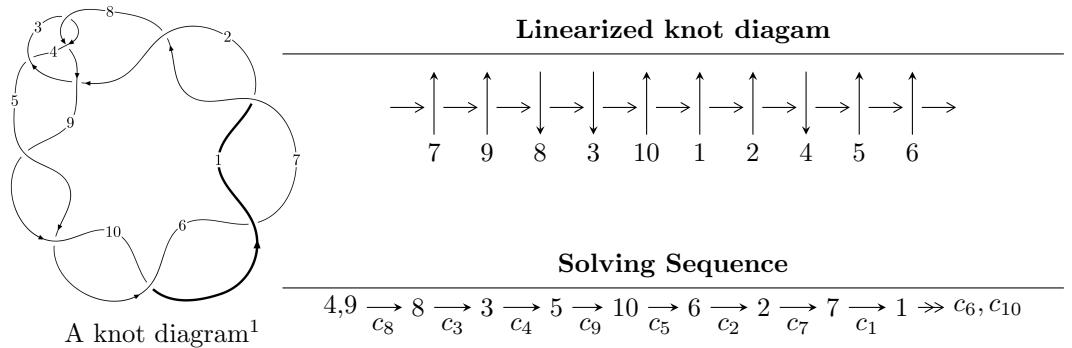


10<sub>5</sub> (K10a<sub>56</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$\begin{aligned} I_1^u &= \langle u^{15} - 3u^{13} - u^{12} + 6u^{11} + 2u^{10} - 6u^9 - 4u^8 + 5u^7 + 3u^6 - 3u^5 - 3u^4 + 3u^3 + u^2 - u - 1 \rangle \\ I_2^u &= \langle u + 1 \rangle \end{aligned}$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 16 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle u^{15} - 3u^{13} - u^{12} + 6u^{11} + 2u^{10} - 6u^9 - 4u^8 + 5u^7 + 3u^6 - 3u^5 - 3u^4 + 3u^3 + u^2 - u - 1 \rangle$$

(i) **Arc colorings**

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^8 - u^6 + u^4 + 1 \\ -u^{10} + 2u^8 - 3u^6 + 2u^4 - u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^{13} - 2u^{11} + 3u^9 - 2u^7 + 2u^5 - 2u^3 + u \\ -u^{12} + 2u^{10} + u^9 - 4u^8 - u^7 + 3u^6 + u^5 - 3u^4 + u^3 + u^2 - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^3 \\ -u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^8 - u^6 + u^4 + 1 \\ -u^8 + 2u^6 - 2u^4 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^{13} + 2u^{11} - 3u^9 + 2u^7 - 2u^5 + 2u^3 - u \\ u^{13} - 3u^{11} + 5u^9 - 4u^7 + 2u^5 - u^3 + u \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes**

$$= -4u^{14} + 12u^{12} + 4u^{11} - 20u^{10} - 8u^9 + 16u^8 + 12u^7 - 8u^6 - 8u^5 + 8u^4 + 4u^3 - 8u^2 - 4u + 10$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_5, c_6$ $c_7, c_9, c_{10}$	$u^{15} + 2u^{14} + \cdots + u + 1$
$c_2$	$u^{15} - 3u^{14} + \cdots + 21u - 5$
$c_3, c_8$	$u^{15} - 3u^{13} + \cdots - u + 1$
$c_4$	$u^{15} + 6u^{14} + \cdots + 3u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_5, c_6$ $c_7, c_9, c_{10}$	$y^{15} - 22y^{14} + \cdots + 3y - 1$
$c_2$	$y^{15} - 3y^{14} + \cdots + 241y - 25$
$c_3, c_8$	$y^{15} - 6y^{14} + \cdots + 3y - 1$
$c_4$	$y^{15} + 6y^{14} + \cdots - 17y - 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.938536 + 0.379610I$	$-1.44795 - 1.44538I$	$0.924314 + 0.710077I$
$u = 0.938536 - 0.379610I$	$-1.44795 + 1.44538I$	$0.924314 - 0.710077I$
$u = -0.496009 + 0.834142I$	$17.7129 - 1.8405I$	$12.03822 + 0.10978I$
$u = -0.496009 - 0.834142I$	$17.7129 + 1.8405I$	$12.03822 - 0.10978I$
$u = -1.004360 + 0.506467I$	$-0.48193 + 4.24481I$	$5.44692 - 7.82705I$
$u = -1.004360 - 0.506467I$	$-0.48193 - 4.24481I$	$5.44692 + 7.82705I$
$u = 0.483842 + 0.722916I$	$6.64012 + 1.24233I$	$12.05713 - 0.59928I$
$u = 0.483842 - 0.722916I$	$6.64012 - 1.24233I$	$12.05713 + 0.59928I$
$u = 1.16849$	$11.7390$	$6.35620$
$u = 1.053770 + 0.600336I$	$4.96865 - 6.29824I$	$9.18075 + 5.76248I$
$u = 1.053770 - 0.600336I$	$4.96865 + 6.29824I$	$9.18075 - 5.76248I$
$u = -1.090290 + 0.650224I$	$15.9255 + 7.3739I$	$9.68126 - 4.56542I$
$u = -1.090290 - 0.650224I$	$15.9255 - 7.3739I$	$9.68126 + 4.56542I$
$u = -0.469738 + 0.412319I$	$0.983732 - 0.215278I$	$10.49328 + 1.71815I$
$u = -0.469738 - 0.412319I$	$0.983732 + 0.215278I$	$10.49328 - 1.71815I$

**II.  $I_2^u = \langle u + 1 \rangle$**

(i) **Arc colorings**

$$a_4 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

(ii) **Obstruction class = -1**

(iii) **Cusp Shapes = 6**

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_5$	
$c_6, c_7, c_8$	$u - 1$
$c_9, c_{10}$	
$c_2$	$u$
$c_4$	$u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_5, c_6, c_7$ $c_8, c_9, c_{10}$	$y - 1$
$c_2$	$y$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$	1.64493	6.00000

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_5, c_6$ $c_7, c_9, c_{10}$	$(u - 1)(u^{15} + 2u^{14} + \cdots + u + 1)$
$c_2$	$u(u^{15} - 3u^{14} + \cdots + 21u - 5)$
$c_3, c_8$	$(u - 1)(u^{15} - 3u^{13} + \cdots - u + 1)$
$c_4$	$(u + 1)(u^{15} + 6u^{14} + \cdots + 3u + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_5, c_6$ $c_7, c_9, c_{10}$	$(y - 1)(y^{15} - 22y^{14} + \cdots + 3y - 1)$
$c_2$	$y(y^{15} - 3y^{14} + \cdots + 241y - 25)$
$c_3, c_8$	$(y - 1)(y^{15} - 6y^{14} + \cdots + 3y - 1)$
$c_4$	$(y - 1)(y^{15} + 6y^{14} + \cdots - 17y - 1)$