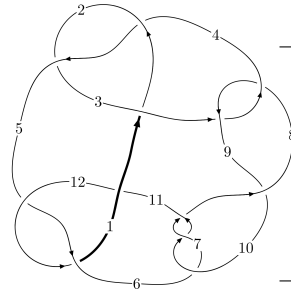
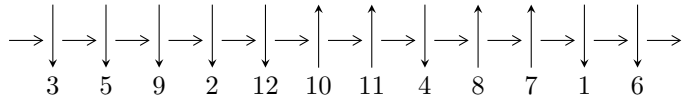


12a<sub>0164</sub> (K12a<sub>0164</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$3,9 \xrightarrow{c_3} 4,5,12 \xrightarrow{c_5} 6 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_8} 8 \xrightarrow{c_9} 10 \xrightarrow{c_{11}} 11 \xrightarrow{c_7} 7 \longrightarrow c_4, c_6, c_{10}, c_{12}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

$$I_1^u = \langle 798299739247u^{24} + 2218887488039u^{23} + \dots + 14116099211116d - 8843381349140, \\ - 364885635753u^{24} + 1117648334550u^{23} + \dots + 28232198422232c - 44559223365168, \\ 458802669672u^{24} + 367351897733u^{23} + \dots + 7058049605558b - 1244576019090, \\ - 1687329917173u^{24} - 1804551705088u^{23} + \dots + 28232198422232a - 30643572770096, \\ u^{25} + 2u^{24} + \dots - 16u - 8 \rangle$$

$$I_2^u = \langle d + 1, 2u^{10}a + u^{10} + \dots - 4a + 4, -u^{10}a + u^{10} + \dots + b - 2, -3u^{10}a + u^{10} + \dots + 2a^2 - 2a, \\ u^{11} - 3u^{10} + 6u^9 - 7u^8 + 7u^7 - 3u^6 - 2u^5 + 8u^4 - 7u^3 + 5u^2 - 2u + 2 \rangle$$

$$I_3^u = \langle d + 1, -u^7a - 3u^5a + u^5 - 2u^3a - 3au + c + a + u, -u^7a + u^7 + u^5 - u^3a + 2u^3 + b + u - 1, \\ 2u^8a - 2u^8 + \dots + 2a - 2, u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1 \rangle$$

$$I_4^u = \langle d + 1, 2u^7c - u^8 + 2u^6c + 2u^5c - u^6 + 2u^4c + u^5 + 4u^3c - 2u^4 + 2u^2c + c^2 - u^2 + c + 2u, \\ -u^7 - u^5 - 2u^3 + b - u, -u^5 + a - u, u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1 \rangle$$

$$I_5^u = \langle 2u^8 + 2u^7 + 4u^6 + 4u^5 + 6u^4 + 4u^3 + 4u^2 + d + 4u, 2u^8 + 2u^6 + 4u^4 + 2u^2 + c + 1, -u^7 - u^5 - 2u^3 + b - \\ - u^5 + a - u, u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1 \rangle$$

$$I_1^v = \langle a, d + 1, c + a + 1, b - 1, v + 1 \rangle$$

$$I_2^v = \langle c, d + 1, b, a - 1, v - 1 \rangle$$

$$I_3^v = \langle a, d + 1, c + a, b - 1, v - 1 \rangle$$

$$I_4^v = \langle a, da - c - 1, dv + v - 1, cv + av - a + v, b - 1 \rangle$$

\* 8 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 95 representations.

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 1$

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<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 7.98 \times 10^{11}u^{24} + 2.22 \times 10^{12}u^{23} + \dots + 1.41 \times 10^{13}d - 8.84 \times 10^{12}, -3.65 \times 10^{11}u^{24} + 1.12 \times 10^{12}u^{23} + \dots + 2.82 \times 10^{13}c - 4.46 \times 10^{13}, 4.59 \times 10^{11}u^{24} + 3.67 \times 10^{11}u^{23} + \dots + 7.06 \times 10^{12}b - 1.24 \times 10^{12}, -1.69 \times 10^{12}u^{24} - 1.80 \times 10^{12}u^{23} + \dots + 2.82 \times 10^{13}a - 3.06 \times 10^{13}, u^{25} + 2u^{24} + \dots - 16u - 8 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.0597662u^{24} + 0.0639182u^{23} + \dots - 0.107083u + 1.08541 \\ -0.0650042u^{24} - 0.0520472u^{23} + \dots + 0.578878u + 0.176334 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.0129244u^{24} - 0.0395877u^{23} + \dots + 0.145173u + 1.57831 \\ -0.0565524u^{24} - 0.157188u^{23} + \dots - 1.05131u + 0.626475 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.0747149u^{24} + 0.105730u^{23} + \dots + 0.724685u + 0.690091 \\ 0.00202430u^{24} + 0.0813992u^{23} + \dots + 0.686595u - 0.973634 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.0597662u^{24} + 0.0639182u^{23} + \dots - 0.107083u + 1.08541 \\ 0.0375166u^{24} + 0.0396045u^{23} + \dots - 0.990575u - 0.621247 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.0972828u^{24} + 0.103523u^{23} + \dots - 1.09766u + 0.464165 \\ 0.0375166u^{24} + 0.0396045u^{23} + \dots - 0.990575u - 0.621247 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.0159383u^{24} - 0.0332769u^{23} + \dots - 0.0633916u + 1.31412 \\ -0.0587766u^{24} - 0.139007u^{23} + \dots - 0.788077u + 0.624033 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.0395277u^{24} + 0.0675081u^{23} + \dots + 0.598270u + 0.845409 \\ -0.0839809u^{24} - 0.0749523u^{23} + \dots + 1.66833u + 0.315163 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= \frac{8058725701665}{7058049605558}u^{24} + \frac{10736954342885}{7058049605558}u^{23} + \dots - \frac{38478403451674}{3529024802779}u - \frac{29622418287164}{3529024802779}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_{11}$	$u^{25} + 12u^{24} + \dots + 3u + 1$
$c_2, c_4, c_5$ $c_{12}$	$u^{25} - 2u^{24} + \dots - u + 1$
$c_3, c_8$	$u^{25} - 2u^{24} + \dots - 16u + 8$
$c_6, c_7, c_{10}$	$u^{25} + 2u^{24} + \dots + 8u + 4$
$c_9$	$u^{25} - 6u^{24} + \dots + 64u + 64$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$y^{25} + 8y^{24} + \dots - 13y - 1$
$c_2, c_4, c_5$ $c_{12}$	$y^{25} - 12y^{24} + \dots + 3y - 1$
$c_3, c_8$	$y^{25} + 6y^{24} + \dots + 64y - 64$
$c_6, c_7, c_{10}$	$y^{25} - 22y^{24} + \dots + 88y - 16$
$c_9$	$y^{25} + 14y^{24} + \dots + 43008y - 4096$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.041130 + 0.234144I$ $a = 0.494693 + 0.148943I$ $b = 0.853442 - 0.558038I$ $c = 0.755058 + 0.911073I$ $d = 1.06504 + 1.52742I$	$3.14377 + 4.46824I$	$-1.00511 - 6.27335I$
$u = 1.041130 - 0.234144I$ $a = 0.494693 - 0.148943I$ $b = 0.853442 + 0.558038I$ $c = 0.755058 - 0.911073I$ $d = 1.06504 - 1.52742I$	$3.14377 - 4.46824I$	$-1.00511 + 6.27335I$
$u = -0.804646 + 0.457350I$ $a = 0.661026 + 0.327338I$ $b = 0.214886 - 0.601608I$ $c = 0.598042 + 0.576553I$ $d = 0.536475 + 0.287592I$	$2.41327 - 0.90505I$	$1.24488 - 0.76686I$
$u = -0.804646 - 0.457350I$ $a = 0.661026 - 0.327338I$ $b = 0.214886 + 0.601608I$ $c = 0.598042 - 0.576553I$ $d = 0.536475 - 0.287592I$	$2.41327 + 0.90505I$	$1.24488 + 0.76686I$
$u = -0.336133 + 1.048560I$ $a = 0.23291 - 1.77170I$ $b = -0.927060 + 0.554841I$ $c = -2.44072 - 0.00843I$ $d = 1.28789 + 1.63373I$	$0.70247 + 6.59785I$	$-2.96140 - 9.56947I$
$u = -0.336133 - 1.048560I$ $a = 0.23291 + 1.77170I$ $b = -0.927060 - 0.554841I$ $c = -2.44072 + 0.00843I$ $d = 1.28789 - 1.63373I$	$0.70247 - 6.59785I$	$-2.96140 + 9.56947I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.926049 + 0.758012I$ $a = 0.437271 + 0.092989I$ $b = 1.187970 - 0.465287I$ $c = 1.33714 + 0.95866I$ $d = 2.30915 + 1.75468I$	$-7.68831 + 5.75962I$	$-10.13195 - 4.49272I$
$u = 0.926049 - 0.758012I$ $a = 0.437271 - 0.092989I$ $b = 1.187970 + 0.465287I$ $c = 1.33714 - 0.95866I$ $d = 2.30915 - 1.75468I$	$-7.68831 - 5.75962I$	$-10.13195 + 4.49272I$
$u = -0.759240 + 0.251838I$ $a = 0.519076 - 0.093919I$ $b = 0.865432 + 0.337523I$ $c = 0.49147 - 1.32874I$ $d = 0.46170 - 2.46248I$	$-2.09943 - 2.64913I$	$-8.26724 + 7.08829I$
$u = -0.759240 - 0.251838I$ $a = 0.519076 + 0.093919I$ $b = 0.865432 - 0.337523I$ $c = 0.49147 + 1.32874I$ $d = 0.46170 + 2.46248I$	$-2.09943 + 2.64913I$	$-8.26724 - 7.08829I$
$u = -0.169266 + 0.764490I$ $a = 1.154810 + 0.812291I$ $b = -0.420684 - 0.407489I$ $c = 0.77118 + 1.56321I$ $d = 0.194809 - 0.625745I$	$1.62680 - 1.08260I$	$3.35440 + 3.89731I$
$u = -0.169266 - 0.764490I$ $a = 1.154810 - 0.812291I$ $b = -0.420684 + 0.407489I$ $c = 0.77118 - 1.56321I$ $d = 0.194809 + 0.625745I$	$1.62680 + 1.08260I$	$3.35440 - 3.89731I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.096683 + 1.217070I$ $a = 0.512583 - 1.088800I$ $b = -0.646064 + 0.751814I$ $c = -0.430370 - 0.686592I$ $d = 0.984764 + 0.859225I$	$8.85704 + 0.98974I$	$4.51267 - 2.53049I$
$u = 0.096683 - 1.217070I$ $a = 0.512583 + 1.088800I$ $b = -0.646064 - 0.751814I$ $c = -0.430370 + 0.686592I$ $d = 0.984764 - 0.859225I$	$8.85704 - 0.98974I$	$4.51267 + 2.53049I$
$u = -0.661369 + 1.057320I$ $a = 0.574734 + 0.631929I$ $b = -0.212320 - 0.866068I$ $c = 0.370547 + 0.605496I$ $d = 0.879125 - 0.241772I$	$4.06909 + 6.32284I$	$1.86961 - 4.09954I$
$u = -0.661369 - 1.057320I$ $a = 0.574734 - 0.631929I$ $b = -0.212320 + 0.866068I$ $c = 0.370547 - 0.605496I$ $d = 0.879125 + 0.241772I$	$4.06909 - 6.32284I$	$1.86961 + 4.09954I$
$u = -1.024310 + 0.754591I$ $a = 0.432415 - 0.103048I$ $b = 1.188320 + 0.521494I$ $c = 1.26644 - 0.88578I$ $d = 2.18015 - 1.59332I$	$-3.22783 - 10.10170I$	$-5.60475 + 6.88322I$
$u = -1.024310 - 0.754591I$ $a = 0.432415 + 0.103048I$ $b = 1.188320 - 0.521494I$ $c = 1.26644 + 0.88578I$ $d = 2.18015 + 1.59332I$	$-3.22783 + 10.10170I$	$-5.60475 - 6.88322I$



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.425565 + 1.220260I$ $a = -0.00331 + 1.51391I$ $b = -1.001440 - 0.660540I$ $c = -1.51553 - 0.69262I$ $d = 1.55274 - 1.36521I$	$6.70868 - 9.75196I$	$0.64851 + 8.69449I$
$u = 0.425565 - 1.220260I$ $a = -0.00331 - 1.51391I$ $b = -1.001440 + 0.660540I$ $c = -1.51553 + 0.69262I$ $d = 1.55274 + 1.36521I$	$6.70868 + 9.75196I$	$0.64851 - 8.69449I$
$u = 0.797713 + 1.033120I$ $a = -0.66380 + 1.63521I$ $b = -1.213130 - 0.525024I$ $c = -1.11526 - 2.93778I$ $d = 2.23603 - 1.53373I$	$-6.80818 - 12.11480I$	$-8.50713 + 8.67244I$
$u = 0.797713 - 1.033120I$ $a = -0.66380 - 1.63521I$ $b = -1.213130 + 0.525024I$ $c = -1.11526 + 2.93778I$ $d = 2.23603 + 1.53373I$	$-6.80818 + 12.11480I$	$-8.50713 - 8.67244I$
$u = -0.832592 + 1.087810I$ $a = -0.64807 - 1.52933I$ $b = -1.234910 + 0.554337I$ $c = -0.80559 + 2.69461I$ $d = 2.22655 + 1.42478I$	$-2.1296 + 16.8657I$	$-4.74649 - 10.33694I$
$u = -0.832592 - 1.087810I$ $a = -0.64807 + 1.52933I$ $b = -1.234910 - 0.554337I$ $c = -0.80559 - 2.69461I$ $d = 2.22655 - 1.42478I$	$-2.1296 - 16.8657I$	$-4.74649 + 10.33694I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.600838$		
$a = 0.591322$		
$b = 0.691126$	-1.26593	-6.81200
$c = -0.564782$		
$d = -1.82889$		

$$\text{II. } I_2^u = \langle d+1, 2u^{10}a + u^{10} + \dots - 4a + 4, -u^{10}a + u^{10} + \dots + b - 2, -3u^{10}a + u^{10} + \dots + 2a^2 - 2a, u^{11} - 3u^{10} + \dots - 2u + 2 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ u^{10}a - u^{10} + \dots - u + 2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^{10}a - \frac{1}{2}u^{10} + \dots + 2a - 2 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{3}{2}u^{10} + \frac{5}{2}u^9 + \dots + \frac{1}{2}u^2 - \frac{3}{2}u \\ -u^{10} + 2u^9 - 3u^8 + 2u^7 - 2u^6 - u^5 + 3u^4 - 4u^3 + u^2 - u + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a \\ -u^{10}a + u^{10} + \dots + u - 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^{10}a + u^{10} + \dots + a - 2 \\ -u^{10}a + u^{10} + \dots + u - 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{3}{2}u^{10} + \frac{9}{2}u^9 + \dots - \frac{3}{2}u + 3 \\ 2u^9 - 3u^8 + 5u^7 - 3u^6 + 4u^5 + 3u^4 - 4u^3 + 6u^2 + 3 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -\frac{1}{2}u^{10} + \frac{1}{2}u^9 + \dots + \frac{1}{2}u^2 + \frac{1}{2}u \\ -u^{10} + 2u^9 - 3u^8 + 3u^7 - 2u^6 + 3u^4 - 2u^3 + 2u^2 + 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= 2u^{10} - 8u^9 + 10u^8 - 10u^7 + 4u^6 - 4u^5 - 14u^4 + 12u^3 - 6u^2 - 8u - 12$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_{11}$	$u^{22} + 11u^{21} + \dots + 40u + 16$
$c_2, c_4, c_5$ $c_{12}$	$u^{22} - u^{21} + \dots - 4u + 4$
$c_3, c_8$	$(u^{11} + 3u^{10} + 6u^9 + 7u^8 + 7u^7 + 3u^6 - 2u^5 - 8u^4 - 7u^3 - 5u^2 - 2u - 2)^2$
$c_6, c_7, c_{10}$	$(u^{11} + u^{10} - 5u^9 - 4u^8 + 9u^7 + 4u^6 - 5u^5 + 3u^4 - 3u^3 - 5u^2 + 3u - 1)^2$
$c_9$	$(u^{11} - 3u^{10} + \dots - 16u + 4)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$y^{22} - 3y^{21} + \dots - 544y + 256$
$c_2, c_4, c_5$ $c_{12}$	$y^{22} - 11y^{21} + \dots - 40y + 16$
$c_3, c_8$	$(y^{11} + 3y^{10} + \dots - 16y - 4)^2$
$c_6, c_7, c_{10}$	$(y^{11} - 11y^{10} + \dots - y - 1)^2$
$c_9$	$(y^{11} + 7y^{10} + \dots + 24y - 16)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.992754$ $a = 0.541424 + 0.181355I$ $b = 0.660661 - 0.556253I$ $c = -0.173971 + 0.420983I$ $d = -1.00000$	3.69004	0.666830
$u = -0.992754$ $a = 0.541424 - 0.181355I$ $b = 0.660661 + 0.556253I$ $c = -0.173971 - 0.420983I$ $d = -1.00000$	3.69004	0.666830
$u = 0.762686 + 0.875309I$ $a = 0.432041 + 0.071853I$ $b = 1.252300 - 0.374583I$ $c = -1.077570 - 0.728230I$ $d = -1.00000$	$-7.89368 - 2.87937I$	$-10.41286 + 3.23335I$
$u = 0.762686 + 0.875309I$ $a = -0.83899 + 1.92556I$ $b = -1.190170 - 0.436468I$ $c = -0.92410 + 2.27150I$ $d = -1.00000$	$-7.89368 - 2.87937I$	$-10.41286 + 3.23335I$
$u = 0.762686 - 0.875309I$ $a = 0.432041 - 0.071853I$ $b = 1.252300 + 0.374583I$ $c = -1.077570 + 0.728230I$ $d = -1.00000$	$-7.89368 + 2.87937I$	$-10.41286 - 3.23335I$
$u = 0.762686 - 0.875309I$ $a = -0.83899 - 1.92556I$ $b = -1.190170 + 0.436468I$ $c = -0.92410 - 2.27150I$ $d = -1.00000$	$-7.89368 + 2.87937I$	$-10.41286 - 3.23335I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.958422 + 0.661375I$ $a = 0.580062 - 0.402139I$ $b = 0.164345 + 0.807203I$ $c = 0.034579 - 0.677196I$ $d = -1.00000$	$-0.20533 + 5.20915I$	$-2.55774 - 3.72118I$
$u = 0.958422 + 0.661375I$ $a = 0.445846 + 0.101514I$ $b = 1.132380 - 0.485520I$ $c = -0.435696 + 0.436381I$ $d = -1.00000$	$-0.20533 + 5.20915I$	$-2.55774 - 3.72118I$
$u = 0.958422 - 0.661375I$ $a = 0.580062 + 0.402139I$ $b = 0.164345 - 0.807203I$ $c = 0.034579 + 0.677196I$ $d = -1.00000$	$-0.20533 - 5.20915I$	$-2.55774 + 3.72118I$
$u = 0.958422 - 0.661375I$ $a = 0.445846 - 0.101514I$ $b = 1.132380 + 0.485520I$ $c = -0.435696 - 0.436381I$ $d = -1.00000$	$-0.20533 - 5.20915I$	$-2.55774 + 3.72118I$
$u = -0.273627 + 1.210650I$ $a = 0.547051 + 0.920222I$ $b = -0.522674 - 0.802934I$ $c = 1.04176 - 1.12578I$ $d = -1.00000$	$8.10965 + 4.33574I$	$3.31243 - 3.68401I$
$u = -0.273627 + 1.210650I$ $a = 0.21367 - 1.45637I$ $b = -0.901383 + 0.672173I$ $c = 0.872371 - 0.074382I$ $d = -1.00000$	$8.10965 + 4.33574I$	$3.31243 - 3.68401I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.273627 - 1.210650I$ $a = 0.547051 - 0.920222I$ $b = -0.522674 + 0.802934I$ $c = 1.04176 + 1.12578I$ $d = -1.00000$	$8.10965 - 4.33574I$	$3.31243 + 3.68401I$
$u = -0.273627 - 1.210650I$ $a = 0.21367 + 1.45637I$ $b = -0.901383 - 0.672173I$ $c = 0.872371 + 0.074382I$ $d = -1.00000$	$8.10965 - 4.33574I$	$3.31243 + 3.68401I$
$u = 0.764438 + 1.080520I$ $a = 0.535931 - 0.594839I$ $b = -0.163987 + 0.927905I$ $c = 0.36336 + 1.80240I$ $d = -1.00000$	$1.11929 - 11.51290I$	$-1.55919 + 7.44023I$
$u = 0.764438 + 1.080520I$ $a = -0.56921 + 1.60575I$ $b = -1.196120 - 0.553243I$ $c = -0.063151 + 0.595914I$ $d = -1.00000$	$1.11929 - 11.51290I$	$-1.55919 + 7.44023I$
$u = 0.764438 - 1.080520I$ $a = 0.535931 + 0.594839I$ $b = -0.163987 - 0.927905I$ $c = 0.36336 - 1.80240I$ $d = -1.00000$	$1.11929 + 11.51290I$	$-1.55919 - 7.44023I$
$u = 0.764438 - 1.080520I$ $a = -0.56921 - 1.60575I$ $b = -1.196120 + 0.553243I$ $c = -0.063151 - 0.595914I$ $d = -1.00000$	$1.11929 + 11.51290I$	$-1.55919 - 7.44023I$



Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.215541 + 0.601634I$ $a = 0.466364 - 0.019525I$ $b = 1.140500 + 0.089613I$ $c = -1.154200 + 0.288451I$ $d = -1.00000$	$-2.97495 + 0.92758I$	$-6.11605 - 7.40073I$
$u = -0.215541 + 0.601634I$ $a = 2.14581 - 3.56073I$ $b = -0.875845 + 0.206022I$ $c = 2.01661 - 3.69343I$ $d = -1.00000$	$-2.97495 + 0.92758I$	$-6.11605 - 7.40073I$
$u = -0.215541 - 0.601634I$ $a = 0.466364 + 0.019525I$ $b = 1.140500 - 0.089613I$ $c = -1.154200 - 0.288451I$ $d = -1.00000$	$-2.97495 - 0.92758I$	$-6.11605 + 7.40073I$
$u = -0.215541 - 0.601634I$ $a = 2.14581 + 3.56073I$ $b = -0.875845 - 0.206022I$ $c = 2.01661 + 3.69343I$ $d = -1.00000$	$-2.97495 - 0.92758I$	$-6.11605 + 7.40073I$

$$\text{III. } I_3^u = \langle d+1, -u^7a - 3u^5a + \cdots + c + a, -u^7a + u^7 + \cdots + b - 1, 2u^8a - 2u^8 + \cdots + 2a - 2, u^9 + u^8 + \cdots + u - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ u^7a - u^7 - u^5 + u^3a - 2u^3 - u + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^7a + 3u^5a - u^5 + 2u^3a + 3au - a - u \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^7a + 2u^5a - u^5 + u^3a + 2au - a - u + 1 \\ u^7a + u^3a + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a \\ -u^7a + u^7 + u^5 - u^3a + u^2a + 2u^3 + u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^7a + u^7 + u^5 - u^3a + u^2a + 2u^3 + a + u - 1 \\ -u^7a + u^7 + u^5 - u^3a + u^2a + 2u^3 + u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^8a - u^6a - u^7 - u^4a - u^5 - u^2a - u^3 + au + u^2 - u \\ -u^8a - u^7a + \cdots + a - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^8a + u^6a + u^7 + u^4a + u^5 - u^3a + u^2a + u^3 - u^2 + u \\ u^8a + u^7a + u^6a + u^7 + u^5a + u^4a + u^3a + u^2a + u^3 + au - u^2 - a + 1 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -4u^7 - 4u^6 - 4u^5 - 4u^4 - 8u^3 - 4u^2 - 6$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{18} + 13u^{17} + \dots + 12u + 1$
$c_2, c_4, c_6$ $c_7, c_{10}$	$u^{18} + u^{17} + \dots - 2u - 1$
$c_3, c_8$	$(u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1)^2$
$c_5, c_{12}$	$(u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1)^2$
$c_9$	$(u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1)^2$
$c_{11}$	$(u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{18} - 17y^{17} + \dots - 156y + 1$
$c_2, c_4, c_6$ $c_7, c_{10}$	$y^{18} - 13y^{17} + \dots - 12y + 1$
$c_3, c_8$	$(y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)^2$
$c_5, c_{12}$	$(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)^2$
$c_9$	$(y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1)^2$
$c_{11}$	$(y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.140343 + 0.966856I$ $a = 0.848261 - 1.052190I$ $b = -0.535620 + 0.576021I$ $c = 1.90798 + 1.04029I$ $d = -1.00000$	$1.78344 - 2.09337I$	$0.51499 + 4.16283I$
$u = 0.140343 + 0.966856I$ $a = 0.432824 + 0.012312I$ $b = 1.308540 - 0.065670I$ $c = -0.899132 - 0.444549I$ $d = -1.00000$	$1.78344 - 2.09337I$	$0.51499 + 4.16283I$
$u = 0.140343 - 0.966856I$ $a = 0.848261 + 1.052190I$ $b = -0.535620 - 0.576021I$ $c = 1.90798 - 1.04029I$ $d = -1.00000$	$1.78344 + 2.09337I$	$0.51499 - 4.16283I$
$u = 0.140343 - 0.966856I$ $a = 0.432824 - 0.012312I$ $b = 1.308540 + 0.065670I$ $c = -0.899132 + 0.444549I$ $d = -1.00000$	$1.78344 + 2.09337I$	$0.51499 - 4.16283I$
$u = 0.628449 + 0.875112I$ $a = 0.435786 + 0.058681I$ $b = 1.253840 - 0.303492I$ $c = -0.559107 + 0.407789I$ $d = -1.00000$	$-0.61694 - 2.45442I$	$-2.32792 + 2.91298I$
$u = 0.628449 + 0.875112I$ $a = -0.55382 + 2.15000I$ $b = -1.112360 - 0.436175I$ $c = 0.109615 + 1.224890I$ $d = -1.00000$	$-0.61694 - 2.45442I$	$-2.32792 + 2.91298I$

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.628449 - 0.875112I$ $a = 0.435786 - 0.058681I$ $b = 1.253840 + 0.303492I$ $c = -0.559107 - 0.407789I$ $d = -1.00000$	$-0.61694 + 2.45442I$	$-2.32792 - 2.91298I$
$u = 0.628449 - 0.875112I$ $a = -0.55382 - 2.15000I$ $b = -1.112360 + 0.436175I$ $c = 0.109615 - 1.224890I$ $d = -1.00000$	$-0.61694 + 2.45442I$	$-2.32792 - 2.91298I$
$u = -0.796005 + 0.733148I$ $a = 0.633756 + 0.458467I$ $b = 0.035822 - 0.749326I$ $c = 0.123475 + 0.714951I$ $d = -1.00000$	$-4.37135 - 1.33617I$	$-7.28409 + 0.70175I$
$u = -0.796005 + 0.733148I$ $a = -1.21946 - 2.08021I$ $b = -1.209730 + 0.357771I$ $c = -1.26364 - 2.41694I$ $d = -1.00000$	$-4.37135 - 1.33617I$	$-7.28409 + 0.70175I$
$u = -0.796005 - 0.733148I$ $a = 0.633756 - 0.458467I$ $b = 0.035822 + 0.749326I$ $c = 0.123475 - 0.714951I$ $d = -1.00000$	$-4.37135 + 1.33617I$	$-7.28409 - 0.70175I$
$u = -0.796005 - 0.733148I$ $a = -1.21946 + 2.08021I$ $b = -1.209730 - 0.357771I$ $c = -1.26364 + 2.41694I$ $d = -1.00000$	$-4.37135 + 1.33617I$	$-7.28409 - 0.70175I$

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.728966 + 0.986295I$ $a = 0.583232 + 0.580415I$ $b = -0.138557 - 0.857281I$ $c = 0.41356 - 1.98115I$ $d = -1.00000$	$-3.59813 + 7.08493I$	$-5.57680 - 5.91335I$
$u = -0.728966 + 0.986295I$ $a = 0.422628 - 0.065267I$ $b = 1.311030 + 0.356898I$ $c = -1.023380 + 0.710048I$ $d = -1.00000$	$-3.59813 + 7.08493I$	$-5.57680 - 5.91335I$
$u = -0.728966 - 0.986295I$ $a = 0.583232 - 0.580415I$ $b = -0.138557 + 0.857281I$ $c = 0.41356 + 1.98115I$ $d = -1.00000$	$-3.59813 - 7.08493I$	$-5.57680 + 5.91335I$
$u = -0.728966 - 0.986295I$ $a = 0.422628 + 0.065267I$ $b = 1.311030 - 0.356898I$ $c = -1.023380 - 0.710048I$ $d = -1.00000$	$-3.59813 - 7.08493I$	$-5.57680 + 5.91335I$
$u = 0.512358$ $a = 0.777682$ $b = 0.285873$ $c = 0.168784$ $d = -1.00000$	$-1.19845$	$-8.65230$
$u = 0.512358$ $a = -8.94409$ $b = -1.11181$ $c = -8.78753$ $d = -1.00000$	$-1.19845$	$-8.65230$

$$\text{IV. } I_4^u = \langle d+1, 2u^7c - u^8 + \dots + c^2 + c, -u^7 - u^5 - 2u^3 + b - u, -u^5 + a - u, u^9 + u^8 + \dots + u - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^5 + u \\ u^7 + u^5 + 2u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} c \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^7c + u^8 + 2u^5c + 2u^3c + u^4 + 2cu + 1 \\ u^7c + u^7 + u^5c + 2u^5 + 2u^3c + 2u^3 + cu + 2u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^5 + u \\ -u^5 - u^3 - u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^3 \\ -u^5 - u^3 - u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^8c - u^6c - u^6 - u^4c + c \\ -u^8c - u^7c - u^8 - u^6c - 2u^5c - u^6 - u^4c - 2u^3c - u^4 - 2cu + c - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^2c + c + 1 \\ u^2c + 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-4u^7 - 4u^6 - 4u^5 - 4u^4 - 8u^3 - 4u^2 - 6$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1)^2$
$c_2, c_4$	$(u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1)^2$
$c_3, c_8$	$(u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1)^2$
$c_5, c_6, c_7$ $c_{10}, c_{12}$	$u^{18} + u^{17} + \dots - 2u - 1$
$c_9$	$(u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1)^2$
$c_{11}$	$u^{18} + 13u^{17} + \dots + 12u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1)^2$
$c_2, c_4$	$(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)^2$
$c_3, c_8$	$(y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)^2$
$c_5, c_6, c_7$ $c_{10}, c_{12}$	$y^{18} - 13y^{17} + \dots - 12y + 1$
$c_9$	$(y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1)^2$
$c_{11}$	$y^{18} - 17y^{17} + \dots - 156y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.140343 + 0.966856I$ $a = 0.72777 + 1.63562I$ $b = -0.772920 - 0.510351I$ $c = 1.76865 + 0.20308I$ $d = -1.00000$	$1.78344 - 2.09337I$	$0.51499 + 4.16283I$
$u = 0.140343 + 0.966856I$ $a = 0.72777 + 1.63562I$ $b = -0.772920 - 0.510351I$ $c = 0.48884 + 1.87834I$ $d = -1.00000$	$1.78344 - 2.09337I$	$0.51499 + 4.16283I$
$u = 0.140343 - 0.966856I$ $a = 0.72777 - 1.63562I$ $b = -0.772920 + 0.510351I$ $c = 1.76865 - 0.20308I$ $d = -1.00000$	$1.78344 + 2.09337I$	$0.51499 - 4.16283I$
$u = 0.140343 - 0.966856I$ $a = 0.72777 - 1.63562I$ $b = -0.772920 + 0.510351I$ $c = 0.48884 - 1.87834I$ $d = -1.00000$	$1.78344 + 2.09337I$	$0.51499 - 4.16283I$
$u = 0.628449 + 0.875112I$ $a = 0.668544 - 0.575994I$ $b = -0.141484 + 0.739668I$ $c = 0.209391 - 0.831348I$ $d = -1.00000$	$-0.61694 - 2.45442I$	$-2.32792 + 2.91298I$
$u = 0.628449 + 0.875112I$ $a = 0.668544 - 0.575994I$ $b = -0.141484 + 0.739668I$ $c = 0.62665 + 2.28784I$ $d = -1.00000$	$-0.61694 - 2.45442I$	$-2.32792 + 2.91298I$

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.628449 - 0.875112I$ $a = 0.668544 + 0.575994I$ $b = -0.141484 - 0.739668I$ $c = 0.209391 + 0.831348I$ $d = -1.00000$	$-0.61694 + 2.45442I$	$-2.32792 - 2.91298I$
$u = 0.628449 - 0.875112I$ $a = 0.668544 + 0.575994I$ $b = -0.141484 - 0.739668I$ $c = 0.62665 - 2.28784I$ $d = -1.00000$	$-0.61694 + 2.45442I$	$-2.32792 - 2.91298I$
$u = -0.796005 + 0.733148I$ $a = 0.445546 - 0.080250I$ $b = 1.173910 + 0.391555I$ $c = -0.485156 - 0.408132I$ $d = -1.00000$	$-4.37135 - 1.33617I$	$-7.28409 + 0.70175I$
$u = -0.796005 + 0.733148I$ $a = 0.445546 - 0.080250I$ $b = 1.173910 + 0.391555I$ $c = -1.156890 + 0.759007I$ $d = -1.00000$	$-4.37135 - 1.33617I$	$-7.28409 + 0.70175I$
$u = -0.796005 - 0.733148I$ $a = 0.445546 + 0.080250I$ $b = 1.173910 - 0.391555I$ $c = -0.485156 + 0.408132I$ $d = -1.00000$	$-4.37135 + 1.33617I$	$-7.28409 - 0.70175I$
$u = -0.796005 - 0.733148I$ $a = 0.445546 + 0.080250I$ $b = 1.173910 - 0.391555I$ $c = -1.156890 - 0.759007I$ $d = -1.00000$	$-4.37135 + 1.33617I$	$-7.28409 - 0.70175I$

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.728966 + 0.986295I$ $a = -0.61569 - 1.78625I$ $b = -1.172470 + 0.500383I$ $c = -0.058202 - 0.817156I$ $d = -1.00000$	$-3.59813 + 7.08493I$	$-5.57680 - 5.91335I$
$u = -0.728966 + 0.986295I$ $a = -0.61569 - 1.78625I$ $b = -1.172470 + 0.500383I$ $c = -0.73020 - 2.13952I$ $d = -1.00000$	$-3.59813 + 7.08493I$	$-5.57680 - 5.91335I$
$u = -0.728966 - 0.986295I$ $a = -0.61569 + 1.78625I$ $b = -1.172470 - 0.500383I$ $c = -0.058202 + 0.817156I$ $d = -1.00000$	$-3.59813 - 7.08493I$	$-5.57680 + 5.91335I$
$u = -0.728966 - 0.986295I$ $a = -0.61569 + 1.78625I$ $b = -1.172470 - 0.500383I$ $c = -0.73020 + 2.13952I$ $d = -1.00000$	$-3.59813 - 7.08493I$	$-5.57680 + 5.91335I$
$u = 0.512358$ $a = 0.547665$ $b = 0.825933$ $c = -0.316966$ $d = -1.00000$	$-1.19845$	$-8.65230$
$u = 0.512358$ $a = 0.547665$ $b = 0.825933$ $c = -2.00921$ $d = -1.00000$	$-1.19845$	$-8.65230$

$$\mathbf{V. } I_5^u = \langle 2u^8 + 2u^7 + \cdots + d + 4u, 2u^8 + 2u^6 + \cdots + c + 1, -u^7 - u^5 - 2u^3 + b - u, -u^5 + a - u, u^9 + u^8 + \cdots + u - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^5 + u \\ u^7 + u^5 + 2u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -2u^8 - 2u^6 - 4u^4 - 2u^2 - 1 \\ -2u^8 - 2u^7 - 4u^6 - 4u^5 - 6u^4 - 4u^3 - 4u^2 - 4u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^7 + 2u^6 + 2u^5 + 2u^4 + 2u^3 + 2u^2 + 2u \\ 2u^8 + u^7 + 4u^6 + u^5 + 6u^4 + 2u^3 + 4u^2 + u + 2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^5 + u \\ -u^5 - u^3 - u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^3 \\ -u^5 - u^3 - u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^8 - u^6 - 3u^4 - 2u^2 - 1 \\ -u^8 - u^7 - 3u^6 - 2u^5 - 5u^4 - 2u^3 - 4u^2 - 2u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 2u^6 + 2u^4 + 3u^2 + 1 \\ 2u^8 + 4u^6 + 6u^4 + 5u^2 + 2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-4u^7 - 4u^6 - 4u^5 - 4u^4 - 8u^3 - 4u^2 - 6$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_{11}$	$u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1$
$c_2, c_4, c_5$ $c_6, c_7, c_{10}$ $c_{12}$	$u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1$
$c_3, c_8$	$u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1$
$c_9$	$u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1$
$c_2, c_4, c_5$ $c_6, c_7, c_{10}$ $c_{12}$	$y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1$
$c_3, c_8$	$y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1$
$c_9$	$y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.140343 + 0.966856I$ $a = 0.72777 + 1.63562I$ $b = -0.772920 - 0.510351I$ $c = -1.76992 + 1.63785I$ $d = 0.75135 - 1.48568I$	$1.78344 - 2.09337I$	$0.51499 + 4.16283I$
$u = 0.140343 - 0.966856I$ $a = 0.72777 - 1.63562I$ $b = -0.772920 + 0.510351I$ $c = -1.76992 - 1.63785I$ $d = 0.75135 + 1.48568I$	$1.78344 + 2.09337I$	$0.51499 - 4.16283I$
$u = 0.628449 + 0.875112I$ $a = 0.668544 - 0.575994I$ $b = -0.141484 + 0.739668I$ $c = 0.472416 - 0.682058I$ $d = 0.714469 + 0.176194I$	$-0.61694 - 2.45442I$	$-2.32792 + 2.91298I$
$u = 0.628449 - 0.875112I$ $a = 0.668544 + 0.575994I$ $b = -0.141484 - 0.739668I$ $c = 0.472416 + 0.682058I$ $d = 0.714469 - 0.176194I$	$-0.61694 + 2.45442I$	$-2.32792 - 2.91298I$
$u = -0.796005 + 0.733148I$ $a = 0.445546 - 0.080250I$ $b = 1.173910 + 0.391555I$ $c = 1.44301 - 1.09794I$ $d = 2.50189 - 2.05286I$	$-4.37135 - 1.33617I$	$-7.28409 + 0.70175I$
$u = -0.796005 - 0.733148I$ $a = 0.445546 + 0.080250I$ $b = 1.173910 - 0.391555I$ $c = 1.44301 + 1.09794I$ $d = 2.50189 + 2.05286I$	$-4.37135 + 1.33617I$	$-7.28409 - 0.70175I$

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.728966 + 0.986295I$ $a = -0.61569 - 1.78625I$ $b = -1.172470 + 0.500383I$ $c = -1.72233 + 3.04233I$ $d = 2.17857 + 1.68557I$	$-3.59813 + 7.08493I$	$-5.57680 - 5.91335I$
$u = -0.728966 - 0.986295I$ $a = -0.61569 + 1.78625I$ $b = -1.172470 - 0.500383I$ $c = -1.72233 - 3.04233I$ $d = 2.17857 - 1.68557I$	$-3.59813 - 7.08493I$	$-5.57680 + 5.91335I$
$u = 0.512358$ $a = 0.547665$ $b = 0.825933$ $c = -1.84635$ $d = -4.29257$	$-1.19845$	$-8.65230$

$$\text{VI. } I_1^v = \langle a, d + 1, c + a + 1, b - 1, v + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -12

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_2, c_5$ $c_{11}$	$u - 1$
$c_3, c_6, c_7$ $c_8, c_9, c_{10}$	$u$
$c_4, c_{12}$	$u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_5, c_{11}, c_{12}$	$y - 1$
$c_3, c_6, c_7$ $c_8, c_9, c_{10}$	$y$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -1.00000$		
$a = 0$		
$b = 1.00000$	-3.28987	-12.0000
$c = -1.00000$		
$d = -1.00000$		

$$\text{VII. } I_2^v = \langle c, d + 1, b, a - 1, v - 1 \rangle$$

**(i) Arc colorings**

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 2 \\ 1 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes = 0**

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_8, c_9$	$u$
$c_5, c_6, c_7$	$u + 1$
$c_{10}, c_{11}, c_{12}$	$u - 1$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_8, c_9$	$y$
$c_5, c_6, c_7$ $c_{10}, c_{11}, c_{12}$	$y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 1.00000$		
$a = 1.00000$		
$b = 0$	0	0
$c = 0$		
$d = -1.00000$		

$$\text{VIII. } I_3^v = \langle a, d + 1, c + a, b - 1, v - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_2, c_{10}$	$u - 1$
$c_3, c_5, c_8$ $c_9, c_{11}, c_{12}$	$u$
$c_4, c_6, c_7$	$u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_6, c_7, c_{10}$	$y - 1$
$c_3, c_5, c_8$ $c_9, c_{11}, c_{12}$	$y$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 1.00000$		
$a = 0$		
$b = 1.00000$	0	0
$c = 0$		
$d = -1.00000$		

$$\text{IX. } I_4^v = \langle a, da - c - 1, dv + v - 1, cv + av - a + v, b - 1 \rangle$$

**(i) Arc colorings**

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1 \\ d \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ d + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ d + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} v - 1 \\ d + 1 \end{pmatrix}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes =  $d^2 + v^2 + 2d - 7$**

**(iv) u-Polynomials at the component :** It cannot be defined for a positive dimension component.

**(v) Riley Polynomials at the component :** It cannot be defined for a positive dimension component.

(iv) Complex Volumes and Cusp Shapes

Solution to $I_4^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = \dots$		
$a = \dots$		
$b = \dots$	-1.64493	-9.16360 - 0.46474I
$c = \dots$		
$d = \dots$		



## X. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_{11}$	$u(u-1)^2(u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1)^3$ $\cdot (u^{18} + 13u^{17} + \dots + 12u + 1)(u^{22} + 11u^{21} + \dots + 40u + 16)$ $\cdot (u^{25} + 12u^{24} + \dots + 3u + 1)$
$c_2$	$u(u-1)^2(u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1)^3$ $\cdot (u^{18} + u^{17} + \dots - 2u - 1)(u^{22} - u^{21} + \dots - 4u + 4)$ $\cdot (u^{25} - 2u^{24} + \dots - u + 1)$
$c_3, c_8$	$u^3(u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1)^5$ $\cdot (u^{11} + 3u^{10} + 6u^9 + 7u^8 + 7u^7 + 3u^6 - 2u^5 - 8u^4 - 7u^3 - 5u^2 - 2u - 2)^2$ $\cdot (u^{25} - 2u^{24} + \dots - 16u + 8)$
$c_4$	$u(u+1)^2(u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1)^3$ $\cdot (u^{18} + u^{17} + \dots - 2u - 1)(u^{22} - u^{21} + \dots - 4u + 4)$ $\cdot (u^{25} - 2u^{24} + \dots - u + 1)$
$c_5, c_{12}$	$u(u-1)(u+1)(u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1)^3$ $\cdot (u^{18} + u^{17} + \dots - 2u - 1)(u^{22} - u^{21} + \dots - 4u + 4)$ $\cdot (u^{25} - 2u^{24} + \dots - u + 1)$
$c_6, c_7$	$u(u+1)^2(u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1)$ $\cdot (u^{11} + u^{10} - 5u^9 - 4u^8 + 9u^7 + 4u^6 - 5u^5 + 3u^4 - 3u^3 - 5u^2 + 3u - 1)^2$ $\cdot ((u^{18} + u^{17} + \dots - 2u - 1)^2)(u^{25} + 2u^{24} + \dots + 8u + 4)$
$c_9$	$u^3(u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1)^5$ $\cdot ((u^{11} - 3u^{10} + \dots - 16u + 4)^2)(u^{25} - 6u^{24} + \dots + 64u + 64)$
$c_{10}$	$u(u-1)^2(u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1)$ $\cdot (u^{11} + u^{10} - 5u^9 - 4u^8 + 9u^7 + 4u^6 - 5u^5 + 3u^4 - 3u^3 - 5u^2 + 3u - 1)^2$ $\cdot ((u^{18} + u^{17} + \dots - 2u - 1)^2)(u^{25} + 2u^{24} + \dots + 8u + 4)$

## XI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$y(y-1)^2(y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1)^3$ $\cdot (y^{18} - 17y^{17} + \dots - 156y + 1)(y^{22} - 3y^{21} + \dots - 544y + 256)$ $\cdot (y^{25} + 8y^{24} + \dots - 13y - 1)$
$c_2, c_4, c_5$ $c_{12}$	$y(y-1)^2(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)^3$ $\cdot (y^{18} - 13y^{17} + \dots - 12y + 1)(y^{22} - 11y^{21} + \dots - 40y + 16)$ $\cdot (y^{25} - 12y^{24} + \dots + 3y - 1)$
$c_3, c_8$	$y^3(y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)^5$ $\cdot ((y^{11} + 3y^{10} + \dots - 16y - 4)^2)(y^{25} + 6y^{24} + \dots + 64y - 64)$
$c_6, c_7, c_{10}$	$y(y-1)^2(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)$ $\cdot ((y^{11} - 11y^{10} + \dots - y - 1)^2)(y^{18} - 13y^{17} + \dots - 12y + 1)^2$ $\cdot (y^{25} - 22y^{24} + \dots + 88y - 16)$
$c_9$	$y^3(y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1)^5$ $\cdot ((y^{11} + 7y^{10} + \dots + 24y - 16)^2)(y^{25} + 14y^{24} + \dots + 43008y - 4096)$