0.521609I$ $b = 1.42294 + 0.01679I$	$-1.87097 + 2.75507I$	0
$u = -0.259599 + 0.510135I$ $a = 1.097040 + 0.502994I$ $b = -0.487176 - 0.027827I$	$3.10941 + 0.98990I$	$-5.62147 - 3.24587I$
$u = -0.259599 - 0.510135I$ $a = 1.097040 - 0.502994I$ $b = -0.487176 + 0.027827I$	$3.10941 - 0.98990I$	$-5.62147 + 3.24587I$
$u = -0.155783 + 0.518364I$ $a = -0.34678 + 2.21283I$ $b = 0.279971 + 0.161759I$	$2.26897 - 4.12732I$	$-7.16888 + 3.41220I$
$u = -0.155783 - 0.518364I$ $a = -0.34678 - 2.21283I$ $b = 0.279971 - 0.161759I$	$2.26897 + 4.12732I$	$-7.16888 - 3.41220I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500479 + 0.194028I$ $a = -0.284102 - 1.118860I$ $b = 1.55555 - 0.14096I$	$-2.49270 + 0.60644I$	$-15.4557 - 10.2077I$
$u = -0.500479 - 0.194028I$ $a = -0.284102 + 1.118860I$ $b = 1.55555 + 0.14096I$	$-2.49270 - 0.60644I$	$-15.4557 + 10.2077I$
$u = -1.47733 + 0.20560I$ $a = -0.725820 + 0.543718I$ $b = -1.393370 - 0.049721I$	$2.40189 - 3.52842I$	0
$u = -1.47733 - 0.20560I$ $a = -0.725820 - 0.543718I$ $b = -1.393370 + 0.049721I$	$2.40189 + 3.52842I$	0
$u = -1.50553 + 0.02610I$ $a = -0.820872 - 0.167823I$ $b = -0.584397 + 0.092393I$	$-6.94722 + 0.20354I$	0
$u = -1.50553 - 0.02610I$ $a = -0.820872 + 0.167823I$ $b = -0.584397 - 0.092393I$	$-6.94722 - 0.20354I$	0
$u = -1.49289 + 0.20909I$ $a = -0.845794 - 0.652481I$ $b = -1.309020 - 0.075246I$	$4.05173 + 2.66575I$	0
$u = -1.49289 - 0.20909I$ $a = -0.845794 + 0.652481I$ $b = -1.309020 + 0.075246I$	$4.05173 - 2.66575I$	0
$u = 1.50358 + 0.19450I$ $a = 0.475568 - 0.695908I$ $b = 0.009106 - 0.203705I$	$-1.59595 - 2.66985I$	0
$u = 1.50358 - 0.19450I$ $a = 0.475568 + 0.695908I$ $b = 0.009106 + 0.203705I$	$-1.59595 + 2.66985I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.51480 + 0.19165I$	$-3.36903 + 5.10417I$	0
$a = 2.26122 + 0.97687I$		
$b = 3.13502 + 1.11443I$		
$u = -1.51480 - 0.19165I$	$-3.36903 - 5.10417I$	0
$a = 2.26122 - 0.97687I$		
$b = 3.13502 - 1.11443I$		
$u = 1.53183 + 0.05064I$	$-9.36673 - 1.46427I$	0
$a = -3.83982 + 0.14262I$		
$b = -4.60648 + 0.30137I$		
$u = 1.53183 - 0.05064I$	$-9.36673 + 1.46427I$	0
$a = -3.83982 - 0.14262I$		
$b = -4.60648 - 0.30137I$		
$u = 1.52279 + 0.19719I$	$-1.90943 - 7.69003I$	0
$a = -1.54244 + 2.21672I$		
$b = -2.17598 + 1.87956I$		
$u = 1.52279 - 0.19719I$	$-1.90943 + 7.69003I$	0
$a = -1.54244 - 2.21672I$		
$b = -2.17598 - 1.87956I$		
$u = 1.53422 + 0.10683I$	$-4.84076 - 4.12450I$	0
$a = 0.273455 - 0.876541I$		
$b = 0.465154 - 1.309920I$		
$u = 1.53422 - 0.10683I$	$-4.84076 + 4.12450I$	0
$a = 0.273455 + 0.876541I$		
$b = 0.465154 + 1.309920I$		
$u = -1.53626 + 0.07185I$	$-8.82652 + 3.73842I$	0
$a = 3.07876 + 2.19965I$		
$b = 3.75488 + 1.96290I$		
$u = -1.53626 - 0.07185I$	$-8.82652 - 3.73842I$	0
$a = 3.07876 - 2.19965I$		
$b = 3.75488 - 1.96290I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.53186 + 0.15244I$	$-4.52737 - 4.30571I$	0
$a = 1.54941 - 0.72159I$		
$b = 1.94893 - 0.88041I$		
$u = 1.53186 - 0.15244I$	$-4.52737 + 4.30571I$	0
$a = 1.54941 + 0.72159I$		
$b = 1.94893 + 0.88041I$		
$u = -1.52911 + 0.20775I$	$3.49790 + 8.09634I$	0
$a = 0.822400 - 0.471262I$		
$b = 0.592425 - 1.140080I$		
$u = -1.52911 - 0.20775I$	$3.49790 - 8.09634I$	0
$a = 0.822400 + 0.471262I$		
$b = 0.592425 + 1.140080I$		
$u = -1.53893 + 0.20501I$	$1.4654 + 14.2222I$	0
$a = -2.79319 - 1.84720I$		
$b = -3.58877 - 1.49346I$		
$u = -1.53893 - 0.20501I$	$1.4654 - 14.2222I$	0
$a = -2.79319 + 1.84720I$		
$b = -3.58877 + 1.49346I$		
$u = 1.56803 + 0.09676I$	$-6.75258 - 8.93003I$	0
$a = 3.77845 - 0.81683I$		
$b = 4.48012 - 0.48475I$		
$u = 1.56803 - 0.09676I$	$-6.75258 + 8.93003I$	0
$a = 3.77845 + 0.81683I$		
$b = 4.48012 + 0.48475I$		
$u = -1.57741 + 0.02042I$	$-8.71900 - 1.82197I$	0
$a = -3.19867 - 1.01092I$		
$b = -3.77337 - 1.31247I$		
$u = -1.57741 - 0.02042I$	$-8.71900 + 1.82197I$	0
$a = -3.19867 + 1.01092I$		
$b = -3.77337 + 1.31247I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.403832$ $a = 0.621632$ $b = 0.331645$	$-0.597749$	$-16.5810$
$u = 0.217719 + 0.282787I$ $a = 1.35864 - 1.85170I$ $b = 0.495682 + 0.230950I$	$-0.947414 + 0.254780I$	$-11.01418 + 1.68068I$
$u = 0.217719 - 0.282787I$ $a = 1.35864 + 1.85170I$ $b = 0.495682 - 0.230950I$	$-0.947414 - 0.254780I$	$-11.01418 - 1.68068I$

## II.

$$I_2^u = \langle u^4 - 2u^2 + b + 2u, -u^5 + 3u^3 + a + 1, u^6 + u^5 - 3u^4 - 2u^3 + 2u^2 - u - 1 \rangle$$

### (i) Arc colorings

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^5 - 3u^3 - 1 \\ -u^4 + 2u^2 - 2u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^5 - 3u^3 + u - 1 \\ -u^4 + 2u^2 - u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^5 - 3u^3 + u - 1 \\ -u^4 + 2u^2 - u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^5 - 2u^3 - u \\ u^5 - 3u^3 + u \end{pmatrix}$$

### (ii) Obstruction class = 1

$$(iii) \text{ Cusp Shapes} = -3u^5 - u^4 + 6u^3 + u^2 + 2u - 14$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^6$
$c_3, c_7$	$u^6$
$c_4$	$(u + 1)^6$
$c_5, c_6$	$u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1$
$c_8, c_9$	$u^6 + u^5 + 3u^4 + 2u^3 + 2u^2 + u - 1$
$c_{10}, c_{11}$	$u^6 + u^5 - 3u^4 - 2u^3 + 2u^2 - u - 1$
$c_{12}$	$u^6 - u^5 + 3u^4 - 2u^3 + 2u^2 - u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^6$
$c_3, c_7$	$y^6$
$c_5, c_6, c_{10}$ $c_{11}$	$y^6 - 7y^5 + 17y^4 - 16y^3 + 6y^2 - 5y + 1$
$c_8, c_9, c_{12}$	$y^6 + 5y^5 + 9y^4 + 4y^3 - 6y^2 - 5y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.493180 + 0.575288I$ $a = 0.011399 - 0.918055I$ $b = -0.847526 + 0.083869I$	$1.31531 - 1.97241I$	$-14.7121 + 3.8836I$
$u = 0.493180 - 0.575288I$ $a = 0.011399 + 0.918055I$ $b = -0.847526 - 0.083869I$	$1.31531 + 1.97241I$	$-14.7121 - 3.8836I$
$u = -0.483672$ $a = -0.687021$ $b = 1.38049$	$-2.38379$	$-15.3880$
$u = -1.52087 + 0.16310I$ $a = 1.98288 + 0.88048I$ $b = 2.63293 + 0.95019I$	$-5.34051 + 4.59213I$	$-18.4963 - 3.9250I$
$u = -1.52087 - 0.16310I$ $a = 1.98288 - 0.88048I$ $b = 2.63293 - 0.95019I$	$-5.34051 - 4.59213I$	$-18.4963 + 3.9250I$
$u = 1.53904$ $a = -3.30155$ $b = -3.95130$	$-9.30502$	$-18.1960$

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u-1)^6)(u^{63} + 27u^{62} + \dots + 95u + 1)$
$c_2$	$((u-1)^6)(u^{63} - 7u^{62} + \dots + u + 1)$
$c_3, c_7$	$u^6(u^{63} + u^{62} + \dots + 192u + 64)$
$c_4$	$((u+1)^6)(u^{63} - 7u^{62} + \dots + u + 1)$
$c_5, c_6$	$(u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1)(u^{63} - 2u^{62} + \dots + 2u + 1)$
$c_8, c_9$	$(u^6 + u^5 + 3u^4 + 2u^3 + 2u^2 + u - 1)(u^{63} - 8u^{62} + \dots + 6u + 7)$
$c_{10}, c_{11}$	$(u^6 + u^5 - 3u^4 - 2u^3 + 2u^2 - u - 1)(u^{63} - 2u^{62} + \dots + 2u + 1)$
$c_{12}$	$(u^6 - u^5 + 3u^4 - 2u^3 + 2u^2 - u - 1)(u^{63} - 8u^{62} + \dots + 6u + 7)$



#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y - 1)^6)(y^{63} + 25y^{62} + \dots + 5299y - 1)$
$c_2, c_4$	$((y - 1)^6)(y^{63} - 27y^{62} + \dots + 95y - 1)$
$c_3, c_7$	$y^6(y^{63} + 39y^{62} + \dots - 40960y - 4096)$
$c_5, c_6, c_{10}$ $c_{11}$	$(y^6 - 7y^5 + \dots - 5y + 1)(y^{63} - 68y^{62} + \dots + 14y - 1)$
$c_8, c_9, c_{12}$	$(y^6 + 5y^5 + \dots - 5y + 1)(y^{63} + 64y^{62} + \dots - 2246y - 49)$