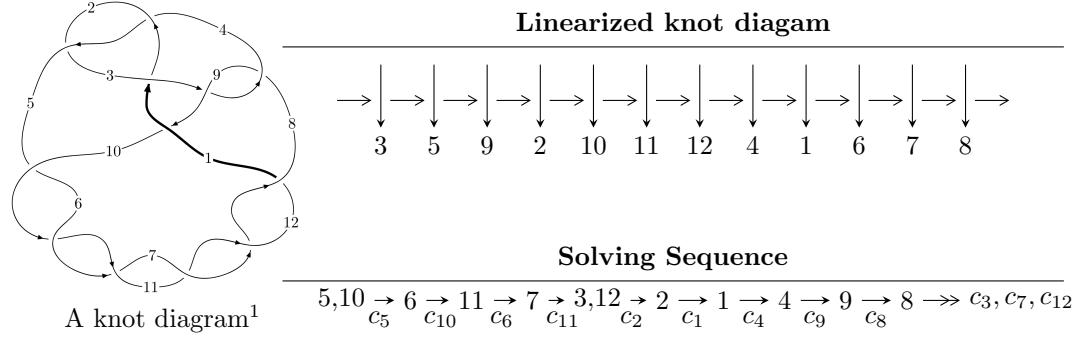


$12a_{0143}$  ( $K12a_{0143}$ )



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -u^{44} - u^{43} + \dots + b + 1, -u^{26} + 19u^{24} + \dots + a - 1, u^{45} + 2u^{44} + \dots + u - 1 \rangle$$

$$I_2^u = \langle b + 1, a + 1, u^3 - u^2 - 2u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 48 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle -u^{44} - u^{43} + \cdots + b + 1, -u^{26} + 19u^{24} + \cdots + a - 1, u^{45} + 2u^{44} + \cdots + u - 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^{26} - 19u^{24} + \cdots + 2u + 1 \\ u^{44} + u^{43} + \cdots + u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^3 - 2u \\ u^5 - 3u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^{44} + u^{43} + \cdots - 19u^3 + 3u \\ u^{44} + u^{43} + \cdots + u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^5 - 4u^3 + 3u \\ u^7 - 5u^5 + 6u^3 - u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 2u^{44} + 2u^{43} + \cdots + 4u^2 + 3u \\ u^{44} + u^{43} + \cdots + 2u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^{11} - 8u^9 + 22u^7 - 24u^5 + 9u^3 \\ u^{13} - 9u^{11} + 29u^9 - 40u^7 + 22u^5 - 3u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^4 - 3u^2 + 1 \\ u^6 - 4u^4 + 3u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $5u^{44} + 4u^{43} + \cdots - 4u - 19$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{45} + 22u^{44} + \cdots + 74u + 1$
$c_2, c_4$	$u^{45} - 4u^{44} + \cdots + 6u + 1$
$c_3, c_8$	$u^{45} - u^{44} + \cdots + 12u + 8$
$c_5, c_6, c_7$ $c_{10}, c_{11}, c_{12}$	$u^{45} - 2u^{44} + \cdots + u + 1$
$c_9$	$u^{45} + 8u^{44} + \cdots + 409u + 55$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{45} + 6y^{44} + \cdots + 4358y - 1$
$c_2, c_4$	$y^{45} - 22y^{44} + \cdots + 74y - 1$
$c_3, c_8$	$y^{45} + 21y^{44} + \cdots + 16y - 64$
$c_5, c_6, c_7$ $c_{10}, c_{11}, c_{12}$	$y^{45} - 64y^{44} + \cdots + 13y - 1$
$c_9$	$y^{45} - 4y^{44} + \cdots - 43479y - 3025$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.962969 + 0.169603I$		
$a = 0.440533 - 0.958645I$	$-0.28984 - 2.31607I$	$-13.48731 + 4.06907I$
$b = 0.692370 + 0.677447I$		
$u = 0.962969 - 0.169603I$		
$a = 0.440533 + 0.958645I$	$-0.28984 + 2.31607I$	$-13.48731 - 4.06907I$
$b = 0.692370 - 0.677447I$		
$u = -1.148590 + 0.071392I$		
$a = 0.801348 + 0.494679I$	$-5.22276 + 0.37204I$	0
$b = -0.427212 - 0.486489I$		
$u = -1.148590 - 0.071392I$		
$a = 0.801348 - 0.494679I$	$-5.22276 - 0.37204I$	0
$b = -0.427212 + 0.486489I$		
$u = 1.176560 + 0.211087I$		
$a = -0.653062 + 0.188078I$	$-2.36170 - 5.17327I$	0
$b = 0.348834 - 0.855887I$		
$u = 1.176560 - 0.211087I$		
$a = -0.653062 - 0.188078I$	$-2.36170 + 5.17327I$	0
$b = 0.348834 + 0.855887I$		
$u = 0.763709 + 0.251528I$		
$a = -0.0103561 - 0.1259090I$	$-1.03136 + 2.41021I$	$-15.6897 - 1.6774I$
$b = 0.955005 - 0.546675I$		
$u = 0.763709 - 0.251528I$		
$a = -0.0103561 + 0.1259090I$	$-1.03136 - 2.41021I$	$-15.6897 + 1.6774I$
$b = 0.955005 + 0.546675I$		
$u = 1.191250 + 0.124036I$		
$a = -1.094580 + 0.310585I$	$-7.65311 - 1.99196I$	0
$b = -1.252440 + 0.198803I$		
$u = 1.191250 - 0.124036I$		
$a = -1.094580 - 0.310585I$	$-7.65311 + 1.99196I$	0
$b = -1.252440 - 0.198803I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.191140 + 0.163730I$		
$a = -0.78548 - 1.96254I$	$-6.91071 + 4.51785I$	0
$b = -1.029290 + 0.504098I$		
$u = -1.191140 - 0.163730I$		
$a = -0.78548 + 1.96254I$	$-6.91071 - 4.51785I$	0
$b = -1.029290 - 0.504098I$		
$u = 1.219810 + 0.229016I$		
$a = 1.09073 - 1.61980I$	$-4.75327 - 10.58690I$	0
$b = 1.150280 + 0.609142I$		
$u = 1.219810 - 0.229016I$		
$a = 1.09073 + 1.61980I$	$-4.75327 + 10.58690I$	0
$b = 1.150280 - 0.609142I$		
$u = -1.316520 + 0.069582I$		
$a = 0.845369 + 0.138843I$	$-7.86567 - 1.43041I$	0
$b = 0.949980 + 0.382113I$		
$u = -1.316520 - 0.069582I$		
$a = 0.845369 - 0.138843I$	$-7.86567 + 1.43041I$	0
$b = 0.949980 - 0.382113I$		
$u = -0.503453 + 0.459470I$		
$a = 0.37795 + 2.46430I$	$0.78058 + 8.20264I$	$-13.8836 - 9.3349I$
$b = 1.101250 - 0.610224I$		
$u = -0.503453 - 0.459470I$		
$a = 0.37795 - 2.46430I$	$0.78058 - 8.20264I$	$-13.8836 + 9.3349I$
$b = 1.101250 + 0.610224I$		
$u = -0.432497 + 0.443637I$		
$a = -1.29853 - 0.73079I$	$2.77707 + 2.93987I$	$-10.12479 - 5.18879I$
$b = 0.428503 + 0.789342I$		
$u = -0.432497 - 0.443637I$		
$a = -1.29853 + 0.73079I$	$2.77707 - 2.93987I$	$-10.12479 + 5.18879I$
$b = 0.428503 - 0.789342I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.442889 + 0.349610I$		
$a = 0.03028 + 3.06490I$	$-1.64546 - 2.76575I$	$-16.0685 + 7.3874I$
$b = -0.954541 - 0.430846I$		
$u = 0.442889 - 0.349610I$		
$a = 0.03028 - 3.06490I$	$-1.64546 + 2.76575I$	$-16.0685 - 7.3874I$
$b = -0.954541 + 0.430846I$		
$u = -0.147862 + 0.512639I$		
$a = -1.34459 - 1.27617I$	$1.83508 - 4.99628I$	$-10.28872 + 3.31837I$
$b = 1.043660 + 0.604880I$		
$u = -0.147862 - 0.512639I$		
$a = -1.34459 + 1.27617I$	$1.83508 + 4.99628I$	$-10.28872 - 3.31837I$
$b = 1.043660 - 0.604880I$		
$u = -0.229805 + 0.471597I$		
$a = -0.25152 + 1.93643I$	$3.37526 + 0.10760I$	$-7.61315 - 2.95177I$
$b = 0.527284 - 0.732325I$		
$u = -0.229805 - 0.471597I$		
$a = -0.25152 - 1.93643I$	$3.37526 - 0.10760I$	$-7.61315 + 2.95177I$
$b = 0.527284 + 0.732325I$		
$u = -0.426938 + 0.242547I$		
$a = -0.516634 - 0.830332I$	$-2.39909 + 0.70824I$	$-15.1495 - 9.1471I$
$b = -1.145690 - 0.133170I$		
$u = -0.426938 - 0.242547I$		
$a = -0.516634 + 0.830332I$	$-2.39909 - 0.70824I$	$-15.1495 + 9.1471I$
$b = -1.145690 + 0.133170I$		
$u = 0.181432 + 0.311155I$		
$a = 2.35597 - 1.25070I$	$-0.905303 + 0.433735I$	$-12.18552 + 1.89292I$
$b = -0.825100 + 0.293052I$		
$u = 0.181432 - 0.311155I$		
$a = 2.35597 + 1.25070I$	$-0.905303 - 0.433735I$	$-12.18552 - 1.89292I$
$b = -0.825100 - 0.293052I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.346739$		
$a = 1.01677$	-0.548092	-17.9540
$b = -0.122928$		
$u = -1.73488 + 0.01556I$		
$a = 0.165858 + 0.798942I$	-10.02540 + 2.83788I	0
$b = 0.805113 - 0.767877I$		
$u = -1.73488 - 0.01556I$		
$a = 0.165858 - 0.798942I$	-10.02540 - 2.83788I	0
$b = 0.805113 + 0.767877I$		
$u = 1.77511 + 0.02023I$		
$a = 0.581848 - 0.527304I$	-15.9251 - 0.7872I	0
$b = -0.425874 + 0.628346I$		
$u = 1.77511 - 0.02023I$		
$a = 0.581848 + 0.527304I$	-15.9251 + 0.7872I	0
$b = -0.425874 - 0.628346I$		
$u = -1.77793 + 0.05224I$		
$a = -0.414828 - 0.211707I$	-13.1145 + 6.3153I	0
$b = 0.314583 + 0.909747I$		
$u = -1.77793 - 0.05224I$		
$a = -0.414828 + 0.211707I$	-13.1145 - 6.3153I	0
$b = 0.314583 - 0.909747I$		
$u = 1.78253 + 0.04085I$		
$a = -0.78346 + 1.57093I$	-17.7770 - 5.4165I	0
$b = -1.063730 - 0.545729I$		
$u = 1.78253 - 0.04085I$		
$a = -0.78346 - 1.57093I$	-17.7770 + 5.4165I	0
$b = -1.063730 + 0.545729I$		
$u = -1.78292 + 0.03166I$		
$a = -1.096720 - 0.115819I$	-18.5397 + 2.6826I	0
$b = -1.302410 - 0.221345I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.78292 - 0.03166I$		
$a = -1.096720 + 0.115819I$	$-18.5397 - 2.6826I$	0
$b = -1.302410 + 0.221345I$		
$u = -1.78906 + 0.05870I$		
$a = 1.08096 + 1.26242I$	$-15.7314 + 11.8740I$	0
$b = 1.181650 - 0.611600I$		
$u = -1.78906 - 0.05870I$		
$a = 1.08096 - 1.26242I$	$-15.7314 - 11.8740I$	0
$b = 1.181650 + 0.611600I$		
$u = 1.81198 + 0.01590I$		
$a = 0.970531 - 0.091202I$	$-19.4518 + 1.0384I$	0
$b = 0.989237 - 0.314096I$		
$u = 1.81198 - 0.01590I$		
$a = 0.970531 + 0.091202I$	$-19.4518 - 1.0384I$	0
$b = 0.989237 + 0.314096I$		

$$\text{II. } I_2^u = \langle b+1, a+1, u^3 - u^2 - 2u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u \\ -u^2 - u + 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u^2 + 1 \\ -u^2 - u + 1 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -1 \\ -1 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} u^2 - 1 \\ u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -2 \\ -1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -1 \\ 0 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -1 \\ -1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_8 &= \begin{pmatrix} u \\ u \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-u^2 + u - 17$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^3$
$c_3, c_8$	$u^3$
$c_4$	$(u + 1)^3$
$c_5, c_6, c_7$ $c_9$	$u^3 - u^2 - 2u + 1$
$c_{10}, c_{11}, c_{12}$	$u^3 + u^2 - 2u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^3$
$c_3, c_8$	$y^3$
$c_5, c_6, c_7$ $c_9, c_{10}, c_{11}$ $c_{12}$	$y^3 - 5y^2 + 6y - 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.24698$		
$a = -1.00000$	-7.98968	-19.8020
$b = -1.00000$		
$u = 0.445042$		
$a = -1.00000$	-2.34991	-16.7530
$b = -1.00000$		
$u = 1.80194$		
$a = -1.00000$	-19.2692	-18.4450
$b = -1.00000$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^3)(u^{45} + 22u^{44} + \cdots + 74u + 1)$
$c_2$	$((u - 1)^3)(u^{45} - 4u^{44} + \cdots + 6u + 1)$
$c_3, c_8$	$u^3(u^{45} - u^{44} + \cdots + 12u + 8)$
$c_4$	$((u + 1)^3)(u^{45} - 4u^{44} + \cdots + 6u + 1)$
$c_5, c_6, c_7$	$(u^3 - u^2 - 2u + 1)(u^{45} - 2u^{44} + \cdots + u + 1)$
$c_9$	$(u^3 - u^2 - 2u + 1)(u^{45} + 8u^{44} + \cdots + 409u + 55)$
$c_{10}, c_{11}, c_{12}$	$(u^3 + u^2 - 2u - 1)(u^{45} - 2u^{44} + \cdots + u + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y - 1)^3)(y^{45} + 6y^{44} + \dots + 4358y - 1)$
$c_2, c_4$	$((y - 1)^3)(y^{45} - 22y^{44} + \dots + 74y - 1)$
$c_3, c_8$	$y^3(y^{45} + 21y^{44} + \dots + 16y - 64)$
$c_5, c_6, c_7$ $c_{10}, c_{11}, c_{12}$	$(y^3 - 5y^2 + 6y - 1)(y^{45} - 64y^{44} + \dots + 13y - 1)$
$c_9$	$(y^3 - 5y^2 + 6y - 1)(y^{45} - 4y^{44} + \dots - 43479y - 3025)$