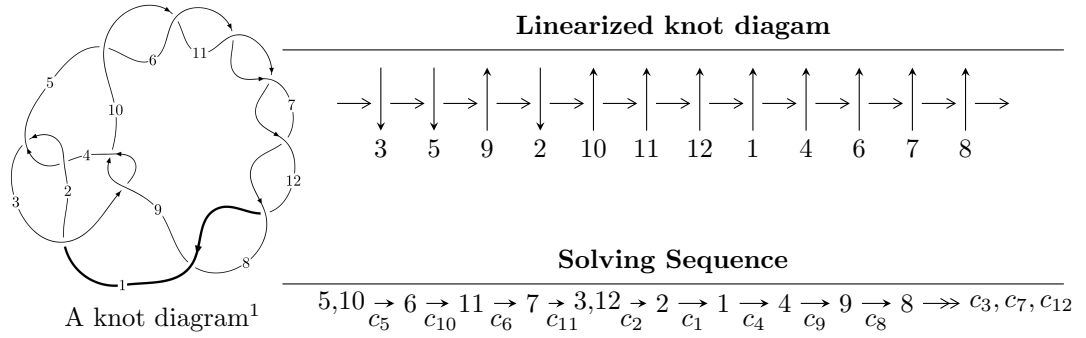


12a<sub>0146</sub> (K12a<sub>0146</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle u^{29} - u^{28} + \dots + b + 1, -u^{29} + u^{28} + \dots + a + 6u, u^{30} - 2u^{29} + \dots - 36u^3 - 1 \rangle$$

$$I_2^u = \langle b + 1, a, u^3 + u^2 - 2u - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 33 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle u^{29} - u^{28} + \dots + b + 1, -u^{29} + u^{28} + \dots + a + 6u, u^{30} - 2u^{29} + \dots - 36u^3 - 1 \rangle \quad \text{I.}$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^{29} - u^{28} + \dots - 8u^2 - 6u \\ -u^{29} + u^{28} + \dots - 2u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^3 + 2u \\ u^5 - 3u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^{14} + 11u^{12} + \dots - 8u - 1 \\ -u^{29} + u^{28} + \dots - 2u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^5 + 4u^3 - 3u \\ u^7 - 5u^5 + 6u^3 - u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^{29} + u^{28} + \dots - 6u - 1 \\ -u^{29} + u^{28} + \dots - u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^6 + 5u^4 - 6u^2 + 1 \\ u^8 - 6u^6 + 10u^4 - 4u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^4 - 3u^2 + 1 \\ -u^6 + 4u^4 - 3u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\begin{aligned} \text{(iii) Cusp Shapes} &= -3u^{29} + 4u^{28} + 62u^{27} - 82u^{26} - 561u^{25} + 739u^{24} + 2918u^{23} - \\ &3849u^{22} - 9630u^{21} + 12801u^{20} + 21006u^{19} - 28320u^{18} - 30675u^{17} + 42061u^{16} + \\ &30044u^{15} - 41342u^{14} - 20264u^{13} + 26026u^{12} + 10788u^{11} - 10222u^{10} - 5598u^9 + \\ &2750u^8 + 2538u^7 - 619u^6 - 778u^5 + 21u^4 + 168u^3 + 52u^2 - 25u + 7 \end{aligned}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{30} + 12u^{29} + \dots + 97u + 1$
$c_2, c_4$	$u^{30} - 4u^{29} + \dots + 13u - 1$
$c_3, c_9$	$u^{30} - u^{29} + \dots - 28u + 8$
$c_5, c_6, c_7$ $c_8, c_{10}, c_{11}$ $c_{12}$	$u^{30} + 2u^{29} + \dots + 36u^3 - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{30} + 16y^{29} + \dots - 7313y + 1$
$c_2, c_4$	$y^{30} - 12y^{29} + \dots - 97y + 1$
$c_3, c_9$	$y^{30} - 21y^{29} + \dots - 1104y + 64$
$c_5, c_6, c_7$ $c_8, c_{10}, c_{11}$ $c_{12}$	$y^{30} - 46y^{29} + \dots + 40y^2 + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.900406 + 0.238240I$ $a = -0.659304 - 0.413832I$ $b = 0.605232 + 0.768254I$	$5.67065 + 1.25696I$	$15.5737 - 1.7388I$
$u = 0.900406 - 0.238240I$ $a = -0.659304 + 0.413832I$ $b = 0.605232 - 0.768254I$	$5.67065 - 1.25696I$	$15.5737 + 1.7388I$
$u = 0.814325 + 0.340165I$ $a = 0.69999 + 1.77618I$ $b = 1.030380 - 0.688639I$	$4.42916 + 6.78890I$	$12.9792 - 7.4265I$
$u = 0.814325 - 0.340165I$ $a = 0.69999 - 1.77618I$ $b = 1.030380 + 0.688639I$	$4.42916 - 6.78890I$	$12.9792 + 7.4265I$
$u = 1.18737$ $a = 0.321529$ $b = 0.549343$	$5.59474$	$18.0870$
$u = -0.736617 + 0.129687I$ $a = 0.52614 + 2.05833I$ $b = -0.816371 - 0.432342I$	$0.97252 - 1.81198I$	$11.73549 + 4.66948I$
$u = -0.736617 - 0.129687I$ $a = 0.52614 - 2.05833I$ $b = -0.816371 + 0.432342I$	$0.97252 + 1.81198I$	$11.73549 - 4.66948I$
$u = 0.654424$ $a = -0.551259$ $b = -1.18483$	$-0.312115$	$16.4990$
$u = -1.37237$ $a = 0.0265788$ $b = -1.33306$	$6.56541$	$13.9410$
$u = 1.393080 + 0.049142I$ $a = 0.62086 - 1.75059I$ $b = -0.838747 + 0.622252I$	$8.15659 + 2.43505I$	$13.02410 - 2.90794I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.393080 - 0.049142I$ $a = 0.62086 + 1.75059I$ $b = -0.838747 - 0.622252I$	$8.15659 - 2.43505I$	$13.02410 + 2.90794I$
$u = -1.41889 + 0.15784I$ $a = 0.01368 - 1.73786I$ $b = 1.114240 + 0.728134I$	$11.8944 - 8.6308I$	$14.0718 + 5.7224I$
$u = -1.41889 - 0.15784I$ $a = 0.01368 + 1.73786I$ $b = 1.114240 - 0.728134I$	$11.8944 + 8.6308I$	$14.0718 - 5.7224I$
$u = -0.348859 + 0.441668I$ $a = 0.229073 - 0.720707I$ $b = 0.785869 - 0.632862I$	$1.73384 + 0.97008I$	$10.55280 + 0.95390I$
$u = -0.348859 - 0.441668I$ $a = 0.229073 + 0.720707I$ $b = 0.785869 + 0.632862I$	$1.73384 - 0.97008I$	$10.55280 - 0.95390I$
$u = -1.45263 + 0.10165I$ $a = -0.661962 + 1.037750I$ $b = 0.546899 - 0.940788I$	$13.61630 - 2.52281I$	$16.2553 + 0.I$
$u = -1.45263 - 0.10165I$ $a = -0.661962 - 1.037750I$ $b = 0.546899 + 0.940788I$	$13.61630 + 2.52281I$	$16.2553 + 0.I$
$u = -0.206383 + 0.495565I$ $a = 1.71927 - 0.54217I$ $b = 0.926515 + 0.641729I$	$1.28497 - 4.02644I$	$8.41488 + 6.42284I$
$u = -0.206383 - 0.495565I$ $a = 1.71927 + 0.54217I$ $b = 0.926515 - 0.641729I$	$1.28497 + 4.02644I$	$8.41488 - 6.42284I$
$u = -0.362782$ $a = 0.804898$ $b = 0.108164$	$0.561369$	$17.6530$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.118463 + 0.232287I$ $a = -1.31174 - 2.44567I$ $b = -0.912796 + 0.166074I$	$-1.60535 + 0.58110I$	$-1.83750 - 2.62782I$
$u = 0.118463 - 0.232287I$ $a = -1.31174 + 2.44567I$ $b = -0.912796 - 0.166074I$	$-1.60535 - 0.58110I$	$-1.83750 + 2.62782I$
$u = -1.79109$ $a = 0.214755$ $b = 0.718711$	16.5830	0
$u = 1.83755$ $a = 0.242340$ $b = -1.40717$	18.6422	0
$u = -1.84184 + 0.01166I$ $a = 0.64542 + 1.69046I$ $b = -0.867094 - 0.716132I$	$-19.1326 - 2.7360I$	0
$u = -1.84184 - 0.01166I$ $a = 0.64542 - 1.69046I$ $b = -0.867094 + 0.716132I$	$-19.1326 + 2.7360I$	0
$u = 1.84728 + 0.04017I$ $a = -0.22651 + 1.65159I$ $b = 1.166510 - 0.750722I$	$-15.2987 + 9.6434I$	0
$u = 1.84728 - 0.04017I$ $a = -0.22651 - 1.65159I$ $b = 1.166510 + 0.750722I$	$-15.2987 - 9.6434I$	0
$u = 1.85511 + 0.02516I$ $a = -0.624328 - 1.260080I$ $b = 0.533783 + 1.034720I$	$-13.33250 + 3.18487I$	0
$u = 1.85511 - 0.02516I$ $a = -0.624328 + 1.260080I$ $b = 0.533783 - 1.034720I$	$-13.33250 - 3.18487I$	0

$$\text{II. } I_2^u = \langle b + 1, a, u^3 + u^2 - 2u - 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u^2 - u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 + 1 \\ u^2 - u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^2 - 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $u^2 + u + 5$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^3$
$c_3, c_9$	$u^3$
$c_4$	$(u + 1)^3$
$c_5, c_6, c_7$ $c_8$	$u^3 + u^2 - 2u - 1$
$c_{10}, c_{11}, c_{12}$	$u^3 - u^2 - 2u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^3$
$c_3, c_9$	$y^3$
$c_5, c_6, c_7$ $c_8, c_{10}, c_{11}$ $c_{12}$	$y^3 - 5y^2 + 6y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.24698$ $a = 0$ $b = -1.00000$	4.69981	7.80190
$u = -0.445042$ $a = 0$ $b = -1.00000$	-0.939962	4.75300
$u = -1.80194$ $a = 0$ $b = -1.00000$	15.9794	6.44500

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^3)(u^{30} + 12u^{29} + \dots + 97u + 1)$
$c_2$	$((u - 1)^3)(u^{30} - 4u^{29} + \dots + 13u - 1)$
$c_3, c_9$	$u^3(u^{30} - u^{29} + \dots - 28u + 8)$
$c_4$	$((u + 1)^3)(u^{30} - 4u^{29} + \dots + 13u - 1)$
$c_5, c_6, c_7$ $c_8$	$(u^3 + u^2 - 2u - 1)(u^{30} + 2u^{29} + \dots + 36u^3 - 1)$
$c_{10}, c_{11}, c_{12}$	$(u^3 - u^2 - 2u + 1)(u^{30} + 2u^{29} + \dots + 36u^3 - 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y - 1)^3)(y^{30} + 16y^{29} + \dots - 7313y + 1)$
$c_2, c_4$	$((y - 1)^3)(y^{30} - 12y^{29} + \dots - 97y + 1)$
$c_3, c_9$	$y^3(y^{30} - 21y^{29} + \dots - 1104y + 64)$
$c_5, c_6, c_7$ $c_8, c_{10}, c_{11}$ $c_{12}$	$(y^3 - 5y^2 + 6y - 1)(y^{30} - 46y^{29} + \dots + 40y^2 + 1)$