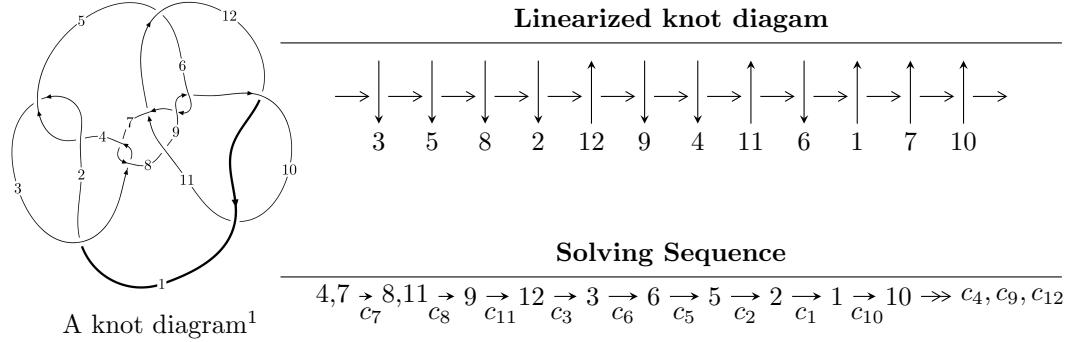


## $12a_{0115}$ ( $K12a_{0115}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle 1.03066 \times 10^{465} u^{124} + 3.82536 \times 10^{465} u^{123} + \dots + 1.54622 \times 10^{467} b + 1.91851 \times 10^{468}, \\ 7.22439 \times 10^{466} u^{124} + 2.12080 \times 10^{467} u^{123} + \dots + 2.31933 \times 10^{468} a + 1.10931 \times 10^{470}, \\ u^{125} + 2u^{124} + \dots + 512u + 512 \rangle$$

$$I_2^u = \langle b, 3a + 3u - 5, u^2 - u - 1 \rangle$$

$$I_1^v = \langle a, 16726v^8 - 41423v^7 + \dots + 11959b + 26601, \\ v^9 - 3v^8 - 2v^7 - 6v^6 + 25v^5 - 11v^4 - 9v^3 + 2v^2 + 3v - 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 136 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 1.03 \times 10^{465} u^{124} + 3.83 \times 10^{465} u^{123} + \dots + 1.55 \times 10^{467} b + 1.92 \times 10^{468}, 7.22 \times 10^{466} u^{124} + 2.12 \times 10^{467} u^{123} + \dots + 2.32 \times 10^{468} a + 1.11 \times 10^{470}, u^{125} + 2u^{124} + \dots + 512u + 512 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_4 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -0.0311487u^{124} - 0.0914405u^{123} + \dots - 13.8068u - 47.8291 \\ -0.00666572u^{124} - 0.0247401u^{123} + \dots - 5.19981u - 12.4077 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -0.0129299u^{124} - 0.0674498u^{123} + \dots + 31.3986u - 57.3336 \\ 0.00112353u^{124} + 0.0331708u^{123} + \dots - 7.29416u + 30.7948 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -0.0378144u^{124} - 0.116181u^{123} + \dots - 19.0066u - 60.2369 \\ -0.00666572u^{124} - 0.0247401u^{123} + \dots - 5.19981u - 12.4077 \end{pmatrix} \\ a_3 &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_6 &= \begin{pmatrix} -0.0591666u^{124} - 0.127059u^{123} + \dots - 50.3219u - 34.3988 \\ -0.0116249u^{124} - 0.0371386u^{123} + \dots + 1.86792u - 26.7347 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -0.0241892u^{124} - 0.0463826u^{123} + \dots - 18.7830u - 12.5336 \\ -0.0277806u^{124} - 0.0245777u^{123} + \dots - 33.9805u + 8.02032 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.0165610u^{124} + 0.00694800u^{123} + \dots - 26.5606u + 21.5758 \\ -0.0651205u^{124} - 0.0919181u^{123} + \dots - 57.3802u - 11.4736 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.00359135u^{124} + 0.0218049u^{123} + \dots - 15.1975u + 20.5539 \\ -0.0514815u^{124} - 0.0693144u^{123} + \dots - 46.9834u - 6.82131 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -0.0277532u^{124} - 0.0756995u^{123} + \dots - 20.2561u - 33.4474 \\ 0.0514815u^{124} + 0.0693144u^{123} + \dots + 46.9834u + 6.82131 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-0.0955818u^{124} - 0.136137u^{123} + \dots - 86.1084u - 11.1303$

**(iv) u-Polynomials at the component**

| Crossings        | u-Polynomials at each crossing   |
|------------------|--|
| $c_1$            | $u^{125} + 63u^{124} + \cdots + 271u + 1$  |
| $c_2, c_4$       | $u^{125} - 11u^{124} + \cdots - 9u - 1$  |
| $c_3, c_7$       | $u^{125} + 2u^{124} + \cdots + 512u + 512$                                       |
| $c_5$            | $9(9u^{125} - 12u^{124} + \cdots + 2.83664 \times 10^9 u + 2.59859 \times 10^8)$ |
| $c_6, c_9$       | $u^{125} - 3u^{124} + \cdots + 3u - 1$   |
| $c_8$            | $9(9u^{125} - 21u^{124} + \cdots + 1.22889 \times 10^8 u + 5290529)$             |
| $c_{10}, c_{12}$ | $u^{125} + 4u^{124} + \cdots - 2358u + 81$                                       |
| $c_{11}$         | $u^{125} - 2u^{124} + \cdots - 756u + 324$                                       |

**(v) Riley Polynomials at the component**

| Crossings        | Riley Polynomials at each crossing  |
|------------------|---|
| $c_1$            | $y^{125} + 9y^{124} + \cdots + 91007y - 1$  |
| $c_2, c_4$       | $y^{125} - 63y^{124} + \cdots + 271y - 1$   |
| $c_3, c_7$       | $y^{125} + 54y^{124} + \cdots - 1572864y - 262144$  |
| $c_5$            | $81(81y^{125} - 3294y^{124} + \cdots + 2.87254 \times 10^{18}y - 6.75265 \times 10^{16})$ |
| $c_6, c_9$       | $y^{125} + 85y^{124} + \cdots + 31y - 1$  |
| $c_8$            | $81 \cdot (81y^{125} - 4023y^{124} + \cdots + 7567318376329835y - 27989697099841)$        |
| $c_{10}, c_{12}$ | $y^{125} - 90y^{124} + \cdots + 665982y - 6561$   |
| $c_{11}$         | $y^{125} - 12y^{124} + \cdots + 16685352y - 104976$                                       |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -0.189225 + 0.989929I$ |                                       |            |
| $a = -2.72604 - 1.67999I$   | $4.85915 + 0.90928I$                  | 0          |
| $b = 0.545603 - 0.015975I$  |                                       |            |
| $u = -0.189225 - 0.989929I$ |                                       |            |
| $a = -2.72604 + 1.67999I$   | $4.85915 - 0.90928I$                  | 0          |
| $b = 0.545603 + 0.015975I$  |                                       |            |
| $u = 0.913335 + 0.327879I$  |                                       |            |
| $a = -0.13404 - 1.61461I$   | $4.24550 + 3.85404I$                  | 0          |
| $b = 1.42964 - 1.22199I$    |                                       |            |
| $u = 0.913335 - 0.327879I$  |                                       |            |
| $a = -0.13404 + 1.61461I$   | $4.24550 - 3.85404I$                  | 0          |
| $b = 1.42964 + 1.22199I$    |                                       |            |
| $u = 0.532227 + 0.797562I$  |                                       |            |
| $a = 1.88338 + 0.31904I$    | $-4.18791 - 0.46329I$                 | 0          |
| $b = -0.465658 + 0.870917I$ |                                       |            |
| $u = 0.532227 - 0.797562I$  |                                       |            |
| $a = 1.88338 - 0.31904I$    | $-4.18791 + 0.46329I$                 | 0          |
| $b = -0.465658 - 0.870917I$ |                                       |            |
| $u = 0.495636 + 0.814877I$  |                                       |            |
| $a = 0.168018 + 0.065540I$  | $-4.15405 - 3.73457I$                 | 0          |
| $b = 0.221515 + 1.197440I$  |                                       |            |
| $u = 0.495636 - 0.814877I$  |                                       |            |
| $a = 0.168018 - 0.065540I$  | $-4.15405 + 3.73457I$                 | 0          |
| $b = 0.221515 - 1.197440I$  |                                       |            |
| $u = 0.080750 + 1.051060I$  |                                       |            |
| $a = 1.320830 + 0.182380I$  | $2.33153 + 1.50993I$                  | 0          |
| $b = -0.932530 - 0.275816I$ |                                       |            |
| $u = 0.080750 - 1.051060I$  |                                       |            |
| $a = 1.320830 - 0.182380I$  | $2.33153 - 1.50993I$                  | 0          |
| $b = -0.932530 + 0.275816I$ |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -0.413672 + 0.836934I$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |            |
| $a = -0.275409 - 0.177834I$ | $-0.983702 - 0.642828I$               | 0          |
| $b = -0.74713 + 1.37671I$   |                                       |            |
| $u = -0.413672 - 0.836934I$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |            |
| $a = -0.275409 + 0.177834I$ | $-0.983702 + 0.642828I$               | 0          |
| $b = -0.74713 - 1.37671I$   |                                       |            |
| $u = 0.918385 + 0.543413I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |            |
| $a = 0.240683 + 0.155590I$  | $-3.67094 + 2.96823I$                 | 0          |
| $b = 0.604955 + 0.884379I$  |                                       |            |
| $u = 0.918385 - 0.543413I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |            |
| $a = 0.240683 - 0.155590I$  | $-3.67094 - 2.96823I$                 | 0          |
| $b = 0.604955 - 0.884379I$  |                                       |            |
| $u = -0.422750 + 0.821064I$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |            |
| $a = -3.17983 + 0.68595I$   | $-1.03348 + 4.20848I$                 | 0          |
| $b = 1.19189 + 1.04668I$    |                                       |            |
| $u = -0.422750 - 0.821064I$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |            |
| $a = -3.17983 - 0.68595I$   | $-1.03348 - 4.20848I$                 | 0          |
| $b = 1.19189 - 1.04668I$    |                                       |            |
| $u = -0.962365 + 0.485559I$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |            |
| $a = -0.437124 - 0.102030I$ | $-0.31912 - 6.67340I$                 | 0          |
| $b = -1.34087 + 1.13393I$   |                                       |            |
| $u = -0.962365 - 0.485559I$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |            |
| $a = -0.437124 + 0.102030I$ | $-0.31912 + 6.67340I$                 | 0          |
| $b = -1.34087 - 1.13393I$   |                                       |            |
| $u = -0.807203 + 0.430889I$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |            |
| $a = 0.056330 + 0.856214I$  | $-0.121971 - 0.719876I$               | 0          |
| $b = -0.364132 - 0.128397I$ |                                       |            |
| $u = -0.807203 - 0.430889I$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |            |
| $a = 0.056330 - 0.856214I$  | $-0.121971 + 0.719876I$               | 0          |
| $b = -0.364132 + 0.128397I$ |                                       |            |

| Solutions to $I_1^u$          | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-------------------------------|---------------------------------------|------------|
| $u = -0.828223 + 0.376343I$   |                                       |            |
| $a = 1.21716 - 1.20280I$      | $0.06073 - 2.33875I$                  | 0          |
| $b = -0.702944 - 0.443518I$   |                                       |            |
| $u = -0.828223 - 0.376343I$   |                                       |            |
| $a = 1.21716 + 1.20280I$      | $0.06073 + 2.33875I$                  | 0          |
| $b = -0.702944 + 0.443518I$   |                                       |            |
| $u = -0.599973 + 0.683518I$   |                                       |            |
| $a = -0.077597 + 0.147796I$   | $1.14990 + 7.95106I$                  | 0          |
| $b = 0.471466 + 0.834279I$    |                                       |            |
| $u = -0.599973 - 0.683518I$   |                                       |            |
| $a = -0.077597 - 0.147796I$   | $1.14990 - 7.95106I$                  | 0          |
| $b = 0.471466 - 0.834279I$    |                                       |            |
| $u = 0.402370 + 1.037470I$    |                                       |            |
| $a = -0.86209 - 1.36616I$     | $3.98203 - 1.01780I$                  | 0          |
| $b = 0.498531 - 0.049477I$    |                                       |            |
| $u = 0.402370 - 1.037470I$    |                                       |            |
| $a = -0.86209 + 1.36616I$     | $3.98203 + 1.01780I$                  | 0          |
| $b = 0.498531 + 0.049477I$    |                                       |            |
| $u = 1.090330 + 0.256832I$    |                                       |            |
| $a = -0.0476149 + 0.1171240I$ | $6.12909 + 7.71732I$                  | 0          |
| $b = 1.10513 + 0.90387I$      |                                       |            |
| $u = 1.090330 - 0.256832I$    |                                       |            |
| $a = -0.0476149 - 0.1171240I$ | $6.12909 - 7.71732I$                  | 0          |
| $b = 1.10513 - 0.90387I$      |                                       |            |
| $u = -0.248400 + 1.101470I$   |                                       |            |
| $a = -1.33263 + 0.83830I$     | $4.76652 + 0.18641I$                  | 0          |
| $b = 0.354052 + 0.770723I$    |                                       |            |
| $u = -0.248400 - 1.101470I$   |                                       |            |
| $a = -1.33263 - 0.83830I$     | $4.76652 - 0.18641I$                  | 0          |
| $b = 0.354052 - 0.770723I$    |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape      |
|-----------------------------|---------------------------------------|-----------------|
| $u = -0.433618 + 1.055720I$ |                                       |                 |
| $a = 2.35530 - 0.20832I$    | $3.54058 + 9.87816I$                  | 0               |
| $b = -1.11177 - 1.01672I$   |                                       |                 |
| $u = -0.433618 - 1.055720I$ |                                       |                 |
| $a = 2.35530 + 0.20832I$    | $3.54058 - 9.87816I$                  | 0               |
| $b = -1.11177 + 1.01672I$   |                                       |                 |
| $u = -0.442173 + 1.054840I$ |                                       |                 |
| $a = 1.210110 - 0.399870I$  | $1.15542 + 3.12032I$                  | 0               |
| $b = -1.063990 - 0.003120I$ |                                       |                 |
| $u = -0.442173 - 1.054840I$ |                                       |                 |
| $a = 1.210110 + 0.399870I$  | $1.15542 - 3.12032I$                  | 0               |
| $b = -1.063990 + 0.003120I$ |                                       |                 |
| $u = -0.840842 + 0.156626I$ |                                       |                 |
| $a = 0.52324 - 1.86364I$    | $4.74563 + 0.17252I$                  | $5.48395 + 0.I$ |
| $b = 0.84914 - 1.46811I$    |                                       |                 |
| $u = -0.840842 - 0.156626I$ |                                       |                 |
| $a = 0.52324 + 1.86364I$    | $4.74563 - 0.17252I$                  | $5.48395 + 0.I$ |
| $b = 0.84914 + 1.46811I$    |                                       |                 |
| $u = -0.064934 + 1.160180I$ |                                       |                 |
| $a = -1.74953 + 0.85168I$   | $5.99018 - 4.39123I$                  | 0               |
| $b = 1.73930 - 0.46575I$    |                                       |                 |
| $u = -0.064934 - 1.160180I$ |                                       |                 |
| $a = -1.74953 - 0.85168I$   | $5.99018 + 4.39123I$                  | 0               |
| $b = 1.73930 + 0.46575I$    |                                       |                 |
| $u = 0.380832 + 1.099280I$  |                                       |                 |
| $a = -1.49403 + 0.23024I$   | $-1.50629 - 4.23005I$                 | 0               |
| $b = 0.649724 - 0.705708I$  |                                       |                 |
| $u = 0.380832 - 1.099280I$  |                                       |                 |
| $a = -1.49403 - 0.23024I$   | $-1.50629 + 4.23005I$                 | 0               |
| $b = 0.649724 + 0.705708I$  |                                       |                 |

| Solutions to $I_1^u$          | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape      |
|-------------------------------|---------------------------------------|-----------------|
| $u = 0.349086 + 1.109990I$    |                                       |                 |
| $a = -1.222110 - 0.226288I$   | $4.36419 - 2.43164I$                  | 0               |
| $b = 0.746699 + 0.641099I$    |                                       |                 |
| $u = 0.349086 - 1.109990I$    |                                       |                 |
| $a = -1.222110 + 0.226288I$   | $4.36419 + 2.43164I$                  | 0               |
| $b = 0.746699 - 0.641099I$    |                                       |                 |
| $u = 0.375408 + 1.108420I$    |                                       |                 |
| $a = -1.25787 - 1.15535I$     | $5.08150 - 0.59588I$                  | 0               |
| $b = 1.85937 - 0.00043I$      |                                       |                 |
| $u = 0.375408 - 1.108420I$    |                                       |                 |
| $a = -1.25787 + 1.15535I$     | $5.08150 + 0.59588I$                  | 0               |
| $b = 1.85937 + 0.00043I$      |                                       |                 |
| $u = -0.235520 + 0.777319I$   |                                       |                 |
| $a = -0.153207 + 0.244390I$   | $-0.40273 + 3.66473I$                 | $0. - 6.36269I$ |
| $b = -0.262287 - 1.105520I$   |                                       |                 |
| $u = -0.235520 - 0.777319I$   |                                       |                 |
| $a = -0.153207 - 0.244390I$   | $-0.40273 - 3.66473I$                 | $0. + 6.36269I$ |
| $b = -0.262287 + 1.105520I$   |                                       |                 |
| $u = 1.112620 + 0.422938I$    |                                       |                 |
| $a = -0.0662946 - 0.1070030I$ | $5.54144 - 5.18578I$                  | 0               |
| $b = 0.823523 - 0.441900I$    |                                       |                 |
| $u = 1.112620 - 0.422938I$    |                                       |                 |
| $a = -0.0662946 + 0.1070030I$ | $5.54144 + 5.18578I$                  | 0               |
| $b = 0.823523 + 0.441900I$    |                                       |                 |
| $u = 0.523784 + 1.069500I$    |                                       |                 |
| $a = -4.10601 - 0.42204I$     | $3.20788 - 5.56394I$                  | 0               |
| $b = 0.376955 - 0.151157I$    |                                       |                 |
| $u = 0.523784 - 1.069500I$    |                                       |                 |
| $a = -4.10601 + 0.42204I$     | $3.20788 + 5.56394I$                  | 0               |
| $b = 0.376955 + 0.151157I$    |                                       |                 |

| Solutions to $I_1^u$         | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|------------------------------|---------------------------------------|-----------------------|
| $u = 0.634089 + 0.498710I$   |                                       |                       |
| $a = 3.69497 + 8.88764I$     | $1.42901 + 1.00847I$                  | $-31.0649 + 44.2359I$ |
| $b = -0.145181 + 0.241855I$  |                                       |                       |
| $u = 0.634089 - 0.498710I$   |                                       |                       |
| $a = 3.69497 - 8.88764I$     | $1.42901 - 1.00847I$                  | $-31.0649 - 44.2359I$ |
| $b = -0.145181 - 0.241855I$  |                                       |                       |
| $u = -0.505552 + 1.083710I$  |                                       |                       |
| $a = 1.41400 - 0.27693I$     | $0.63717 + 3.65490I$                  | 0                     |
| $b = -0.785972 - 0.862103I$  |                                       |                       |
| $u = -0.505552 - 1.083710I$  |                                       |                       |
| $a = 1.41400 + 0.27693I$     | $0.63717 - 3.65490I$                  | 0                     |
| $b = -0.785972 + 0.862103I$  |                                       |                       |
| $u = -1.185770 + 0.210987I$  |                                       |                       |
| $a = 0.0868843 - 0.0106217I$ | $0.98816 - 1.89695I$                  | 0                     |
| $b = -0.608506 + 0.512349I$  |                                       |                       |
| $u = -1.185770 - 0.210987I$  |                                       |                       |
| $a = 0.0868843 + 0.0106217I$ | $0.98816 + 1.89695I$                  | 0                     |
| $b = -0.608506 - 0.512349I$  |                                       |                       |
| $u = -0.666834 + 0.423916I$  |                                       |                       |
| $a = 0.286152 - 0.017589I$   | $-1.37803 + 0.83267I$                 | $-5.49260 - 3.40594I$ |
| $b = 0.257842 - 0.749663I$   |                                       |                       |
| $u = -0.666834 - 0.423916I$  |                                       |                       |
| $a = 0.286152 + 0.017589I$   | $-1.37803 - 0.83267I$                 | $-5.49260 + 3.40594I$ |
| $b = 0.257842 + 0.749663I$   |                                       |                       |
| $u = 0.234448 + 1.189590I$   |                                       |                       |
| $a = 1.74701 - 0.56723I$     | $9.39087 + 0.67963I$                  | 0                     |
| $b = -1.01937 + 1.93388I$    |                                       |                       |
| $u = 0.234448 - 1.189590I$   |                                       |                       |
| $a = 1.74701 + 0.56723I$     | $9.39087 - 0.67963I$                  | 0                     |
| $b = -1.01937 - 1.93388I$    |                                       |                       |

| Solutions to $I_1^u$          | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-------------------------------|---------------------------------------|----------------------|
| $u = 0.750828 + 0.154017I$    |                                       |                      |
| $a = -0.540540 + 0.290736I$   | $1.33029 + 2.74208I$                  | $0.45355 - 2.62957I$ |
| $b = -1.094100 - 0.737261I$   |                                       |                      |
| $u = 0.750828 - 0.154017I$    |                                       |                      |
| $a = -0.540540 - 0.290736I$   | $1.33029 - 2.74208I$                  | $0.45355 + 2.62957I$ |
| $b = -1.094100 + 0.737261I$   |                                       |                      |
| $u = -0.360615 + 1.181320I$   |                                       |                      |
| $a = 0.77945 - 1.47555I$      | $8.85777 + 3.95009I$                  | 0                    |
| $b = -1.65817 + 1.47843I$     |                                       |                      |
| $u = -0.360615 - 1.181320I$   |                                       |                      |
| $a = 0.77945 + 1.47555I$      | $8.85777 - 3.95009I$                  | 0                    |
| $b = -1.65817 - 1.47843I$     |                                       |                      |
| $u = 0.521373 + 1.124290I$    |                                       |                      |
| $a = -0.96167 - 1.14782I$     | $3.12453 - 5.20896I$                  | 0                    |
| $b = 0.202332 - 0.843758I$    |                                       |                      |
| $u = 0.521373 - 1.124290I$    |                                       |                      |
| $a = -0.96167 + 1.14782I$     | $3.12453 + 5.20896I$                  | 0                    |
| $b = 0.202332 + 0.843758I$    |                                       |                      |
| $u = -1.124900 + 0.535801I$   |                                       |                      |
| $a = -0.0411915 - 0.1178360I$ | $4.42812 - 12.73300I$                 | 0                    |
| $b = 1.16484 - 1.07257I$      |                                       |                      |
| $u = -1.124900 - 0.535801I$   |                                       |                      |
| $a = -0.0411915 + 0.1178360I$ | $4.42812 + 12.73300I$                 | 0                    |
| $b = 1.16484 + 1.07257I$      |                                       |                      |
| $u = 0.492797 + 1.146900I$    |                                       |                      |
| $a = -2.03102 - 0.36281I$     | $4.19431 - 7.27901I$                  | 0                    |
| $b = 1.54887 - 1.18166I$      |                                       |                      |
| $u = 0.492797 - 1.146900I$    |                                       |                      |
| $a = -2.03102 + 0.36281I$     | $4.19431 + 7.27901I$                  | 0                    |
| $b = 1.54887 + 1.18166I$      |                                       |                      |

| Solutions to $I_1^u$         | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|------------------------------|---------------------------------------|-----------------------|
| $u = -0.615779 + 1.088750I$  |                                       |                       |
| $a = -0.650976 + 1.024930I$  | $1.80618 + 5.96754I$                  | 0                     |
| $b = 0.414729 + 0.215546I$   |                                       |                       |
| $u = -0.615779 - 1.088750I$  |                                       |                       |
| $a = -0.650976 - 1.024930I$  | $1.80618 - 5.96754I$                  | 0                     |
| $b = 0.414729 - 0.215546I$   |                                       |                       |
| $u = 0.699810 + 0.253258I$   |                                       |                       |
| $a = 0.45949 - 2.64155I$     | $0.621061 + 0.585081I$                | $-8.38094 - 6.55158I$ |
| $b = -0.233666 - 0.523885I$  |                                       |                       |
| $u = 0.699810 - 0.253258I$   |                                       |                       |
| $a = 0.45949 + 2.64155I$     | $0.621061 - 0.585081I$                | $-8.38094 + 6.55158I$ |
| $b = -0.233666 + 0.523885I$  |                                       |                       |
| $u = 1.156140 + 0.507162I$   |                                       |                       |
| $a = 0.0934185 - 0.0006937I$ | $-0.51148 + 7.10641I$                 | 0                     |
| $b = -0.757298 - 0.778048I$  |                                       |                       |
| $u = 1.156140 - 0.507162I$   |                                       |                       |
| $a = 0.0934185 + 0.0006937I$ | $-0.51148 - 7.10641I$                 | 0                     |
| $b = -0.757298 + 0.778048I$  |                                       |                       |
| $u = -0.329817 + 0.655522I$  |                                       |                       |
| $a = 0.27779 + 2.85032I$     | $-0.74776 - 1.32568I$                 | $-1.37223 - 2.12566I$ |
| $b = 0.435012 - 0.387028I$   |                                       |                       |
| $u = -0.329817 - 0.655522I$  |                                       |                       |
| $a = 0.27779 - 2.85032I$     | $-0.74776 + 1.32568I$                 | $-1.37223 + 2.12566I$ |
| $b = 0.435012 + 0.387028I$   |                                       |                       |
| $u = -0.585773 + 1.136850I$  |                                       |                       |
| $a = 0.270868 - 0.774974I$   | $2.57218 - 2.94748I$                  | 0                     |
| $b = -0.675543 + 0.280117I$  |                                       |                       |
| $u = -0.585773 - 1.136850I$  |                                       |                       |
| $a = 0.270868 + 0.774974I$   | $2.57218 + 2.94748I$                  | 0                     |
| $b = -0.675543 - 0.280117I$  |                                       |                       |

| Solutions to $I_1^u$         | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|------------------------------|---------------------------------------|-----------------------|
| $u = 0.164951 + 0.699060I$   |                                       |                       |
| $a = 2.01057 + 3.83403I$     | $3.23791 - 1.80187I$                  | $7.60062 + 5.39442I$  |
| $b = -1.12027 - 1.11356I$    |                                       |                       |
| $u = 0.164951 - 0.699060I$   |                                       |                       |
| $a = 2.01057 - 3.83403I$     | $3.23791 + 1.80187I$                  | $7.60062 - 5.39442I$  |
| $b = -1.12027 + 1.11356I$    |                                       |                       |
| $u = -0.494783 + 1.183550I$  |                                       |                       |
| $a = 1.67549 + 0.02049I$     | $7.89707 + 4.62521I$                  | 0                     |
| $b = -0.72180 - 2.14415I$    |                                       |                       |
| $u = -0.494783 - 1.183550I$  |                                       |                       |
| $a = 1.67549 - 0.02049I$     | $7.89707 - 4.62521I$                  | 0                     |
| $b = -0.72180 + 2.14415I$    |                                       |                       |
| $u = -0.581083 + 1.144450I$  |                                       |                       |
| $a = -0.927414 + 0.371926I$  | $2.41939 + 7.59298I$                  | 0                     |
| $b = 0.912764 - 0.614051I$   |                                       |                       |
| $u = -0.581083 - 1.144450I$  |                                       |                       |
| $a = -0.927414 - 0.371926I$  | $2.41939 - 7.59298I$                  | 0                     |
| $b = 0.912764 + 0.614051I$   |                                       |                       |
| $u = 0.277864 + 0.645271I$   |                                       |                       |
| $a = 0.1293420 - 0.0177373I$ | $-3.17582 + 1.37189I$                 | $-2.02901 + 3.10189I$ |
| $b = -0.259855 - 1.133830I$  |                                       |                       |
| $u = 0.277864 - 0.645271I$   |                                       |                       |
| $a = 0.1293420 + 0.0177373I$ | $-3.17582 - 1.37189I$                 | $-2.02901 - 3.10189I$ |
| $b = -0.259855 + 1.133830I$  |                                       |                       |
| $u = -0.349910 + 0.596945I$  |                                       |                       |
| $a = -0.044338 - 0.135561I$  | $1.92234 - 6.42207I$                  | $1.61043 - 2.58323I$  |
| $b = 0.776083 - 1.123390I$   |                                       |                       |
| $u = -0.349910 - 0.596945I$  |                                       |                       |
| $a = -0.044338 + 0.135561I$  | $1.92234 + 6.42207I$                  | $1.61043 + 2.58323I$  |
| $b = 0.776083 + 1.123390I$   |                                       |                       |

| Solutions to $I_1^u$          | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-------------------------------|---------------------------------------|----------------------|
| $u = 0.675342 + 0.102623I$    |                                       |                      |
| $a = -0.475944 - 0.632806I$   | $1.33240 - 2.49877I$                  | $0.06108 + 4.74869I$ |
| $b = -0.798997 + 0.456385I$   |                                       |                      |
| $u = 0.675342 - 0.102623I$    |                                       |                      |
| $a = -0.475944 + 0.632806I$   | $1.33240 + 2.49877I$                  | $0.06108 - 4.74869I$ |
| $b = -0.798997 - 0.456385I$   |                                       |                      |
| $u = 0.675422 + 1.130710I$    |                                       |                      |
| $a = 1.322000 + 0.441156I$    | $-1.80399 - 8.86816I$                 | 0                    |
| $b = -0.812816 + 1.037590I$   |                                       |                      |
| $u = 0.675422 - 1.130710I$    |                                       |                      |
| $a = 1.322000 - 0.441156I$    | $-1.80399 + 8.86816I$                 | 0                    |
| $b = -0.812816 - 1.037590I$   |                                       |                      |
| $u = 0.585027 + 1.188980I$    |                                       |                      |
| $a = 0.35499 + 1.37574I$      | $6.93778 - 9.34093I$                  | 0                    |
| $b = -1.89934 - 1.32123I$     |                                       |                      |
| $u = 0.585027 - 1.188980I$    |                                       |                      |
| $a = 0.35499 - 1.37574I$      | $6.93778 + 9.34093I$                  | 0                    |
| $b = -1.89934 + 1.32123I$     |                                       |                      |
| $u = -0.670642 + 1.165170I$   |                                       |                      |
| $a = -1.78726 + 0.65220I$     | $1.83437 + 12.66320I$                 | 0                    |
| $b = 1.52212 + 1.38459I$      |                                       |                      |
| $u = -0.670642 - 1.165170I$   |                                       |                      |
| $a = -1.78726 - 0.65220I$     | $1.83437 - 12.66320I$                 | 0                    |
| $b = 1.52212 - 1.38459I$      |                                       |                      |
| $u = -1.212360 + 0.646222I$   |                                       |                      |
| $a = -0.0620166 + 0.0911191I$ | $3.33646 - 0.19030I$                  | 0                    |
| $b = 0.676884 + 0.094872I$    |                                       |                      |
| $u = -1.212360 - 0.646222I$   |                                       |                      |
| $a = -0.0620166 - 0.0911191I$ | $3.33646 + 0.19030I$                  | 0                    |
| $b = 0.676884 - 0.094872I$    |                                       |                      |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------|---------------------------------------|----------------------|
| $u = -0.327090 + 0.526695I$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                      |
| $a = -2.03892 + 2.29943I$   | $-0.596246 + 0.416978I$               | $0.26642 - 6.11778I$ |
| $b = 0.609994 - 0.249849I$  |                                       |                      |
| $u = -0.327090 - 0.526695I$ |                                       |                      |
| $a = -2.03892 - 2.29943I$   | $-0.596246 - 0.416978I$               | $0.26642 + 6.11778I$ |
| $b = 0.609994 + 0.249849I$  |                                       |                      |
| $u = 0.612331 + 1.251960I$  |                                       |                      |
| $a = 1.73548 + 0.43034I$    | $9.2901 - 13.7168I$                   | 0                    |
| $b = -1.25293 + 1.11281I$   |                                       |                      |
| $u = 0.612331 - 1.251960I$  |                                       |                      |
| $a = 1.73548 - 0.43034I$    | $9.2901 + 13.7168I$                   | 0                    |
| $b = -1.25293 - 1.11281I$   |                                       |                      |
| $u = -0.60524 + 1.28225I$   |                                       |                      |
| $a = -1.283780 + 0.186550I$ | $4.45793 + 8.07080I$                  | 0                    |
| $b = 0.904103 + 0.810181I$  |                                       |                      |
| $u = -0.60524 - 1.28225I$   |                                       |                      |
| $a = -1.283780 - 0.186550I$ | $4.45793 - 8.07080I$                  | 0                    |
| $b = 0.904103 - 0.810181I$  |                                       |                      |
| $u = -0.75455 + 1.21679I$   |                                       |                      |
| $a = 1.62826 - 0.67265I$    | $6.6329 + 19.4885I$                   | 0                    |
| $b = -1.23586 - 1.20855I$   |                                       |                      |
| $u = -0.75455 - 1.21679I$   |                                       |                      |
| $a = 1.62826 + 0.67265I$    | $6.6329 - 19.4885I$                   | 0                    |
| $b = -1.23586 + 1.20855I$   |                                       |                      |
| $u = 0.07864 + 1.43412I$    |                                       |                      |
| $a = 1.38519 - 0.43108I$    | $12.5560 - 9.3062I$                   | 0                    |
| $b = -1.30927 + 0.70376I$   |                                       |                      |
| $u = 0.07864 - 1.43412I$    |                                       |                      |
| $a = 1.38519 + 0.43108I$    | $12.5560 + 9.3062I$                   | 0                    |
| $b = -1.30927 - 0.70376I$   |                                       |                      |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = 0.75063 + 1.23502I$    |                                       |            |
| $a = -1.301480 - 0.365678I$ | $1.84566 - 13.92260I$                 | 0          |
| $b = 0.913051 - 0.950042I$  |                                       |            |
| $u = 0.75063 - 1.23502I$    |                                       |            |
| $a = -1.301480 + 0.365678I$ | $1.84566 + 13.92260I$                 | 0          |
| $b = 0.913051 + 0.950042I$  |                                       |            |
| $u = 0.15570 + 1.44249I$    |                                       |            |
| $a = 1.116080 + 0.615912I$  | $12.41370 + 3.14260I$                 | 0          |
| $b = -1.255060 - 0.503238I$ |                                       |            |
| $u = 0.15570 - 1.44249I$    |                                       |            |
| $a = 1.116080 - 0.615912I$  | $12.41370 - 3.14260I$                 | 0          |
| $b = -1.255060 + 0.503238I$ |                                       |            |
| $u = -0.546681$             |                                       |            |
| $a = 0.853690$              | -1.13268                              | -9.63470   |
| $b = 0.327961$              |                                       |            |
| $u = 0.69181 + 1.30600I$    |                                       |            |
| $a = 0.556692 + 0.479724I$  | $8.30974 - 1.49559I$                  | 0          |
| $b = -0.828035 + 0.099208I$ |                                       |            |
| $u = 0.69181 - 1.30600I$    |                                       |            |
| $a = 0.556692 - 0.479724I$  | $8.30974 + 1.49559I$                  | 0          |
| $b = -0.828035 - 0.099208I$ |                                       |            |
| $u = -0.79848 + 1.26772I$   |                                       |            |
| $a = 0.617339 - 0.371174I$  | $5.49346 + 7.52898I$                  | 0          |
| $b = -0.753084 - 0.344913I$ |                                       |            |
| $u = -0.79848 - 1.26772I$   |                                       |            |
| $a = 0.617339 + 0.371174I$  | $5.49346 - 7.52898I$                  | 0          |
| $b = -0.753084 + 0.344913I$ |                                       |            |
| $u = -0.09910 + 1.49843I$   |                                       |            |
| $a = -0.912897 - 0.029897I$ | $7.75260 + 3.19534I$                  | 0          |
| $b = 0.928225 + 0.156147I$  |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------|---------------------------------------|----------------------|
| $u = -0.09910 - 1.49843I$   |                                       |                      |
| $a = -0.912897 + 0.029897I$ | $7.75260 - 3.19534I$                  | 0                    |
| $b = 0.928225 - 0.156147I$  |                                       |                      |
| $u = -0.234925 + 0.344834I$ |                                       |                      |
| $a = -0.39694 - 3.35327I$   | $4.30327 + 1.14568I$                  | $3.56993 + 0.21405I$ |
| $b = 0.591198 - 0.673652I$  |                                       |                      |
| $u = -0.234925 - 0.344834I$ |                                       |                      |
| $a = -0.39694 + 3.35327I$   | $4.30327 - 1.14568I$                  | $3.56993 - 0.21405I$ |
| $b = 0.591198 + 0.673652I$  |                                       |                      |
| $u = 1.62729$               |                                       |                      |
| $a = 0.0237227$             | -7.22833                              | 0                    |
| $b = -0.0964470$            |                                       |                      |
| $u = 0.239647$              |                                       |                      |
| $a = 3.21183$               | 1.26613                               | 9.42890              |
| $b = -0.449696$             |                                       |                      |

$$\text{II. } I_2^u = \langle b, 3a + 3u - 5, u^2 - u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_4 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ u+1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u + \frac{5}{3} \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -\frac{8}{9}u + \frac{22}{9} \\ u+1 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -u + \frac{5}{3} \\ 0 \end{pmatrix} \\ a_3 &= \begin{pmatrix} u \\ 3u+1 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -\frac{2}{3}u - \frac{5}{9} \\ -3u-2 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u \\ -3u-2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -1 \\ -2u-2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -2u-2 \\ -9u-6 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u + \frac{11}{3} \\ 9u+6 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-\frac{560}{3}u - \frac{1105}{9}$

**(iv) u-Polynomials at the component**

| Crossings  | u-Polynomials at each crossing |
|------------|--------------------------------|
| $c_1, c_6$ | $u^2 - 3u + 1$                 |
| $c_2, c_3$ | $u^2 + u - 1$                  |
| $c_4, c_7$ | $u^2 - u - 1$                  |
| $c_5$      | $(3u - 1)^2$                   |
| $c_8$      | $9u^2 + 9u + 1$                |
| $c_9$      | $u^2 + 3u + 1$                 |
| $c_{10}$   | $(u + 1)^2$                    |
| $c_{11}$   | $u^2$                          |
| $c_{12}$   | $(u - 1)^2$                    |

**(v) Riley Polynomials at the component**

| Crossings                | Riley Polynomials at each crossing |
|--------------------------|------------------------------------|
| $c_1, c_6, c_9$          | $y^2 - 7y + 1$                     |
| $c_2, c_3, c_4$<br>$c_7$ | $y^2 - 3y + 1$                     |
| $c_5$                    | $(9y - 1)^2$                       |
| $c_8$                    | $81y^2 - 63y + 1$                  |
| $c_{10}, c_{12}$         | $(y - 1)^2$                        |
| $c_{11}$                 | $y^2$                              |

**(vi) Complex Volumes and Cusp Shapes**

| Solutions to $I_2^u$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|---------------------------------------|------------|
| $u = -0.618034$      |                                       |            |
| $a = 2.28470$        | 0.657974                              | -7.41140   |
| $b = 0$              |                                       |            |
| $u = 1.61803$        |                                       |            |
| $a = 0.0486327$      | -7.23771                              | -424.810   |
| $b = 0$              |                                       |            |

### III.

$$I_1^v = \langle a, 16726v^8 - 41423v^7 + \cdots + 11959b + 26601, v^9 - 3v^8 + \cdots + 3v - 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_4 &= \begin{pmatrix} v \\ 0 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ -1.39861v^8 + 3.46375v^7 + \cdots + 3.94598v - 2.22435 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ 1.45213v^8 - 3.82515v^7 + \cdots - 3.73944v + 4.14098 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -1.39861v^8 + 3.46375v^7 + \cdots + 3.94598v - 2.22435 \\ -1.39861v^8 + 3.46375v^7 + \cdots + 3.94598v - 2.22435 \end{pmatrix} \\ a_3 &= \begin{pmatrix} v \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -1.45213v^8 + 3.82515v^7 + \cdots + 3.73944v - 3.14098 \\ -1.21114v^8 + 2.94147v^7 + \cdots + 5.63826v - 2.00702 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0.759010v^8 - 2.11631v^7 + \cdots + 0.101179v + 1.86604 \\ v^8 - 3v^7 - 2v^6 - 6v^5 + 25v^4 - 11v^3 - 9v^2 + 2v + 3 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.759010v^8 + 2.11631v^7 + \cdots + 0.898821v - 1.86604 \\ -v^8 + 3v^7 + 2v^6 + 6v^5 - 25v^4 + 11v^3 + 9v^2 - 2v - 3 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.759010v^8 + 2.11631v^7 + \cdots - 0.101179v - 1.86604 \\ -v^8 + 3v^7 + 2v^6 + 6v^5 - 25v^4 + 11v^3 + 9v^2 - 2v - 3 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -0.240990v^8 + 0.883686v^7 + \cdots - 1.89882v - 1.13396 \\ -v^8 + 3v^7 + 2v^6 + 6v^5 - 25v^4 + 11v^3 + 9v^2 - 2v - 3 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes =**  
 $\frac{109765}{11959}v^8 - \frac{294476}{11959}v^7 - \frac{325323}{11959}v^6 - \frac{729072}{11959}v^5 + \frac{2542695}{11959}v^4 - \frac{295872}{11959}v^3 - \frac{1329263}{11959}v^2 - \frac{115465}{11959}v + \frac{259811}{11959}$

**(iv) u-Polynomials at the component**

| Crossings  | u-Polynomials at each crossing                                     |
|------------|--|
| $c_1, c_2$ | $(u - 1)^9$  |
| $c_3, c_7$ | $u^9$  |
| $c_4$      | $(u + 1)^9$  |
| $c_5$      | $u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1$    |
| $c_6$      | $u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1$ |
| $c_8$      | $u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1$               |
| $c_9$      | $u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1$ |
| $c_{10}$   | $u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1$              |
| $c_{11}$   | $u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1$               |
| $c_{12}$   | $u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1$              |

**(v) Riley Polynomials at the component**

| Crossings        | Riley Polynomials at each crossing                                 |
|------------------|--|
| $c_1, c_2, c_4$  | $(y - 1)^9$  |
| $c_3, c_7$       | $y^9$  |
| $c_5$            | $y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1$          |
| $c_6, c_9$       | $y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1$      |
| $c_8, c_{11}$    | $y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1$ |
| $c_{10}, c_{12}$ | $y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1$    |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^v$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $v = 1.022450 + 0.246780I$  |                                       |                       |
| $a = 0$                     | $-1.02799 - 2.45442I$                 | $-3.88318 + 3.00529I$ |
| $b = -0.628449 + 0.875112I$ |                                       |                       |
| $v = 1.022450 - 0.246780I$  |                                       |                       |
| $a = 0$                     | $-1.02799 + 2.45442I$                 | $-3.88318 - 3.00529I$ |
| $b = -0.628449 - 0.875112I$ |                                       |                       |
| $v = -0.483566 + 0.305056I$ |                                       |                       |
| $a = 0$                     | $-3.42837 - 2.09337I$                 | $-7.05683 + 6.62869I$ |
| $b = -0.140343 + 0.966856I$ |                                       |                       |
| $v = -0.483566 - 0.305056I$ |                                       |                       |
| $a = 0$                     | $-3.42837 + 2.09337I$                 | $-7.05683 - 6.62869I$ |
| $b = -0.140343 - 0.966856I$ |                                       |                       |
| $v = 0.411691 + 0.129409I$  |                                       |                       |
| $a = 0$                     | $1.95319 + 7.08493I$                  | $2.13339 - 8.87891I$  |
| $b = 0.728966 + 0.986295I$  |                                       |                       |
| $v = 0.411691 - 0.129409I$  |                                       |                       |
| $a = 0$                     | $1.95319 - 7.08493I$                  | $2.13339 + 8.87891I$  |
| $b = 0.728966 - 0.986295I$  |                                       |                       |
| $v = -1.23246 + 1.62704I$   |                                       |                       |
| $a = 0$                     | $2.72642 - 1.33617I$                  | $-1.90921 - 3.07774I$ |
| $b = 0.796005 + 0.733148I$  |                                       |                       |
| $v = -1.23246 - 1.62704I$   |                                       |                       |
| $a = 0$                     | $2.72642 + 1.33617I$                  | $-1.90921 + 3.07774I$ |
| $b = 0.796005 - 0.733148I$  |                                       |                       |
| $v = 3.56378$               |                                       |                       |
| $a = 0$                     | $-0.446489$                           | $13.4320$             |
| $b = -0.512358$             |                                       |                       |

#### IV. u-Polynomials

| Crossings | u-Polynomials at each crossing   |
|-----------|--|
| $c_1$     | $((u - 1)^9)(u^2 - 3u + 1)(u^{125} + 63u^{124} + \dots + 271u + 1)$  |
| $c_2$     | $((u - 1)^9)(u^2 + u - 1)(u^{125} - 11u^{124} + \dots - 9u - 1)$   |
| $c_3$     | $u^9(u^2 + u - 1)(u^{125} + 2u^{124} + \dots + 512u + 512)$  |
| $c_4$     | $((u + 1)^9)(u^2 - u - 1)(u^{125} - 11u^{124} + \dots - 9u - 1)$   |
| $c_5$     | $(3u - 1)^2(u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1) \cdot (9u^{125} - 12u^{124} + \dots + 2836642102u + 259858639)$ |
| $c_6$     | $(u^2 - 3u + 1)(u^9 - 3u^8 + \dots + u + 1) \cdot (u^{125} - 3u^{124} + \dots + 3u - 1)$   |
| $c_7$     | $u^9(u^2 - u - 1)(u^{125} + 2u^{124} + \dots + 512u + 512)$  |
| $c_8$     | $(9u^2 + 9u + 1)(u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1) \cdot (9u^{125} - 21u^{124} + \dots + 122889219u + 5290529)$          |
| $c_9$     | $(u^2 + 3u + 1)(u^9 + 3u^8 + \dots + u - 1) \cdot (u^{125} - 3u^{124} + \dots + 3u - 1)$   |
| $c_{10}$  | $(u + 1)^2(u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1) \cdot (u^{125} + 4u^{124} + \dots - 2358u + 81)$                           |
| $c_{11}$  | $u^2(u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1) \cdot (u^{125} - 2u^{124} + \dots - 756u + 324)$                                  |
| $c_{12}$  | $(u - 1)^2(u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1) \cdot (u^{125} + 4u^{124} + \dots - 2358u + 81)$                           |

## V. Riley Polynomials

| Crossings        | Riley Polynomials at each crossing  |
|------------------|---|
| $c_1$            | $((y - 1)^9)(y^2 - 7y + 1)(y^{125} + 9y^{124} + \dots + 91007y - 1)$  |
| $c_2, c_4$       | $((y - 1)^9)(y^2 - 3y + 1)(y^{125} - 63y^{124} + \dots + 271y - 1)$   |
| $c_3, c_7$       | $y^9(y^2 - 3y + 1)(y^{125} + 54y^{124} + \dots - 1572864y - 262144)$  |
| $c_5$            | $(9y - 1)^2(y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1)$<br>$\cdot (81y^{125} - 3294y^{124} + \dots + 2.87 \times 10^{18}y - 6.75 \times 10^{16})$                     |
| $c_6, c_9$       | $(y^2 - 7y + 1)(y^9 + 7y^8 + \dots + 13y - 1)$<br>$\cdot (y^{125} + 85y^{124} + \dots + 31y - 1)$   |
| $c_8$            | $(81y^2 - 63y + 1)$<br>$\cdot (y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)$<br>$\cdot (81y^{125} - 4023y^{124} + \dots + 7567318376329835y - 27989697099841)$ |
| $c_{10}, c_{12}$ | $(y - 1)^2(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)$<br>$\cdot (y^{125} - 90y^{124} + \dots + 665982y - 6561)$  |
| $c_{11}$         | $y^2(y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)$<br>$\cdot (y^{125} - 12y^{124} + \dots + 16685352y - 104976)$   |