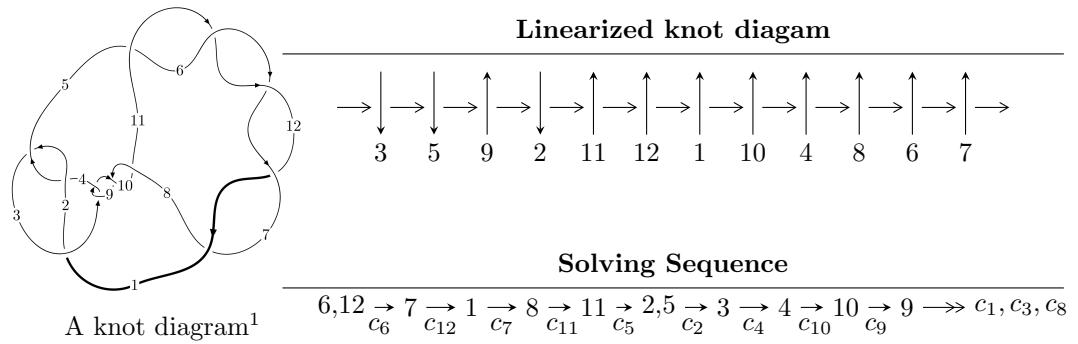


$12a_{0160} (K12a_{0160})$



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle u^{51} + u^{50} + \dots + b - u, -u^{51} - u^{50} + \dots + a - 1, u^{52} + 2u^{51} + \dots + 2u + 1 \rangle$$

$$I_2^u = \langle b + u + 2, a - u - 1, u^2 - u - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 54 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle u^{51} + u^{50} + \dots + b - u, \ -u^{51} - u^{50} + \dots + a - 1, \ u^{52} + 2u^{51} + \dots + 2u + 1 \rangle^{\mathbf{I}_*}$$

(i) **Arc colorings**

$$\begin{aligned} a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u \\ -u^3 + u \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} u^{51} + u^{50} + \dots + 7u + 1 \\ -u^{51} - u^{50} + \dots - 4u^2 + u \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} u^{50} + u^{49} + \dots + 18u^2 + 5u \\ u^{51} - 32u^{49} + \dots + 2u + 1 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -2u^{51} - u^{50} + \dots - 7u - 1 \\ 3u^{51} + 2u^{50} + \dots + u + 1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u^7 - 4u^5 + 4u^3 - 2u \\ -u^9 + 5u^7 - 7u^5 + 2u^3 + u \end{pmatrix} \\ a_9 &= \begin{pmatrix} -u^{12} + 7u^{10} - 17u^8 + 18u^6 - 10u^4 + u^2 + 1 \\ u^{14} - 8u^{12} + 23u^{10} - 28u^8 + 12u^6 + 2u^4 - 3u^2 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** =  $-1$

(iii) **Cusp Shapes** =  $8u^{51} + 9u^{50} + \dots - 9u + 11$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{52} + 29u^{51} + \cdots + 29u + 1$
$c_2, c_4$	$u^{52} - 3u^{51} + \cdots - 9u + 1$
$c_3, c_9$	$u^{52} - u^{51} + \cdots - 4u + 4$
$c_5, c_6, c_7$ $c_{11}, c_{12}$	$u^{52} - 2u^{51} + \cdots - 2u + 1$
$c_8, c_{10}$	$u^{52} - 15u^{51} + \cdots - 248u + 16$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{52} - 9y^{51} + \cdots - 593y + 1$
$c_2, c_4$	$y^{52} - 29y^{51} + \cdots - 29y + 1$
$c_3, c_9$	$y^{52} - 15y^{51} + \cdots - 248y + 16$
$c_5, c_6, c_7$ $c_{11}, c_{12}$	$y^{52} - 66y^{51} + \cdots + 6y + 1$
$c_8, c_{10}$	$y^{52} + 41y^{51} + \cdots - 9504y + 256$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.002200 + 0.101685I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.620325 + 0.568001I$	$5.42587 + 0.91536I$	$15.8250 + 0.I$
$b = -0.338736 - 0.201694I$		
$u = 1.002200 - 0.101685I$		
$a = 0.620325 - 0.568001I$	$5.42587 - 0.91536I$	$15.8250 + 0.I$
$b = -0.338736 + 0.201694I$		
$u = 0.900408 + 0.415514I$		
$a = -0.686316 + 0.426160I$	$-2.89703 + 10.97490I$	$6.84879 - 9.10557I$
$b = -1.32817 - 1.98079I$		
$u = 0.900408 - 0.415514I$		
$a = -0.686316 - 0.426160I$	$-2.89703 - 10.97490I$	$6.84879 + 9.10557I$
$b = -1.32817 + 1.98079I$		
$u = 0.993272 + 0.210152I$		
$a = 0.306112 - 0.310737I$	$4.36145 + 5.53576I$	$12.8247 - 7.7042I$
$b = -1.09437 - 1.05834I$		
$u = 0.993272 - 0.210152I$		
$a = 0.306112 + 0.310737I$	$4.36145 - 5.53576I$	$12.8247 + 7.7042I$
$b = -1.09437 + 1.05834I$		
$u = 0.887221 + 0.376671I$		
$a = 0.216936 + 0.254530I$	$0.28073 + 6.02352I$	$10.12786 - 6.24694I$
$b = 0.512607 - 0.524064I$		
$u = 0.887221 - 0.376671I$		
$a = 0.216936 - 0.254530I$	$0.28073 - 6.02352I$	$10.12786 + 6.24694I$
$b = 0.512607 + 0.524064I$		
$u = -0.853207 + 0.384206I$		
$a = 0.903606 + 0.104965I$	$-3.75080 - 4.74137I$	$5.53664 + 4.96484I$
$b = 1.14253 - 1.97773I$		
$u = -0.853207 - 0.384206I$		
$a = 0.903606 - 0.104965I$	$-3.75080 + 4.74137I$	$5.53664 - 4.96484I$
$b = 1.14253 + 1.97773I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.825680 + 0.382316I$	$-3.92292 + 1.91465I$	$5.33907 - 3.86780I$
$a = -0.111743 - 0.969230I$		
$b = 1.57224 + 1.67207I$		
$u = 0.825680 - 0.382316I$	$-3.92292 - 1.91465I$	$5.33907 + 3.86780I$
$a = -0.111743 + 0.969230I$		
$b = 1.57224 - 1.67207I$		
$u = -0.768059 + 0.439344I$	$-3.69972 + 3.78870I$	$5.61035 - 2.00055I$
$a = -0.195399 - 0.893583I$		
$b = -1.17619 + 1.70576I$		
$u = -0.768059 - 0.439344I$	$-3.69972 - 3.78870I$	$5.61035 + 2.00055I$
$a = -0.195399 + 0.893583I$		
$b = -1.17619 - 1.70576I$		
$u = -0.869138 + 0.090566I$	$1.28982 - 1.61982I$	$10.04112 + 4.38556I$
$a = -0.624942 - 0.906814I$		
$b = 0.124670 - 0.964759I$		
$u = -0.869138 - 0.090566I$	$1.28982 + 1.61982I$	$10.04112 - 4.38556I$
$a = -0.624942 + 0.906814I$		
$b = 0.124670 + 0.964759I$		
$u = -0.778648 + 0.361263I$	$-0.394378 - 0.492969I$	$9.04055 + 1.45710I$
$a = -0.381137 + 0.106397I$		
$b = -0.541900 - 0.279638I$		
$u = -0.778648 - 0.361263I$	$-0.394378 + 0.492969I$	$9.04055 - 1.45710I$
$a = -0.381137 - 0.106397I$		
$b = -0.541900 + 0.279638I$		
$u = 0.803120$		
$a = -0.675162$	0.0369555	14.8580
$b = 2.05557$		
$u = -0.062250 + 0.639708I$	$-5.82794 - 7.41916I$	$2.02402 + 6.23213I$
$a = -3.04229 + 0.33326I$		
$b = 0.028753 - 0.273837I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.062250 - 0.639708I$		
$a = -3.04229 - 0.33326I$	$-5.82794 + 7.41916I$	$2.02402 - 6.23213I$
$b = 0.028753 + 0.273837I$		
$u = 0.013286 + 0.599769I$		
$a = 3.16045 + 0.60539I$	$-6.37556 + 1.41175I$	$0.512224 - 0.772694I$
$b = 0.050264 - 0.426280I$		
$u = 0.013286 - 0.599769I$		
$a = 3.16045 - 0.60539I$	$-6.37556 - 1.41175I$	$0.512224 + 0.772694I$
$b = 0.050264 + 0.426280I$		
$u = -0.051648 + 0.589699I$		
$a = -0.118187 + 0.761845I$	$-2.57484 - 2.75018I$	$4.73313 + 3.20106I$
$b = 0.019107 + 0.393978I$		
$u = -0.051648 - 0.589699I$		
$a = -0.118187 - 0.761845I$	$-2.57484 + 2.75018I$	$4.73313 - 3.20106I$
$b = 0.019107 - 0.393978I$		
$u = -0.429505 + 0.363992I$		
$a = -0.283846 + 0.092161I$	$0.985801 + 0.373941I$	$10.64681 + 0.40187I$
$b = -0.501430 + 0.658806I$		
$u = -0.429505 - 0.363992I$		
$a = -0.283846 - 0.092161I$	$0.985801 - 0.373941I$	$10.64681 - 0.40187I$
$b = -0.501430 - 0.658806I$		
$u = -0.260485 + 0.467225I$		
$a = -1.65751 + 0.54880I$	$0.44749 - 3.27943I$	$7.33672 + 8.28421I$
$b = -0.417669 - 0.022465I$		
$u = -0.260485 - 0.467225I$		
$a = -1.65751 - 0.54880I$	$0.44749 + 3.27943I$	$7.33672 - 8.28421I$
$b = -0.417669 + 0.022465I$		
$u = -0.449135$		
$a = -0.461577$	$0.706606$	$14.1070$
$b = -0.372331$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.58988$		
$a = 2.20327$	7.80979	0
$b = -3.13699$		
$u = 1.62815 + 0.10007I$		
$a = 2.77026 + 1.09581I$	$4.49371 - 1.83490I$	0
$b = -3.78872 - 1.31091I$		
$u = 1.62815 - 0.10007I$		
$a = 2.77026 - 1.09581I$	$4.49371 + 1.83490I$	0
$b = -3.78872 + 1.31091I$		
$u = 1.65492 + 0.07803I$		
$a = 0.986803 - 0.272171I$	$8.08427 + 2.03863I$	0
$b = -1.64509 + 0.11104I$		
$u = 1.65492 - 0.07803I$		
$a = 0.986803 + 0.272171I$	$8.08427 - 2.03863I$	0
$b = -1.64509 - 0.11104I$		
$u = -1.66220 + 0.09221I$		
$a = -3.12446 + 1.04099I$	$4.73033 - 3.67102I$	0
$b = 4.21717 - 1.24397I$		
$u = -1.66220 - 0.09221I$		
$a = -3.12446 - 1.04099I$	$4.73033 + 3.67102I$	0
$b = 4.21717 + 1.24397I$		
$u = -1.67125$		
$a = -3.25510$	8.84251	0
$b = 4.37303$		
$u = 1.67019 + 0.09664I$		
$a = -2.99043 - 2.84568I$	$5.04044 + 6.55656I$	0
$b = 4.30768 + 4.47913I$		
$u = 1.67019 - 0.09664I$		
$a = -2.99043 + 2.84568I$	$5.04044 - 6.55656I$	0
$b = 4.30768 - 4.47913I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.68080 + 0.01746I$		
$a = 0.01213 - 2.15798I$	$10.32590 + 1.99807I$	0
$b = -0.39566 + 3.61473I$		
$u = 1.68080 - 0.01746I$		
$a = 0.01213 + 2.15798I$	$10.32590 - 1.99807I$	0
$b = -0.39566 - 3.61473I$		
$u = -1.68130 + 0.09775I$		
$a = -0.765995 - 0.522974I$	$9.25802 - 7.84981I$	0
$b = 1.297310 + 0.421881I$		
$u = -1.68130 - 0.09775I$		
$a = -0.765995 + 0.522974I$	$9.25802 + 7.84981I$	0
$b = 1.297310 - 0.421881I$		
$u = -1.68310 + 0.11088I$		
$a = 3.15694 - 2.48000I$	$6.1040 - 13.0204I$	0
$b = -4.50686 + 3.86266I$		
$u = -1.68310 - 0.11088I$		
$a = 3.15694 + 2.48000I$	$6.1040 + 13.0204I$	0
$b = -4.50686 - 3.86266I$		
$u = -1.70835 + 0.02404I$		
$a = 0.042019 + 0.436305I$	$15.0483 - 1.4053I$	0
$b = 0.256089 - 1.030400I$		
$u = -1.70835 - 0.02404I$		
$a = 0.042019 - 0.436305I$	$15.0483 + 1.4053I$	0
$b = 0.256089 + 1.030400I$		
$u = -1.70818 + 0.04745I$		
$a = 1.55667 - 1.83823I$	$13.9392 - 6.5232I$	0
$b = -1.98030 + 3.09035I$		
$u = -1.70818 - 0.04745I$		
$a = 1.55667 + 1.83823I$	$13.9392 + 6.5232I$	0
$b = -1.98030 - 3.09035I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.123626 + 0.224585I$		
$a = 0.84430 + 2.89252I$	$-1.62775 + 0.54260I$	$-3.36212 - 1.40035I$
$b = 0.727029 - 0.150879I$		
$u = 0.123626 - 0.224585I$		
$a = 0.84430 - 2.89252I$	$-1.62775 - 0.54260I$	$-3.36212 + 1.40035I$
$b = 0.727029 + 0.150879I$		

$$\text{II. } I_2^u = \langle b + u + 2, \ a - u - 1, \ u^2 - u - 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ -u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u + 1 \\ -u - 2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 3

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^2$
$c_3, c_8, c_9$ $c_{10}$	$u^2$
$c_4$	$(u + 1)^2$
$c_5, c_6, c_7$	$u^2 - u - 1$
$c_{11}, c_{12}$	$u^2 + u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^2$
$c_3, c_8, c_9$ $c_{10}$	$y^2$
$c_5, c_6, c_7$ $c_{11}, c_{12}$	$y^2 - 3y + 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.618034$		
$a = 0.381966$	-0.657974	3.00000
$b = -1.38197$		
$u = 1.61803$		
$a = 2.61803$	7.23771	3.00000
$b = -3.61803$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^2)(u^{52} + 29u^{51} + \dots + 29u + 1)$
$c_2$	$((u - 1)^2)(u^{52} - 3u^{51} + \dots - 9u + 1)$
$c_3, c_9$	$u^2(u^{52} - u^{51} + \dots - 4u + 4)$
$c_4$	$((u + 1)^2)(u^{52} - 3u^{51} + \dots - 9u + 1)$
$c_5, c_6, c_7$	$(u^2 - u - 1)(u^{52} - 2u^{51} + \dots - 2u + 1)$
$c_8, c_{10}$	$u^2(u^{52} - 15u^{51} + \dots - 248u + 16)$
$c_{11}, c_{12}$	$(u^2 + u - 1)(u^{52} - 2u^{51} + \dots - 2u + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y - 1)^2)(y^{52} - 9y^{51} + \dots - 593y + 1)$
$c_2, c_4$	$((y - 1)^2)(y^{52} - 29y^{51} + \dots - 29y + 1)$
$c_3, c_9$	$y^2(y^{52} - 15y^{51} + \dots - 248y + 16)$
$c_5, c_6, c_7$ $c_{11}, c_{12}$	$(y^2 - 3y + 1)(y^{52} - 66y^{51} + \dots + 6y + 1)$
$c_8, c_{10}$	$y^2(y^{52} + 41y^{51} + \dots - 9504y + 256)$