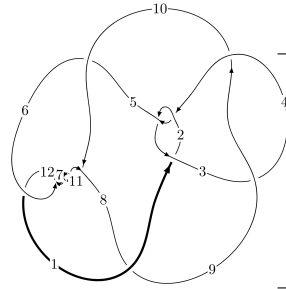
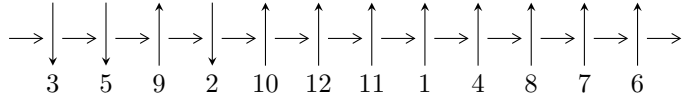


12a₀₁₅₃ (K12a₀₁₅₃)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$3,9 \xrightarrow{c_3} 4 \xrightarrow{c_9} 5,10 \xrightarrow{c_5} 6 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_8} 8 \xrightarrow{c_{10}} 11 \xrightarrow{c_7} 7 \xrightarrow{c_{12}} 12 \rightsquigarrow c_4, c_6, c_{11}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 5.60722 \times 10^{81} u^{57} + 1.67247 \times 10^{81} u^{56} + \dots + 2.33772 \times 10^{82} b + 1.81103 \times 10^{83}, \\ 7.27818 \times 10^{82} u^{57} + 4.91560 \times 10^{82} u^{56} + \dots + 1.87018 \times 10^{83} a + 1.91879 \times 10^{84}, u^{58} + u^{57} + \dots + 64u + 3 \rangle$$

$$I_1^v = \langle a, b - 1, v^5 - v^4 + v^2 + v - 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 63 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 5.61 \times 10^{81} u^{57} + 1.67 \times 10^{81} u^{56} + \dots + 2.34 \times 10^{82} b + 1.81 \times 10^{83}, 7.28 \times 10^{82} u^{57} + 4.92 \times 10^{82} u^{56} + \dots + 1.87 \times 10^{83} a + 1.92 \times 10^{84}, u^{58} + u^{57} + \dots + 64u + 32 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.389171u^{57} - 0.262841u^{56} + \dots + 4.54781u - 10.2600 \\ -0.239859u^{57} - 0.0715429u^{56} + \dots - 7.02146u - 7.74698 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.522817u^{57} - 0.268126u^{56} + \dots - 1.68093u - 13.8759 \\ -0.207902u^{57} - 0.0373370u^{56} + \dots - 9.31175u - 7.25535 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.389171u^{57} - 0.262841u^{56} + \dots + 4.54781u - 10.2600 \\ 0.420518u^{57} + 0.181191u^{56} + \dots + 2.65309u + 11.7895 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.0313472u^{57} - 0.0816505u^{56} + \dots + 7.20090u + 1.52957 \\ 0.420518u^{57} + 0.181191u^{56} + \dots + 2.65309u + 11.7895 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.713059u^{57} + 0.0359583u^{56} + \dots - 41.8715u - 42.2736 \\ -0.0618638u^{57} + 0.0517051u^{56} + \dots - 0.420514u + 0.205394 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.427906u^{57} + 0.0462409u^{56} + \dots + 18.0771u + 11.5849 \\ -0.749808u^{57} + 0.0101401u^{56} + \dots - 32.6805u - 32.2330 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.393422u^{57} + 0.397378u^{56} + \dots - 1.00737u + 23.9064 \\ -0.558340u^{57} - 0.192853u^{56} + \dots - 13.8407u - 26.9810 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.460418u^{57} + 0.147034u^{56} + \dots + 20.1920u + 18.9774 \\ -0.416036u^{57} - 0.145859u^{56} + \dots - 7.89835u - 13.2725 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-2.02102u^{57} - 0.114366u^{56} + \dots - 107.539u - 65.1509$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{58} + 26u^{57} + \dots + 36u + 1$
c_2, c_4	$u^{58} - 6u^{57} + \dots + 12u - 1$
c_3, c_9	$u^{58} - u^{57} + \dots - 64u + 32$
c_5, c_8	$u^{58} + 2u^{57} + \dots - 1314u - 445$
c_6, c_7, c_{10} c_{11}, c_{12}	$u^{58} + 2u^{57} + \dots - 2u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{58} + 18y^{57} + \dots - 1608y + 1$
c_2, c_4	$y^{58} - 26y^{57} + \dots - 36y + 1$
c_3, c_9	$y^{58} - 33y^{57} + \dots - 19968y + 1024$
c_5, c_8	$y^{58} - 38y^{57} + \dots + 2799054y + 198025$
c_6, c_7, c_{10} c_{11}, c_{12}	$y^{58} + 74y^{57} + \dots + 6y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.988918 + 0.213289I$		
$a = 0.430565 + 0.018643I$	$-11.06150 - 4.52126I$	$2.64115 + 3.57478I$
$b = 1.318190 - 0.100375I$		
$u = -0.988918 - 0.213289I$		
$a = 0.430565 - 0.018643I$	$-11.06150 + 4.52126I$	$2.64115 - 3.57478I$
$b = 1.318190 + 0.100375I$		
$u = -1.012520 + 0.149144I$		
$a = 0.62352 + 1.58705I$	$1.31063 - 0.82722I$	$9.15613 - 0.70745I$
$b = -0.785549 - 0.545845I$		
$u = -1.012520 - 0.149144I$		
$a = 0.62352 - 1.58705I$	$1.31063 + 0.82722I$	$9.15613 + 0.70745I$
$b = -0.785549 + 0.545845I$		
$u = 0.670998 + 0.708770I$		
$a = 0.455472 - 0.072472I$	$-14.4352 - 1.2271I$	$-2.32982 + 0.23811I$
$b = 1.141310 + 0.340713I$		
$u = 0.670998 - 0.708770I$		
$a = 0.455472 + 0.072472I$	$-14.4352 + 1.2271I$	$-2.32982 - 0.23811I$
$b = 1.141310 - 0.340713I$		
$u = 0.120330 + 1.017630I$		
$a = 0.516133 - 0.162101I$	$-0.454989 + 0.856173I$	$4.39334 - 1.34405I$
$b = 0.763532 + 0.553870I$		
$u = 0.120330 - 1.017630I$		
$a = 0.516133 + 0.162101I$	$-0.454989 - 0.856173I$	$4.39334 + 1.34405I$
$b = 0.763532 - 0.553870I$		
$u = -0.023513 + 1.056290I$		
$a = 0.524037 + 0.186326I$	$-9.08024 - 2.35274I$	$2.89470 - 0.08369I$
$b = 0.694092 - 0.602349I$		
$u = -0.023513 - 1.056290I$		
$a = 0.524037 - 0.186326I$	$-9.08024 + 2.35274I$	$2.89470 + 0.08369I$
$b = 0.694092 + 0.602349I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.926509 + 0.140364I$ $a = 0.436398 - 0.012440I$ $b = 1.289630 + 0.065266I$	$-2.19660 + 2.97198I$	$4.77337 - 5.16018I$
$u = 0.926509 - 0.140364I$ $a = 0.436398 + 0.012440I$ $b = 1.289630 - 0.065266I$	$-2.19660 - 2.97198I$	$4.77337 + 5.16018I$
$u = -0.229073 + 1.043540I$ $a = 0.495133 + 0.149970I$ $b = 0.849943 - 0.560327I$	$1.83802 + 2.24390I$	$9.07567 - 3.44705I$
$u = -0.229073 - 1.043540I$ $a = 0.495133 - 0.149970I$ $b = 0.849943 + 0.560327I$	$1.83802 - 2.24390I$	$9.07567 + 3.44705I$
$u = -0.898579$ $a = 0.439075$ $b = 1.27751$	0.376807	11.1020
$u = 0.970754 + 0.521236I$ $a = -0.18922 - 2.00022I$ $b = -1.046870 + 0.495511I$	$-13.4454 + 5.9801I$	$0. - 6.24129I$
$u = 0.970754 - 0.521236I$ $a = -0.18922 + 2.00022I$ $b = -1.046870 - 0.495511I$	$-13.4454 - 5.9801I$	$0. + 6.24129I$
$u = 0.312376 + 1.070610I$ $a = 0.479995 - 0.143589I$ $b = 0.912231 + 0.572038I$	$-0.92817 - 5.38733I$	$3.26193 + 6.82724I$
$u = 0.312376 - 1.070610I$ $a = 0.479995 + 0.143589I$ $b = 0.912231 - 0.572038I$	$-0.92817 + 5.38733I$	$3.26193 - 6.82724I$
$u = 1.079810 + 0.293215I$ $a = 0.28949 - 1.67352I$ $b = -0.899638 + 0.580183I$	$0.92519 + 3.70734I$	$7.01990 - 7.67884I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.079810 - 0.293215I$ $a = 0.28949 + 1.67352I$ $b = -0.899638 - 0.580183I$	$0.92519 - 3.70734I$	$7.01990 + 7.67884I$
$u = -1.025060 + 0.450289I$ $a = -0.00985 + 1.87728I$ $b = -1.002790 - 0.532670I$	$-3.60799 - 5.37901I$	$0. + 6.85674I$
$u = -1.025060 - 0.450289I$ $a = -0.00985 - 1.87728I$ $b = -1.002790 + 0.532670I$	$-3.60799 + 5.37901I$	$0. - 6.85674I$
$u = -0.616932 + 0.596574I$ $a = 0.766075 - 0.434828I$ $b = -0.012721 + 0.560385I$	$-11.10310 - 2.21498I$	$3.03458 + 3.08140I$
$u = -0.616932 - 0.596574I$ $a = 0.766075 + 0.434828I$ $b = -0.012721 - 0.560385I$	$-11.10310 + 2.21498I$	$3.03458 - 3.08140I$
$u = -0.561331 + 0.640996I$ $a = 0.470504 + 0.066767I$ $b = 1.083430 - 0.295649I$	$-5.09839 + 1.07706I$	$-3.30982 - 0.29304I$
$u = -0.561331 - 0.640996I$ $a = 0.470504 - 0.066767I$ $b = 1.083430 + 0.295649I$	$-5.09839 - 1.07706I$	$-3.30982 + 0.29304I$
$u = -0.365820 + 1.106240I$ $a = 0.469197 + 0.142290I$ $b = 0.951796 - 0.591908I$	$-9.86525 + 7.09450I$	$0. - 5.09520I$
$u = -0.365820 - 1.106240I$ $a = 0.469197 - 0.142290I$ $b = 0.951796 + 0.591908I$	$-9.86525 - 7.09450I$	$0. + 5.09520I$
$u = 0.821553 + 0.120863I$ $a = 1.20206 - 1.80781I$ $b = -0.744954 + 0.383569I$	$-2.46309 - 1.43775I$	$4.26235 + 0.30434I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.821553 - 0.120863I$ $a = 1.20206 + 1.80781I$ $b = -0.744954 - 0.383569I$	$-2.46309 + 1.43775I$	$4.26235 - 0.30434I$
$u = -0.727877 + 0.161089I$ $a = 1.58949 + 2.25794I$ $b = -0.791536 - 0.296132I$	$-11.94240 + 2.62554I$	$4.16578 + 2.14464I$
$u = -0.727877 - 0.161089I$ $a = 1.58949 - 2.25794I$ $b = -0.791536 + 0.296132I$	$-11.94240 - 2.62554I$	$4.16578 - 2.14464I$
$u = 0.518918 + 0.402182I$ $a = 0.931285 + 0.375334I$ $b = -0.076260 - 0.372294I$	$-2.01038 + 1.63657I$	$4.07721 - 4.69025I$
$u = 0.518918 - 0.402182I$ $a = 0.931285 - 0.375334I$ $b = -0.076260 + 0.372294I$	$-2.01038 - 1.63657I$	$4.07721 + 4.69025I$
$u = -1.336420 + 0.272826I$ $a = 0.447495 - 0.910443I$ $b = -0.565183 + 0.884648I$	$4.83453 + 1.13962I$	0
$u = -1.336420 - 0.272826I$ $a = 0.447495 + 0.910443I$ $b = -0.565183 - 0.884648I$	$4.83453 - 1.13962I$	0
$u = 1.329630 + 0.349002I$ $a = 0.459401 + 0.858056I$ $b = -0.515046 - 0.905782I$	$7.02632 + 2.30073I$	0
$u = 1.329630 - 0.349002I$ $a = 0.459401 - 0.858056I$ $b = -0.515046 + 0.905782I$	$7.02632 - 2.30073I$	0
$u = -1.316660 + 0.413705I$ $a = 0.469503 - 0.816218I$ $b = -0.470472 + 0.920569I$	$4.18115 - 5.70575I$	0

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.316660 - 0.413705I$ $a = 0.469503 + 0.816218I$ $b = -0.470472 - 0.920569I$	$4.18115 + 5.70575I$	0
$u = 1.377690 + 0.196979I$ $a = 0.403381 + 0.956988I$ $b = -0.625994 - 0.887297I$	$-3.49813 - 2.89761I$	0
$u = 1.377690 - 0.196979I$ $a = 0.403381 - 0.956988I$ $b = -0.625994 + 0.887297I$	$-3.49813 + 2.89761I$	0
$u = 1.317010 + 0.468560I$ $a = 0.468183 + 0.782796I$ $b = -0.437256 - 0.940900I$	$-4.76531 + 7.61575I$	0
$u = 1.317010 - 0.468560I$ $a = 0.468183 - 0.782796I$ $b = -0.437256 + 0.940900I$	$-4.76531 - 7.61575I$	0
$u = 1.296970 + 0.533749I$ $a = -0.15451 - 1.41849I$ $b = -1.075890 + 0.696711I$	$3.27838 + 4.69767I$	0
$u = 1.296970 - 0.533749I$ $a = -0.15451 + 1.41849I$ $b = -1.075890 - 0.696711I$	$3.27838 - 4.69767I$	0
$u = -1.336730 + 0.459923I$ $a = -0.067104 + 1.368720I$ $b = -1.035730 - 0.728859I$	$-4.74657 - 3.04886I$	0
$u = -1.336730 - 0.459923I$ $a = -0.067104 - 1.368720I$ $b = -1.035730 + 0.728859I$	$-4.74657 + 3.04886I$	0
$u = -1.29402 + 0.59257I$ $a = -0.22697 + 1.41455I$ $b = -1.110590 - 0.689193I$	$5.21330 - 8.16966I$	0

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.29402 - 0.59257I$ $a = -0.22697 - 1.41455I$ $b = -1.110590 + 0.689193I$	$5.21330 + 8.16966I$	0
$u = 1.28224 + 0.63700I$ $a = -0.28338 - 1.41775I$ $b = -1.135570 + 0.678245I$	$2.15742 + 11.57290I$	0
$u = 1.28224 - 0.63700I$ $a = -0.28338 + 1.41775I$ $b = -1.135570 - 0.678245I$	$2.15742 - 11.57290I$	0
$u = -1.27688 + 0.67254I$ $a = -0.32722 + 1.41208I$ $b = -1.155740 - 0.672085I$	$-6.9557 - 13.5111I$	0
$u = -1.27688 - 0.67254I$ $a = -0.32722 - 1.41208I$ $b = -1.155740 + 0.672085I$	$-6.9557 + 13.5111I$	0
$u = 0.233547 + 0.502739I$ $a = 0.516311 - 0.040838I$ $b = 0.924775 + 0.152243I$	$-1.61764 - 0.55942I$	$-2.71688 + 2.11275I$
$u = 0.233547 - 0.502739I$ $a = 0.516311 + 0.040838I$ $b = 0.924775 - 0.152243I$	$-1.61764 + 0.55942I$	$-2.71688 - 2.11275I$
$u = -0.394574$ $a = 1.19015$ $b = -0.159767$	0.637461	15.7740

$$\text{II. } I_1^v = \langle a, b - 1, v^5 - v^4 + v^2 + v - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} v^2 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ v \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -v^3 + v \\ -v^3 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} v^4 - v^3 - v^2 + 1 \\ v^4 - v^2 + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} v^4 \\ v^2 - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $3v^4 - 4v^2 + 3v + 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2	$(u - 1)^5$
c_3, c_9	u^5
c_4	$(u + 1)^5$
c_5, c_8	$u^5 + u^4 - u^2 + u + 1$
c_6, c_7	$u^5 + u^4 + 4u^3 + 3u^2 + 3u + 1$
c_{10}, c_{11}, c_{12}	$u^5 - u^4 + 4u^3 - 3u^2 + 3u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4	$(y - 1)^5$
c_3, c_9	y^5
c_5, c_8	$y^5 - y^4 + 4y^3 - 3y^2 + 3y - 1$
c_6, c_7, c_{10} c_{11}, c_{12}	$y^5 + 7y^4 + 16y^3 + 13y^2 + 3y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^v	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -0.758138 + 0.584034I$ $a = 0$ $b = 1.00000$	$-3.46474 - 2.21397I$	$-1.39794 + 4.05273I$
$v = -0.758138 - 0.584034I$ $a = 0$ $b = 1.00000$	$-3.46474 + 2.21397I$	$-1.39794 - 4.05273I$
$v = 0.935538 + 0.903908I$ $a = 0$ $b = 1.00000$	$-12.60320 + 3.33174I$	$-1.99723 - 3.46299I$
$v = 0.935538 - 0.903908I$ $a = 0$ $b = 1.00000$	$-12.60320 - 3.33174I$	$-1.99723 + 3.46299I$
$v = 0.645200$ $a = 0$ $b = 1.00000$	-0.762751	4.79030

III. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u - 1)^5)(u^{58} + 26u^{57} + \dots + 36u + 1)$
c_2	$((u - 1)^5)(u^{58} - 6u^{57} + \dots + 12u - 1)$
c_3, c_9	$u^5(u^{58} - u^{57} + \dots - 64u + 32)$
c_4	$((u + 1)^5)(u^{58} - 6u^{57} + \dots + 12u - 1)$
c_5, c_8	$(u^5 + u^4 - u^2 + u + 1)(u^{58} + 2u^{57} + \dots - 1314u - 445)$
c_6, c_7	$(u^5 + u^4 + 4u^3 + 3u^2 + 3u + 1)(u^{58} + 2u^{57} + \dots - 2u - 1)$
c_{10}, c_{11}, c_{12}	$(u^5 - u^4 + 4u^3 - 3u^2 + 3u - 1)(u^{58} + 2u^{57} + \dots - 2u - 1)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$((y - 1)^5)(y^{58} + 18y^{57} + \dots - 1608y + 1)$
c_2, c_4	$((y - 1)^5)(y^{58} - 26y^{57} + \dots - 36y + 1)$
c_3, c_9	$y^5(y^{58} - 33y^{57} + \dots - 19968y + 1024)$
c_5, c_8	$(y^5 - y^4 + 4y^3 - 3y^2 + 3y - 1)$ $\cdot (y^{58} - 38y^{57} + \dots + 2799054y + 198025)$
c_6, c_7, c_{10} c_{11}, c_{12}	$(y^5 + 7y^4 + 16y^3 + 13y^2 + 3y - 1)(y^{58} + 74y^{57} + \dots + 6y + 1)$