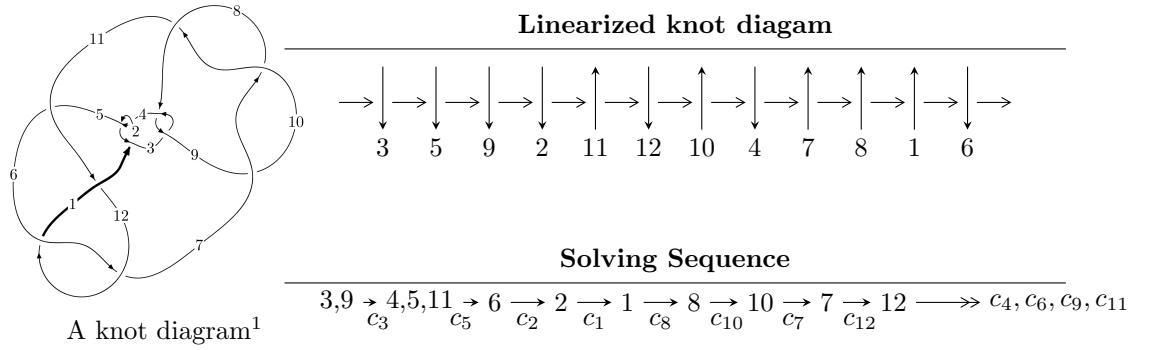


## $12a_{0157}$ ( $K12a_{0157}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle -6.07617 \times 10^{162} u^{76} - 1.59683 \times 10^{163} u^{75} + \dots + 1.45795 \times 10^{166} d + 6.24229 \times 10^{165}, \\
 &\quad - 7.60333 \times 10^{161} u^{76} + 1.20057 \times 10^{161} u^{75} + \dots + 3.64487 \times 10^{165} c + 3.09611 \times 10^{165}, \\
 &\quad - 3.42640 \times 10^{161} u^{76} + 2.87429 \times 10^{161} u^{75} + \dots + 2.56564 \times 10^{164} b + 1.17150 \times 10^{165}, \\
 &\quad 6.98505 \times 10^{162} u^{76} + 6.83866 \times 10^{162} u^{75} + \dots + 1.02626 \times 10^{165} a - 1.03017 \times 10^{166}, \\
 &\quad u^{77} + 2u^{76} + \dots + 2560u^2 + 512 \rangle \\
 I_2^u &= \langle u^3 a^2 - a^2 u^2 - u^3 a + a^2 u + 2u^3 + au + d - 4a + 4, u^3 a^2 - 2u^3 a + a^2 u + 2u^3 + au + c - 2a + 2, \\
 &\quad a^2 u^2 + b + 2a - 2, 2u^3 a^2 - 2a^2 u^2 - 3u^3 a + a^3 + 2a^2 u + 3u^2 a + u^3 - 3au - u^2 + u, u^4 + u^2 + u + 1 \rangle \\
 I_3^u &= \langle u^5 a^2 - 4u^5 a + 2u^3 a^2 + 4u^4 a + 4u^5 - 5u^3 a - 4u^4 + 2a^2 u + 8u^2 a + 6u^3 - 3au - 8u^2 + d + 8a + 4u - 8, \\
 &\quad - 2u^5 a + u^3 a^2 + 2u^4 a + 2u^5 - 4u^3 a - 2u^4 + a^2 u + 4u^2 a + 4u^3 - au - 4u^2 + c + 4a + 2u - 4, \\
 &\quad a^2 u^2 + b + 2a - 2, -4u^5 a^2 + 6u^5 a + \dots - 6a + 2, u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1 \rangle
 \end{aligned}$$

$$I_1^v = \langle c, d - v - 1, b, a - 1, v^2 + v + 1 \rangle$$

$$I_2^v = \langle a, d, c - v, b - 1, v^2 - v + 1 \rangle$$

$$I_3^v = \langle a, d + 1, c + a, b - 1, v - 1 \rangle$$

$$I_4^v = \langle a, a^2 d - c^2 v - 2ca + cv + a - v, dv + 1, c^2 v^2 + 2cav - v^2 c + a^2 - av + v^2, b - 1 \rangle$$

\* 6 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 112 representations.

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 1$

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

$$\text{I. } I_1^u = \langle -6.08 \times 10^{162}u^{76} - 1.60 \times 10^{163}u^{75} + \dots + 1.46 \times 10^{166}d + 6.24 \times 10^{165}, -7.60 \times 10^{161}u^{76} + 1.20 \times 10^{161}u^{75} + \dots + 3.64 \times 10^{165}c + 3.10 \times 10^{165}, -3.43 \times 10^{161}u^{76} + 2.87 \times 10^{161}u^{75} + \dots + 2.57 \times 10^{164}b + 1.17 \times 10^{165}, 6.99 \times 10^{162}u^{76} + 6.84 \times 10^{162}u^{75} + \dots + 1.03 \times 10^{165}a - 1.03 \times 10^{166}, u^{77} + 2u^{76} + \dots + 2560u^2 + 512 \rangle$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.00680634u^{76} - 0.00666370u^{75} + \dots - 13.3533u + 10.0381 \\ 0.00133550u^{76} - 0.00112030u^{75} + \dots + 4.56543u - 4.56612 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.000208604u^{76} - 0.0000329385u^{75} + \dots - 1.00214u - 0.849444 \\ 0.000416762u^{76} + 0.00109526u^{75} + \dots + 0.259754u - 0.428156 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.00584350u^{76} - 0.00606296u^{75} + \dots - 10.5775u + 9.19500 \\ -0.000891648u^{76} - 0.00576153u^{75} + \dots + 4.16493u - 3.32748 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.00680634u^{76} - 0.00666370u^{75} + \dots - 13.3533u + 10.0381 \\ 0.000152722u^{76} + 0.00152555u^{75} + \dots - 1.08059u + 1.00825 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.00665361u^{76} - 0.00513815u^{75} + \dots - 14.4339u + 11.0464 \\ 0.000152722u^{76} + 0.00152555u^{75} + \dots - 1.08059u + 1.00825 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.0000869789u^{76} - 0.000560439u^{75} + \dots - 0.853173u - 0.579783 \\ 0.000218526u^{76} + 0.000662503u^{75} + \dots + 0.560059u - 0.191092 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.000290951u^{76} + 0.00110858u^{75} + \dots + 1.36870u + 0.190813 \\ 0.000499554u^{76} + 0.00107564u^{75} + \dots + 0.366559u - 0.658630 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.00628963u^{76} + 0.0183729u^{75} + \dots + 6.15552u + 8.93643 \\ -0.00429774u^{76} - 0.00774981u^{75} + \dots - 6.38490u - 0.700057 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-0.0221138u^{76} - 0.0478032u^{75} + \dots - 21.6023u + 0.388088$

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<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{77} + 34u^{76} + \cdots + 1568u + 256$
$c_2, c_4$	$u^{77} - 8u^{76} + \cdots - 72u + 16$
$c_3, c_8$	$u^{77} + 2u^{76} + \cdots + 2560u^2 + 512$
$c_5$	$u^{77} + 2u^{76} + \cdots + 351912u + 66564$
$c_6, c_{12}$	$u^{77} - 2u^{76} + \cdots - 27u^2 + 4$
$c_7, c_9, c_{10}$	$u^{77} + 8u^{76} + \cdots - 72u + 16$
$c_{11}$	$u^{77} - 36u^{76} + \cdots + 216u + 16$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{77} + 26y^{76} + \cdots + 3416576y - 65536$
$c_2, c_4$	$y^{77} - 34y^{76} + \cdots + 1568y - 256$
$c_3, c_8$	$y^{77} + 30y^{76} + \cdots - 2621440y - 262144$
$c_5$	$y^{77} - 12y^{76} + \cdots + 120020616504y - 4430766096$
$c_6, c_{12}$	$y^{77} + 36y^{76} + \cdots + 216y - 16$
$c_7, c_9, c_{10}$	$y^{77} - 74y^{76} + \cdots + 7712y - 256$
$c_{11}$	$y^{77} + 12y^{76} + \cdots + 84256y - 256$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.508886 + 0.845592I$		
$a = 0.440978 - 0.047456I$		
$b = 1.241720 + 0.241243I$	$-2.40889 + 4.27390I$	$-3.74115 - 6.44221I$
$c = 1.093870 + 0.364160I$		
$d = 0.443416 - 0.224335I$		
$u = -0.508886 - 0.845592I$		
$a = 0.440978 + 0.047456I$		
$b = 1.241720 - 0.241243I$	$-2.40889 - 4.27390I$	$-3.74115 + 6.44221I$
$c = 1.093870 - 0.364160I$		
$d = 0.443416 + 0.224335I$		
$u = 0.848496 + 0.585068I$		
$a = 0.460618 + 0.092632I$		
$b = 1.086610 - 0.419625I$	$-3.78378 + 2.11500I$	$-7.65464 - 1.99007I$
$c = -0.531801 + 1.113610I$		
$d = -1.32944 + 1.48023I$		
$u = 0.848496 - 0.585068I$		
$a = 0.460618 - 0.092632I$		
$b = 1.086610 + 0.419625I$	$-3.78378 - 2.11500I$	$-7.65464 + 1.99007I$
$c = -0.531801 - 1.113610I$		
$d = -1.32944 - 1.48023I$		
$u = 0.990280 + 0.319237I$		
$a = 0.580990 - 0.275212I$		
$b = 0.405766 + 0.665904I$	$2.98745 + 0.86657I$	0
$c = 0.427768 - 0.711040I$		
$d = 0.003575 - 0.815149I$		
$u = 0.990280 - 0.319237I$		
$a = 0.580990 + 0.275212I$		
$b = 0.405766 - 0.665904I$	$2.98745 - 0.86657I$	0
$c = 0.427768 + 0.711040I$		
$d = 0.003575 + 0.815149I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.617221 + 0.733532I$		
$a = 0.450662 + 0.060640I$		
$b = 1.179500 - 0.293267I$	$-4.09446 + 0.35704I$	$-8.04104 + 0.70386I$
$c = -0.865693 + 0.615479I$		
$d = -0.818586 + 0.224399I$		
$u = 0.617221 - 0.733532I$		
$a = 0.450662 - 0.060640I$		
$b = 1.179500 + 0.293267I$	$-4.09446 - 0.35704I$	$-8.04104 - 0.70386I$
$c = -0.865693 - 0.615479I$		
$d = -0.818586 - 0.224399I$		
$u = -0.517431 + 0.792256I$		
$a = -0.31513 - 2.57319I$		
$b = -1.046890 + 0.382880I$	$-2.57405 - 0.08416I$	$-4.54592 - 2.74373I$
$c = 0.979361 + 0.392885I$		
$d = 0.491329 - 0.041258I$		
$u = -0.517431 - 0.792256I$		
$a = -0.31513 + 2.57319I$		
$b = -1.046890 - 0.382880I$	$-2.57405 + 0.08416I$	$-4.54592 + 2.74373I$
$c = 0.979361 - 0.392885I$		
$d = 0.491329 + 0.041258I$		
$u = 0.082487 + 0.936352I$		
$a = 0.92003 - 1.14713I$		
$b = -0.574527 + 0.530498I$	$1.72016 + 1.41215I$	$1.65188 - 3.77223I$
$c = 1.17847 - 0.94179I$		
$d = -0.290045 + 0.776854I$		
$u = 0.082487 - 0.936352I$		
$a = 0.92003 + 1.14713I$		
$b = -0.574527 - 0.530498I$	$1.72016 - 1.41215I$	$1.65188 + 3.77223I$
$c = 1.17847 + 0.94179I$		
$d = -0.290045 - 0.776854I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.582500 + 0.889546I$ $a = -0.41276 + 2.17080I$ $b = -1.084530 - 0.444586I$ $c = -1.204890 + 0.519522I$ $d = -0.720160 - 0.450817I$	$-3.62010 - 5.07823I$	$-6.10660 + 7.37918I$
$u = 0.582500 - 0.889546I$ $a = -0.41276 - 2.17080I$ $b = -1.084530 + 0.444586I$ $c = -1.204890 - 0.519522I$ $d = -0.720160 + 0.450817I$	$-3.62010 + 5.07823I$	$-6.10660 - 7.37918I$
$u = -0.228301 + 1.040040I$ $a = 0.723676 + 0.951160I$ $b = -0.493370 - 0.665886I$ $c = -0.513216 - 0.329220I$ $d = -0.312338 - 0.999680I$	$3.92825 - 1.69884I$	$4.65730 + 2.32962I$
$u = -0.228301 - 1.040040I$ $a = 0.723676 - 0.951160I$ $b = -0.493370 + 0.665886I$ $c = -0.513216 + 0.329220I$ $d = -0.312338 + 0.999680I$	$3.92825 + 1.69884I$	$4.65730 - 2.32962I$
$u = -0.782003 + 0.468875I$ $a = 0.479369 - 0.088840I$ $b = 1.016810 + 0.373767I$ $c = -0.789013 - 1.040910I$ $d = -0.598791 - 0.392671I$	$-0.65497 - 3.51390I$	$-3.54011 + 4.44478I$
$u = -0.782003 - 0.468875I$ $a = 0.479369 + 0.088840I$ $b = 1.016810 - 0.373767I$ $c = -0.789013 + 1.040910I$ $d = -0.598791 + 0.392671I$	$-0.65497 + 3.51390I$	$-3.54011 - 4.44478I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.374962 + 1.039940I$		
$a = 0.679703 - 0.804881I$		
$b = -0.387561 + 0.725229I$	$3.38837 - 3.78470I$	0
$c = 0.822403 - 0.322418I$		
$d = 0.559284 - 0.573519I$		
$u = 0.374962 - 1.039940I$		
$a = 0.679703 + 0.804881I$		
$b = -0.387561 - 0.725229I$	$3.38837 + 3.78470I$	0
$c = 0.822403 + 0.322418I$		
$d = 0.559284 + 0.573519I$		
$u = -0.965284 + 0.548957I$		
$a = 0.458449 - 0.109175I$		
$b = 1.064210 + 0.491568I$	$-1.81197 - 6.85619I$	0
$c = 0.42927 + 1.36968I$		
$d = 1.62931 + 2.26420I$		
$u = -0.965284 - 0.548957I$		
$a = 0.458449 + 0.109175I$		
$b = 1.064210 - 0.491568I$	$-1.81197 + 6.85619I$	0
$c = 0.42927 - 1.36968I$		
$d = 1.62931 - 2.26420I$		
$u = -0.288832 + 1.092220I$		
$a = 0.655250 + 0.897222I$		
$b = -0.469158 - 0.726873I$	$4.40655 + 2.61636I$	0
$c = -1.39360 - 1.30383I$		
$d = 0.03743 + 1.65696I$		
$u = -0.288832 - 1.092220I$		
$a = 0.655250 - 0.897222I$		
$b = -0.469158 + 0.726873I$	$4.40655 - 2.61636I$	0
$c = -1.39360 + 1.30383I$		
$d = 0.03743 - 1.65696I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.815552 + 0.276755I$ $a = 0.510621 - 0.104384I$ $b = 0.879842 + 0.384286I$ $c = -0.134802 + 0.964627I$ $d = -0.35977 + 2.02275I$	$0.065597 - 0.205341I$	$-1.21551 + 1.86968I$
$u = -0.815552 - 0.276755I$ $a = 0.510621 + 0.104384I$ $b = 0.879842 - 0.384286I$ $c = -0.134802 - 0.964627I$ $d = -0.35977 - 2.02275I$	$0.065597 + 0.205341I$	$-1.21551 - 1.86968I$
$u = 0.008067 + 1.164640I$ $a = 0.524425 + 1.231070I$ $b = -0.707115 - 0.687536I$ $c = -1.63638 - 0.81487I$ $d = 1.18786 + 0.86080I$	$4.97078 - 4.99360I$	0
$u = 0.008067 - 1.164640I$ $a = 0.524425 - 1.231070I$ $b = -0.707115 + 0.687536I$ $c = -1.63638 + 0.81487I$ $d = 1.18786 - 0.86080I$	$4.97078 + 4.99360I$	0
$u = -1.177360 + 0.140655I$ $a = 0.514925 + 0.236545I$ $b = 0.603622 - 0.736667I$ $c = -0.027412 - 0.316988I$ $d = 1.016250 - 0.656214I$	$6.72367 + 2.38646I$	0
$u = -1.177360 - 0.140655I$ $a = 0.514925 - 0.236545I$ $b = 0.603622 + 0.736667I$ $c = -0.027412 + 0.316988I$ $d = 1.016250 + 0.656214I$	$6.72367 - 2.38646I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.516220 + 1.088150I$ $a = -0.14742 + 1.74242I$ $b = -1.048210 - 0.569836I$ $c = 1.105030 - 0.234332I$ $d = 0.652838 + 0.110822I$	$2.28765 - 3.11487I$	0
$u = 0.516220 - 1.088150I$ $a = -0.14742 - 1.74242I$ $b = -1.048210 + 0.569836I$ $c = 1.105030 + 0.234332I$ $d = 0.652838 - 0.110822I$	$2.28765 + 3.11487I$	0
$u = -1.143240 + 0.423905I$ $a = 0.533939 + 0.311288I$ $b = 0.397778 - 0.814910I$ $c = -0.113421 - 0.926777I$ $d = -0.01193 - 1.62150I$	$5.54743 - 5.38085I$	0
$u = -1.143240 - 0.423905I$ $a = 0.533939 - 0.311288I$ $b = 0.397778 + 0.814910I$ $c = -0.113421 + 0.926777I$ $d = -0.01193 + 1.62150I$	$5.54743 + 5.38085I$	0
$u = -1.079500 + 0.575143I$ $a = 0.447329 - 0.120477I$ $b = 1.084300 + 0.561354I$ $c = -0.260355 - 1.216300I$ $d = -0.90050 - 1.58646I$	$1.00971 - 5.65602I$	0
$u = -1.079500 - 0.575143I$ $a = 0.447329 + 0.120477I$ $b = 1.084300 - 0.561354I$ $c = -0.260355 + 1.216300I$ $d = -0.90050 + 1.58646I$	$1.00971 + 5.65602I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.163010 + 0.411297I$		
$a = 0.457972 + 0.144139I$		
$b = 0.986739 - 0.625293I$	$5.58247 + 2.79509I$	0
$c = 0.071233 - 0.902749I$		
$d = -0.10463 - 1.67523I$		
$u = 1.163010 - 0.411297I$		
$a = 0.457972 - 0.144139I$		
$b = 0.986739 + 0.625293I$	$5.58247 - 2.79509I$	0
$c = 0.071233 + 0.902749I$		
$d = -0.10463 + 1.67523I$		
$u = -0.530613 + 1.137340I$		
$a = -0.16592 - 1.65105I$		
$b = -1.060260 + 0.599620I$	$2.68982 + 5.10175I$	0
$c = 1.76242 + 0.34399I$		
$d = -0.11353 - 1.60654I$		
$u = -0.530613 - 1.137340I$		
$a = -0.16592 + 1.65105I$		
$b = -1.060260 - 0.599620I$	$2.68982 - 5.10175I$	0
$c = 1.76242 - 0.34399I$		
$d = -0.11353 + 1.60654I$		
$u = -0.601554 + 1.104580I$		
$a = -0.29797 - 1.68572I$		
$b = -1.101680 + 0.575244I$	$1.29562 + 8.75795I$	0
$c = -1.271520 - 0.218579I$		
$d = -0.788648 + 0.590297I$		
$u = -0.601554 - 1.104580I$		
$a = -0.29797 + 1.68572I$		
$b = -1.101680 - 0.575244I$	$1.29562 - 8.75795I$	0
$c = -1.271520 + 0.218579I$		
$d = -0.788648 - 0.590297I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.666542 + 1.084300I$ $a = -0.41901 + 1.68178I$ $b = -1.139490 - 0.559856I$ $c = -1.67095 + 0.67803I$ $d = -0.92819 - 1.72084I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ $-2.21245 - 7.79054I$	0
$u = 0.666542 - 1.084300I$ $a = -0.41901 - 1.68178I$ $b = -1.139490 + 0.559856I$ $c = -1.67095 - 0.67803I$ $d = -0.92819 + 1.72084I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ $-2.21245 + 7.79054I$	0
$u = 0.620529 + 0.325559I$ $a = 0.505847 + 0.065088I$ $b = 0.944687 - 0.250227I$ $c = 1.17082 - 0.90601I$ $d = 0.328371 - 0.105641I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ $0.115678 - 1.341920I$	$-2.41782 + 1.83708I$
$u = 0.620529 - 0.325559I$ $a = 0.505847 - 0.065088I$ $b = 0.944687 + 0.250227I$ $c = 1.17082 + 0.90601I$ $d = 0.328371 + 0.105641I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ $0.115678 + 1.341920I$	$-2.41782 - 1.83708I$
$u = 1.161000 + 0.625559I$ $a = 0.435979 + 0.124995I$ $b = 1.119470 - 0.607651I$ $c = 0.116799 - 1.332580I$ $d = 1.12055 - 2.13672I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ $3.39852 + 10.69180I$	0
$u = 1.161000 - 0.625559I$ $a = 0.435979 - 0.124995I$ $b = 1.119470 + 0.607651I$ $c = 0.116799 + 1.332580I$ $d = 1.12055 + 2.13672I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ $3.39852 - 10.69180I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.423653 + 0.527399I$ $a = 0.911492 - 0.383290I$ $b = -0.067745 + 0.392021I$ $c = 1.10825 - 1.37074I$ $d = 0.418849 + 0.237150I$	$1.92120 + 0.81846I$	$4.58107 + 0.87681I$
$u = 0.423653 - 0.527399I$ $a = 0.911492 + 0.383290I$ $b = -0.067745 - 0.392021I$ $c = 1.10825 + 1.37074I$ $d = 0.418849 - 0.237150I$	$1.92120 - 0.81846I$	$4.58107 - 0.87681I$
$u = 0.662834 + 0.003253I$ $a = 0.620162 + 0.068360I$ $b = 0.593125 - 0.175609I$ $c = 0.844082 + 0.426336I$ $d = 2.08843 + 0.88000I$	$0.58945 + 2.77011I$	$-1.22579 - 6.61866I$
$u = 0.662834 - 0.003253I$ $a = 0.620162 - 0.068360I$ $b = 0.593125 + 0.175609I$ $c = 0.844082 - 0.426336I$ $d = 2.08843 - 0.88000I$	$0.58945 - 2.77011I$	$-1.22579 + 6.61866I$
$u = -0.703559 + 1.143570I$ $a = -0.43434 - 1.56703I$ $b = -1.164260 + 0.592620I$ $c = 1.82114 + 0.75444I$ $d = 1.05029 - 2.27985I$	$0.07596 + 12.98220I$	0
$u = -0.703559 - 1.143570I$ $a = -0.43434 + 1.56703I$ $b = -1.164260 - 0.592620I$ $c = 1.82114 - 0.75444I$ $d = 1.05029 + 2.27985I$	$0.07596 - 12.98220I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.624723 + 1.201920I$		
$a = 0.513586 - 0.684350I$		
$b = -0.298481 + 0.934769I$	$5.70918 - 6.67323I$	0
$c = 1.343470 - 0.036213I$		
$d = 0.266666 + 0.986054I$		
$u = 0.624723 - 1.201920I$		
$a = 0.513586 + 0.684350I$		
$b = -0.298481 - 0.934769I$	$5.70918 + 6.67323I$	0
$c = 1.343470 + 0.036213I$		
$d = 0.266666 - 0.986054I$		
$u = -0.127875 + 0.624992I$		
$a = 0.463873 - 0.011490I$		
$b = 1.154440 + 0.053363I$	$-0.93270 - 1.56780I$	$1.99036 - 0.81001I$
$c = 0.435762 - 0.358619I$		
$d = -0.038269 + 0.332638I$		
$u = -0.127875 - 0.624992I$		
$a = 0.463873 + 0.011490I$		
$b = 1.154440 - 0.053363I$	$-0.93270 + 1.56780I$	$1.99036 + 0.81001I$
$c = 0.435762 + 0.358619I$		
$d = -0.038269 - 0.332638I$		
$u = 0.115044 + 1.357830I$		
$a = 0.267455 + 1.195870I$		
$b = -0.821892 - 0.796376I$	$9.14335 - 2.92995I$	0
$c = 0.264755 + 0.381750I$		
$d = -0.286633 - 1.330580I$		
$u = 0.115044 - 1.357830I$		
$a = 0.267455 - 1.195870I$		
$b = -0.821892 + 0.796376I$	$9.14335 + 2.92995I$	0
$c = 0.264755 - 0.381750I$		
$d = -0.286633 + 1.330580I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.518606 + 1.307430I$ $a = 0.471054 + 0.753719I$ $b = -0.403718 - 0.954094I$ $c = -1.155440 + 0.212036I$ $d = 0.575561 + 0.435533I$	$10.68990 + 3.50430I$	0
$u = -0.518606 - 1.307430I$ $a = 0.471054 - 0.753719I$ $b = -0.403718 + 0.954094I$ $c = -1.155440 - 0.212036I$ $d = 0.575561 - 0.435533I$	$10.68990 - 3.50430I$	0
$u = -0.758435 + 1.184640I$ $a = -0.47779 - 1.47703I$ $b = -1.198260 + 0.612902I$ $c = -1.59692 - 0.12137I$ $d = -0.81262 + 1.86068I$	$2.97939 + 12.30500I$	0
$u = -0.758435 - 1.184640I$ $a = -0.47779 + 1.47703I$ $b = -1.198260 - 0.612902I$ $c = -1.59692 + 0.12137I$ $d = -0.81262 - 1.86068I$	$2.97939 - 12.30500I$	0
$u = -0.69467 + 1.24791I$ $a = 0.480437 + 0.659159I$ $b = -0.277875 - 0.990754I$ $c = -1.49960 + 0.03004I$ $d = -0.12141 + 1.59948I$	$8.2281 + 11.9338I$	0
$u = -0.69467 - 1.24791I$ $a = 0.480437 - 0.659159I$ $b = -0.277875 + 0.990754I$ $c = -1.49960 - 0.03004I$ $d = -0.12141 - 1.59948I$	$8.2281 - 11.9338I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.043030 + 0.567805I$ $a = 4.08839 - 1.11685I$ $b = -0.772390 + 0.062177I$ $c = 0.144313 - 0.425715I$ $d = -0.013781 + 0.345769I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	$2.35018 - 5.72620I$
$u = -0.043030 - 0.567805I$ $a = 4.08839 + 1.11685I$ $b = -0.772390 - 0.062177I$ $c = 0.144313 + 0.425715I$ $d = -0.013781 - 0.345769I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	$2.35018 + 5.72620I$
$u = 0.68480 + 1.26233I$ $a = -0.34737 + 1.42430I$ $b = -1.161620 - 0.662680I$ $c = 1.48561 + 0.06309I$ $d = -0.01550 + 1.56219I$	$8.38263 - 9.37788I$	0
$u = 0.68480 - 1.26233I$ $a = -0.34737 - 1.42430I$ $b = -1.161620 + 0.662680I$ $c = 1.48561 - 0.06309I$ $d = -0.01550 - 1.56219I$	$8.38263 + 9.37788I$	0
$u = 0.80648 + 1.20827I$ $a = -0.51585 + 1.41688I$ $b = -1.226880 - 0.623174I$ $c = 1.70051 - 0.09972I$ $d = 0.83764 + 2.32804I$	$5.3240 - 17.7550I$	0
$u = 0.80648 - 1.20827I$ $a = -0.51585 - 1.41688I$ $b = -1.226880 + 0.623174I$ $c = 1.70051 + 0.09972I$ $d = 0.83764 - 2.32804I$	$5.3240 + 17.7550I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.00564 + 1.45291I$		
$a = 0.279733 - 1.057890I$		
$b = -0.766380 + 0.883500I$	$13.06970 - 1.34685I$	0
$c = 0.013236 + 0.605297I$		
$d = -0.02236 - 1.73200I$		
$u = 0.00564 - 1.45291I$		
$a = 0.279733 + 1.057890I$		
$b = -0.766380 - 0.883500I$	$13.06970 + 1.34685I$	0
$c = 0.013236 - 0.605297I$		
$d = -0.02236 + 1.73200I$		
$u = -0.22004 + 1.44810I$		
$a = 0.134599 - 1.184980I$		
$b = -0.905365 + 0.833146I$	$12.6554 + 7.5654I$	0
$c = -0.514065 + 0.581969I$		
$d = 0.82290 - 1.33139I$		
$u = -0.22004 - 1.44810I$		
$a = 0.134599 + 1.184980I$		
$b = -0.905365 - 0.833146I$	$12.6554 - 7.5654I$	0
$c = -0.514065 - 0.581969I$		
$d = 0.82290 + 1.33139I$		
$u = -0.499413$		
$a = 0.544041$		
$b = 0.838096$	-1.20722	-9.11790
$c = -0.278989$		
$d = -0.886893$		

$$\text{II. } I_2^u = \langle u^3a^2 - u^3a + \dots - 4a + 4, u^3a^2 - 2u^3a + \dots - 2a + 2, a^2u^2 + b + 2a - 2, 2u^3a^2 - 3u^3a + \dots + a^3 + u, u^4 + u^2 + u + 1 \rangle$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ -a^2u^2 - 2a + 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^3a^2 + 2u^3a - a^2u - 2u^3 - au + 2a - 2 \\ -u^3a^2 + a^2u^2 + u^3a - a^2u - 2u^3 - au + 4a - 4 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^3a^2 - a^2u^2 - a^2u + 2u^2a - a^2 - 3au - 2u^2 + 2u \\ -u^3a^2 - a^2u^2 - 3u^3a + u^2a + 2u^3 - a^2 - 5au - 2u^2 - 3a + 4u + 2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a \\ a^2u^2 + u^2a + 2a - 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a^2u^2 + u^2a + 3a - 2 \\ a^2u^2 + u^2a + 2a - 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 2u^3a - a^2u - 2u^3 + au + 2a - 2u - 2 \\ -u^3a^2 + 3u^3a - 2a^2u - 4u^3 + au + 4a - 2u - 4 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 2u^3a - a^2u - 2u^3 + 2au + 2a - 2u - 2 \\ -u^3a^2 + 4u^3a - 2a^2u - 4u^3 + au + 4a - 2u - 4 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^3a^2 + a^2u^2 + 2u^3a - 2u^2a - 2u^3 + a^2 + 2u^2 + 3a - 2 \\ -u^3a^2 + 2a^2u^2 + u^3a - u^2a - 2u^3 + a^2 + 2u^2 + 5a - 4 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-4u^3 + 4u^2 - 2$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{12} + 8u^{11} + \dots - 5u + 1$
$c_2, c_4, c_7$ $c_9, c_{10}$	$u^{12} - 4u^{10} + 2u^9 + 6u^8 - 6u^7 - u^6 + 6u^5 - 5u^4 - u^3 + 3u^2 - u + 1$
$c_3, c_6, c_8$ $c_{12}$	$(u^4 + u^2 + u + 1)^3$
$c_5$	$(u^4 + 3u^3 + 4u^2 + 3u + 2)^3$
$c_{11}$	$(u^4 - 2u^3 + 3u^2 - u + 1)^3$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{12} - 8y^{11} + \cdots - 31y + 1$
$c_2, c_4, c_7$ $c_9, c_{10}$	$y^{12} - 8y^{11} + \cdots + 5y + 1$
$c_3, c_6, c_8$ $c_{12}$	$(y^4 + 2y^3 + 3y^2 + y + 1)^3$
$c_5$	$(y^4 - y^3 + 2y^2 + 7y + 4)^3$
$c_{11}$	$(y^4 + 2y^3 + 7y^2 + 5y + 1)^3$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.547424 + 0.585652I$		
$a = 0.805204 + 0.420651I$		
$b = -0.024351 - 0.509694I$	$-0.98010 + 1.39709I$	$-3.77019 - 3.86736I$
$c = 0.555240 + 0.479815I$		
$d = 0.395109 + 0.559365I$		
$u = -0.547424 + 0.585652I$		
$a = 0.468622 - 0.054836I$		
$b = 1.105090 + 0.246330I$	$-0.98010 + 1.39709I$	$-3.77019 - 3.86736I$
$c = -1.24165 - 1.00900I$		
$d = -2.55169 - 1.38604I$		
$u = -0.547424 + 0.585652I$		
$a = -1.06407 - 3.47080I$		
$b = -1.080740 + 0.263364I$	$-0.98010 + 1.39709I$	$-3.77019 - 3.86736I$
$c = -1.01721 - 1.29340I$		
$d = -0.641886 + 0.175397I$		
$u = -0.547424 - 0.585652I$		
$a = 0.805204 - 0.420651I$		
$b = -0.024351 + 0.509694I$	$-0.98010 - 1.39709I$	$-3.77019 + 3.86736I$
$c = 0.555240 - 0.479815I$		
$d = 0.395109 - 0.559365I$		
$u = -0.547424 - 0.585652I$		
$a = 0.468622 + 0.054836I$		
$b = 1.105090 - 0.246330I$	$-0.98010 - 1.39709I$	$-3.77019 + 3.86736I$
$c = -1.24165 + 1.00900I$		
$d = -2.55169 + 1.38604I$		
$u = -0.547424 - 0.585652I$		
$a = -1.06407 + 3.47080I$		
$b = -1.080740 - 0.263364I$	$-0.98010 - 1.39709I$	$-3.77019 + 3.86736I$
$c = -1.01721 + 1.29340I$		
$d = -0.641886 - 0.175397I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.547424 + 1.120870I$ $a = 0.573365 - 0.708694I$ $b = -0.310026 + 0.852826I$ $c = -1.72860 + 0.38800I$ $d = -0.04577 - 1.58115I$	$2.62503 - 7.64338I$	$1.77019 + 6.51087I$
$u = 0.547424 + 1.120870I$ $a = 0.415110 + 0.046138I$ $b = 1.379600 - 0.264482I$ $c = 1.170990 - 0.175799I$ $d = 0.561298 + 0.342574I$	$2.62503 - 7.64338I$	$1.77019 + 6.51087I$
$u = 0.547424 + 1.120870I$ $a = -0.19823 + 1.67624I$ $b = -1.069580 - 0.588344I$ $c = 1.26123 - 1.65288I$ $d = 1.28293 + 2.03964I$	$2.62503 - 7.64338I$	$1.77019 + 6.51087I$
$u = 0.547424 - 1.120870I$ $a = 0.573365 + 0.708694I$ $b = -0.310026 - 0.852826I$ $c = -1.72860 - 0.38800I$ $d = -0.04577 + 1.58115I$	$2.62503 + 7.64338I$	$1.77019 - 6.51087I$
$u = 0.547424 - 1.120870I$ $a = 0.415110 - 0.046138I$ $b = 1.379600 + 0.264482I$ $c = 1.170990 + 0.175799I$ $d = 0.561298 - 0.342574I$	$2.62503 + 7.64338I$	$1.77019 - 6.51087I$
$u = 0.547424 - 1.120870I$ $a = -0.19823 - 1.67624I$ $b = -1.069580 + 0.588344I$ $c = 1.26123 + 1.65288I$ $d = 1.28293 - 2.03964I$	$2.62503 + 7.64338I$	$1.77019 - 6.51087I$

$$\text{III. } I_3^u = \langle u^5a^2 - 4u^5a + \dots + 8a - 8, -2u^5a + 2u^5 + \dots + 4a - 4, a^2u^2 + b + 2a - 2, -4u^5a^2 + 6u^5a + \dots - 6a + 2, u^6 - u^5 + \dots - 2u + 1 \rangle$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ -a^2u^2 - 2a + 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 2u^5a - 2u^5 + \dots - 4a + 4 \\ -u^5a^2 + 4u^5a + \dots - 8a + 8 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^5a^2 + 2u^3a^2 + 3u^4a - a^2u^2 - 2u^4 + 2a^2u + 5u^2a - a^2 - 4u^2 + 3a - 2 \\ 2u^5a^2 + 3u^5a + \dots - 2a^2 - a \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a \\ a^2u^2 + u^2a + 2a - 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a^2u^2 + u^2a + 3a - 2 \\ a^2u^2 + u^2a + 2a - 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 2u^5a - 2u^5 + \dots - 4a + 4 \\ 4u^5a - 4u^5 + \dots - 8a + 8 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 2u^5a - 2u^5 + \dots - 4a + 4 \\ 4u^5a - 4u^5 + \dots - 8a + 8 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 5u^5a - 4u^5 + \dots - 5a + 4 \\ -u^5a^2 + 6u^5a + \dots - 9a + 8 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-4u^3 - 4u + 2$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{18} + 12u^{17} + \cdots + 8u^2 + 1$
$c_2, c_4, c_7$ $c_9, c_{10}$	$u^{18} - 6u^{16} + \cdots - 2u^3 + 1$
$c_3, c_6, c_8$ $c_{12}$	$(u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1)^3$
$c_5$	$(u^3 - u^2 + 1)^6$
$c_{11}$	$(u^6 - 3u^5 + 4u^4 - 2u^3 + 1)^3$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{18} - 12y^{17} + \cdots + 16y + 1$
$c_2, c_4, c_7$ $c_9, c_{10}$	$y^{18} - 12y^{17} + \cdots + 8y^2 + 1$
$c_3, c_6, c_8$ $c_{12}$	$(y^6 + 3y^5 + 4y^4 + 2y^3 + 1)^3$
$c_5$	$(y^3 - y^2 + 2y - 1)^6$
$c_{11}$	$(y^6 - y^5 + 4y^4 - 2y^3 + 8y^2 + 1)^3$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.498832 + 1.001300I$		
$a = 0.661188 + 0.699980I$		
$b = -0.286853 - 0.754987I$	$0.26574 + 2.82812I$	$-1.50976 - 2.97945I$
$c = 1.44004 + 0.30697I$		
$d = 0.171485 - 0.832500I$		
$u = -0.498832 + 1.001300I$		
$a = 0.426451 - 0.044014I$		
$b = 1.320220 + 0.239468I$	$0.26574 + 2.82812I$	$-1.50976 - 2.97945I$
$c = -1.064340 - 0.398265I$		
$d = -0.994564 - 0.186619I$		
$u = -0.498832 + 1.001300I$		
$a = -0.12503 - 1.93170I$		
$b = -1.033370 + 0.515520I$	$0.26574 + 2.82812I$	$-1.50976 - 2.97945I$
$c = -1.17291 - 1.50894I$		
$d = -0.97180 + 1.42148I$		
$u = -0.498832 - 1.001300I$		
$a = 0.661188 - 0.699980I$		
$b = -0.286853 + 0.754987I$	$0.26574 - 2.82812I$	$-1.50976 + 2.97945I$
$c = 1.44004 - 0.30697I$		
$d = 0.171485 + 0.832500I$		
$u = -0.498832 - 1.001300I$		
$a = 0.426451 + 0.044014I$		
$b = 1.320220 - 0.239468I$	$0.26574 - 2.82812I$	$-1.50976 + 2.97945I$
$c = -1.064340 + 0.398265I$		
$d = -0.994564 + 0.186619I$		
$u = -0.498832 - 1.001300I$		
$a = -0.12503 + 1.93170I$		
$b = -1.033370 - 0.515520I$	$0.26574 - 2.82812I$	$-1.50976 + 2.97945I$
$c = -1.17291 + 1.50894I$		
$d = -0.97180 - 1.42148I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.284920 + 1.115140I$ $a = 0.633702 - 0.904691I$ $b = -0.480591 + 0.741524I$ $c = -1.63240 - 0.20951I$ $d = 0.919012 - 0.439251I$	4.40332	$5.01951 + 0.I$
$u = 0.284920 + 1.115140I$ $a = 0.419155 + 0.023943I$ $b = 1.377990 - 0.135834I$ $c = 0.633400 - 0.165486I$ $d = 0.184355 - 0.759840I$	4.40332	$5.01951 + 0.I$
$u = 0.284920 + 1.115140I$ $a = 0.27186 + 1.60496I$ $b = -0.897403 - 0.605690I$ $c = 1.42916 - 1.30860I$ $d = -0.10337 + 1.74578I$	4.40332	$5.01951 + 0.I$
$u = 0.284920 - 1.115140I$ $a = 0.633702 + 0.904691I$ $b = -0.480591 - 0.741524I$ $c = -1.63240 + 0.20951I$ $d = 0.919012 + 0.439251I$	4.40332	$5.01951 + 0.I$
$u = 0.284920 - 1.115140I$ $a = 0.419155 - 0.023943I$ $b = 1.377990 + 0.135834I$ $c = 0.633400 + 0.165486I$ $d = 0.184355 + 0.759840I$	4.40332	$5.01951 + 0.I$
$u = 0.284920 - 1.115140I$ $a = 0.27186 - 1.60496I$ $b = -0.897403 + 0.605690I$ $c = 1.42916 + 1.30860I$ $d = -0.10337 - 1.74578I$	4.40332	$5.01951 + 0.I$

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.713912 + 0.305839I$ $a = 0.699357 - 0.245678I$ $b = 0.272813 + 0.447127I$ $c = 0.033182 + 0.755013I$ $d = 0.26687 + 1.47455I$	$0.26574 + 2.82812I$	$-1.50976 - 2.97945I$
$u = 0.713912 + 0.305839I$ $a = 0.509246 + 0.082706I$ $b = 0.913222 - 0.310725I$ $c = 1.33201 - 0.98810I$ $d = 3.24106 - 1.64838I$	$0.26574 + 2.82812I$	$-1.50976 - 2.97945I$
$u = 0.713912 + 0.305839I$ $a = -3.49593 + 2.56326I$ $b = -1.186030 - 0.136403I$ $c = 1.001860 - 0.780958I$ $d = 0.286941 - 0.228535I$	$0.26574 + 2.82812I$	$-1.50976 - 2.97945I$
$u = 0.713912 - 0.305839I$ $a = 0.699357 + 0.245678I$ $b = 0.272813 - 0.447127I$ $c = 0.033182 - 0.755013I$ $d = 0.26687 - 1.47455I$	$0.26574 - 2.82812I$	$-1.50976 + 2.97945I$
$u = 0.713912 - 0.305839I$ $a = 0.509246 - 0.082706I$ $b = 0.913222 + 0.310725I$ $c = 1.33201 + 0.98810I$ $d = 3.24106 + 1.64838I$	$0.26574 - 2.82812I$	$-1.50976 + 2.97945I$
$u = 0.713912 - 0.305839I$ $a = -3.49593 - 2.56326I$ $b = -1.186030 + 0.136403I$ $c = 1.001860 + 0.780958I$ $d = 0.286941 + 0.228535I$	$0.26574 - 2.82812I$	$-1.50976 + 2.97945I$

$$\text{IV. } I_1^v = \langle c, d - v - 1, b, a - 1, v^2 + v + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ v + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -v \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} v \\ v + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ -v - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} v + 1 \\ v + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-4v + 1$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_8$	$u^2$
$c_5, c_{12}$	$u^2 - u + 1$
$c_6, c_{11}$	$u^2 + u + 1$
$c_7$	$(u + 1)^2$
$c_9, c_{10}$	$(u - 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_8$	$y^2$
$c_5, c_6, c_{11}$ $c_{12}$	$y^2 + y + 1$
$c_7, c_9, c_{10}$	$(y - 1)^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -0.500000 + 0.866025I$		
$a = 1.00000$		
$b = 0$	$1.64493 + 2.02988I$	$3.00000 - 3.46410I$
$c = 0$		
$d = 0.500000 + 0.866025I$		
$v = -0.500000 - 0.866025I$		
$a = 1.00000$		
$b = 0$	$1.64493 - 2.02988I$	$3.00000 + 3.46410I$
$c = 0$		
$d = 0.500000 - 0.866025I$		

$$\mathbf{V} \cdot I_2^v = \langle a, d, c - v, b - 1, v^2 - v + 1 \rangle$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} v - 1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} v \\ -v \end{pmatrix}$$

(ii) **Obstruction class** = 1

(iii) **Cusp Shapes** =  $-4v - 7$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^2$
$c_3, c_7, c_8$ $c_9, c_{10}$	$u^2$
$c_4$	$(u + 1)^2$
$c_5, c_{11}, c_{12}$	$u^2 + u + 1$
$c_6$	$u^2 - u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^2$
$c_3, c_7, c_8$ $c_9, c_{10}$	$y^2$
$c_5, c_6, c_{11}$ $c_{12}$	$y^2 + y + 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 0.500000 + 0.866025I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0$		
$b = 1.00000$	$-1.64493 + 2.02988I$	$-9.00000 - 3.46410I$
$c = 0.500000 + 0.866025I$		
$d = 0$		
$v = 0.500000 - 0.866025I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0$		
$b = 1.00000$	$-1.64493 - 2.02988I$	$-9.00000 + 3.46410I$
$c = 0.500000 - 0.866025I$		
$d = 0$		

$$\text{VI. } I_3^v = \langle a, d+1, c+a, b-1, v-1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_9$ $c_{10}$	$u - 1$
$c_3, c_5, c_6$ $c_8, c_{11}, c_{12}$	$u$
$c_4, c_7$	$u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_7, c_9, c_{10}$	$y - 1$
$c_3, c_5, c_6$ $c_8, c_{11}, c_{12}$	$y$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 1.00000$		
$a = 0$		
$b = 1.00000$	0	0
$c = 0$		
$d = -1.00000$		

VII.

$$I_4^v = \langle a, -c^2v + cv + \dots - 2ca + a, dv + 1, c^2v^2 - v^2c + \dots + a^2 - av, b - 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} v \\ 0 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0 \\ 1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} c \\ d \end{pmatrix} \\ a_6 &= \begin{pmatrix} c - 1 \\ dc + 1 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 1 \\ -1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 0 \\ -1 \end{pmatrix} \\ a_8 &= \begin{pmatrix} v \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} c + v \\ d \end{pmatrix} \\ a_7 &= \begin{pmatrix} -c \\ -d \end{pmatrix} \\ a_{12} &= \begin{pmatrix} c \\ d - c \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $d^2 + v^2 - 4c$

(iv) **u-Polynomials at the component** : It cannot be defined for a positive dimension component.

(v) **Riley Polynomials at the component** : It cannot be defined for a positive dimension component.

**(iv) Complex Volumes and Cusp Shapes**

Solution to $I_4^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = \dots$		
$a = \dots$		
$b = \dots$	$-2.02988I$	$0.19616 + 2.89071I$
$c = \dots$		
$d = \dots$		

### VIII. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$u^2(u - 1)^3(u^{12} + 8u^{11} + \dots - 5u + 1)(u^{18} + 12u^{17} + \dots + 8u^2 + 1)$ $\cdot (u^{77} + 34u^{76} + \dots + 1568u + 256)$
$c_2$	$u^2(u - 1)^3$ $\cdot (u^{12} - 4u^{10} + 2u^9 + 6u^8 - 6u^7 - u^6 + 6u^5 - 5u^4 - u^3 + 3u^2 - u + 1)$ $\cdot (u^{18} - 6u^{16} + \dots - 2u^3 + 1)(u^{77} - 8u^{76} + \dots - 72u + 16)$
$c_3, c_8$	$u^5(u^4 + u^2 + u + 1)^3(u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1)^3$ $\cdot (u^{77} + 2u^{76} + \dots + 2560u^2 + 512)$
$c_4$	$u^2(u + 1)^3$ $\cdot (u^{12} - 4u^{10} + 2u^9 + 6u^8 - 6u^7 - u^6 + 6u^5 - 5u^4 - u^3 + 3u^2 - u + 1)$ $\cdot (u^{18} - 6u^{16} + \dots - 2u^3 + 1)(u^{77} - 8u^{76} + \dots - 72u + 16)$
$c_5$	$u(u^2 - u + 1)(u^2 + u + 1)(u^3 - u^2 + 1)^6(u^4 + 3u^3 + 4u^2 + 3u + 2)^3$ $\cdot (u^{77} + 2u^{76} + \dots + 351912u + 66564)$
$c_6, c_{12}$	$u(u^2 - u + 1)(u^2 + u + 1)(u^4 + u^2 + u + 1)^3$ $\cdot ((u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1)^3)(u^{77} - 2u^{76} + \dots - 27u^2 + 4)$
$c_7$	$u^2(u + 1)^3$ $\cdot (u^{12} - 4u^{10} + 2u^9 + 6u^8 - 6u^7 - u^6 + 6u^5 - 5u^4 - u^3 + 3u^2 - u + 1)$ $\cdot (u^{18} - 6u^{16} + \dots - 2u^3 + 1)(u^{77} + 8u^{76} + \dots - 72u + 16)$
$c_9, c_{10}$	$u^2(u - 1)^3$ $\cdot (u^{12} - 4u^{10} + 2u^9 + 6u^8 - 6u^7 - u^6 + 6u^5 - 5u^4 - u^3 + 3u^2 - u + 1)$ $\cdot (u^{18} - 6u^{16} + \dots - 2u^3 + 1)(u^{77} + 8u^{76} + \dots - 72u + 16)$
$c_{11}$	$u(u^2 + u + 1)^2(u^4 - 2u^3 + 3u^2 - u + 1)^3(u^6 - 3u^5 + 4u^4 - 2u^3 + 1)^3$ $\cdot (u^{77} - 36u^{76} + \dots + 216u + 16)$

## IX. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$y^2(y - 1)^3(y^{12} - 8y^{11} + \dots - 31y + 1)(y^{18} - 12y^{17} + \dots + 16y + 1)$ $\cdot (y^{77} + 26y^{76} + \dots + 3416576y - 65536)$
$c_2, c_4$	$y^2(y - 1)^3(y^{12} - 8y^{11} + \dots + 5y + 1)(y^{18} - 12y^{17} + \dots + 8y^2 + 1)$ $\cdot (y^{77} - 34y^{76} + \dots + 1568y - 256)$
$c_3, c_8$	$y^5(y^4 + 2y^3 + 3y^2 + y + 1)^3(y^6 + 3y^5 + 4y^4 + 2y^3 + 1)^3$ $\cdot (y^{77} + 30y^{76} + \dots - 2621440y - 262144)$
$c_5$	$y(y^2 + y + 1)^2(y^3 - y^2 + 2y - 1)^6(y^4 - y^3 + 2y^2 + 7y + 4)^3$ $\cdot (y^{77} - 12y^{76} + \dots + 120020616504y - 4430766096)$
$c_6, c_{12}$	$y(y^2 + y + 1)^2(y^4 + 2y^3 + 3y^2 + y + 1)^3(y^6 + 3y^5 + 4y^4 + 2y^3 + 1)^3$ $\cdot (y^{77} + 36y^{76} + \dots + 216y - 16)$
$c_7, c_9, c_{10}$	$y^2(y - 1)^3(y^{12} - 8y^{11} + \dots + 5y + 1)(y^{18} - 12y^{17} + \dots + 8y^2 + 1)$ $\cdot (y^{77} - 74y^{76} + \dots + 7712y - 256)$
$c_{11}$	$y(y^2 + y + 1)^2(y^4 + 2y^3 + 7y^2 + 5y + 1)^3$ $\cdot ((y^6 - y^5 + 4y^4 - 2y^3 + 8y^2 + 1)^3)(y^{77} + 12y^{76} + \dots + 84256y - 256)$