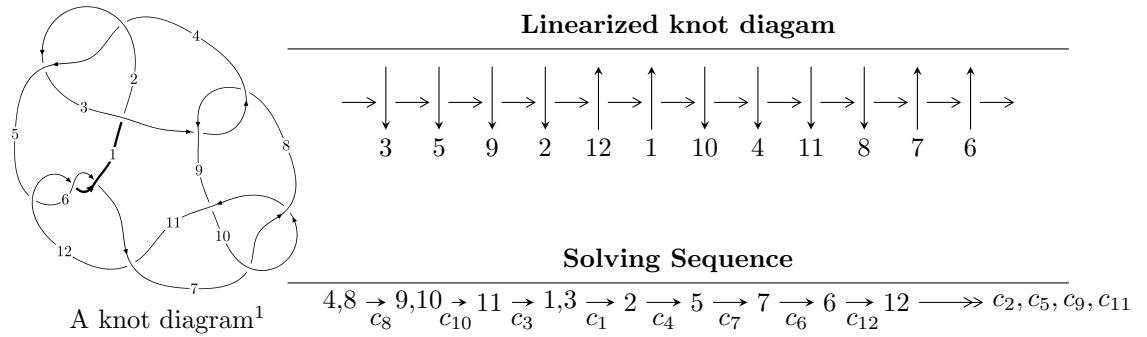


$12a_{0166}$  ( $K12a_{0166}$ )



Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

$$\begin{aligned}
I_1^u &= \langle 458802669672u^{24} + 367351897733u^{23} + \dots + 7058049605558d - 1244576019090, \\
&\quad 147880761515u^{24} - 335144114156u^{23} + \dots + 28232198422232c - 35621876846456, \\
&\quad 1278289196883u^{24} + 1997820239306u^{23} + \dots + 14116099211116b - 10424467040404, \\
&\quad 377943683179u^{24} + 896277965838u^{23} + \dots + 28232198422232a - 14859817453240, \\
&\quad u^{25} + 2u^{24} + \dots - 16u - 8 \rangle \\
I_2^u &= \langle 2u^{10}a - u^{10} + \dots - 6a - 7, 10u^{10}a + 5u^{10} + \dots - 18a - 34, 2u^9a + 3u^{10} + \dots + b + 2a, \\
&\quad 3u^{10}a + 8u^{10} + \dots + 2a^2 - 6, u^{11} - 3u^{10} + 6u^9 - 7u^8 + 7u^7 - 3u^6 - 2u^5 + 8u^4 - 7u^3 + 5u^2 - 2u + 2 \rangle \\
I_3^u &= \langle -u^7 - u^5 - 2u^3 + d - u, -u^7 - 2u^5 - 2u^3 + c - 2u, u^8a + 25u^8 + \dots - 28a + 13, \\
&\quad -u^8 - 2u^7 - 3u^6 - 3u^5 - 3u^4 + u^2a - 2u^3 + a^2 + 2au - 3u^2 + a, \\
&\quad u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1 \rangle \\
I_4^u &= \langle u^8c + 5u^8 + \dots - 27c + 10, 2u^8c - 2u^8 + \dots + 2c - 4, -u^2 + b, -u^2 + a - 1, \\
&\quad u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1 \rangle \\
I_5^u &= \langle -u^7 - u^5 - 2u^3 + d - u, -u^7 - 2u^5 - 2u^3 + c - 2u, -u^2 + b, -u^2 + a - 1, \\
&\quad u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1 \rangle \\
I_1^v &= \langle a, d - 1, c - a - 1, b - 1, v + 1 \rangle \\
I_2^v &= \langle a, d, c - 1, b + 1, v - 1 \rangle \\
I_3^v &= \langle c, d - 1, b, a - 1, v - 1 \rangle \\
I_4^v &= \langle c, d - 1, av + c - v - 1, bv + 1 \rangle
\end{aligned}$$

\* 8 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 95 representations.

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 1$

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<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 4.59 \times 10^{11}u^{24} + 3.67 \times 10^{11}u^{23} + \dots + 7.06 \times 10^{12}d - 1.24 \times 10^{12}, 1.48 \times 10^{11}u^{24} - 3.35 \times 10^{11}u^{23} + \dots + 2.82 \times 10^{13}c - 3.56 \times 10^{13}, 1.28 \times 10^{12}u^{24} + 2.00 \times 10^{12}u^{23} + \dots + 1.41 \times 10^{13}b - 1.04 \times 10^{13}, 3.78 \times 10^{11}u^{24} + 8.96 \times 10^{11}u^{23} + \dots + 2.82 \times 10^{13}a - 1.49 \times 10^{13}, u^{25} + 2u^{24} + \dots - 16u - 8 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.00523802u^{24} + 0.0118710u^{23} + \dots + 0.471795u + 1.26175 \\ -0.0650042u^{24} - 0.0520472u^{23} + \dots + 0.578878u + 0.176334 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.0597662u^{24} + 0.0639182u^{23} + \dots - 0.107083u + 1.08541 \\ -0.0650042u^{24} - 0.0520472u^{23} + \dots + 0.578878u + 0.176334 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.0133870u^{24} - 0.0317467u^{23} + \dots + 1.11820u + 0.526343 \\ -0.0905554u^{24} - 0.141528u^{23} + \dots + 1.83403u + 0.738481 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.0220418u^{24} - 0.0209206u^{23} + \dots + 1.13918u + 0.226210 \\ 0.0223470u^{24} - 0.0180859u^{23} + \dots + 1.17794u - 0.0419041 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.0776559u^{24} - 0.117795u^{23} + \dots + 0.902489u + 0.251920 \\ -0.0910429u^{24} - 0.149542u^{23} + \dots + 2.02069u + 0.778262 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.0972828u^{24} + 0.103523u^{23} + \dots - 1.09766u + 0.464165 \\ 0.0375166u^{24} + 0.0396045u^{23} + \dots - 0.990575u - 0.621247 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.151545u^{24} + 0.183512u^{23} + \dots - 2.01089u - 0.346355 \\ 0.119577u^{24} + 0.131747u^{23} + \dots - 2.07836u - 1.21236 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.0923101u^{24} + 0.0940648u^{23} + \dots - 0.785506u + 0.357069 \\ -0.00497271u^{24} - 0.00945799u^{23} + \dots + 0.312151u - 0.107096 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= \frac{8058725701665}{7058049605558}u^{24} + \frac{10736954342885}{7058049605558}u^{23} + \dots - \frac{38478403451674}{3529024802779}u - \frac{29622418287164}{3529024802779}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_9$	$u^{25} + 12u^{24} + \cdots + 3u + 1$
$c_2, c_4, c_7$ $c_{10}$	$u^{25} - 2u^{24} + \cdots - u + 1$
$c_3, c_8$	$u^{25} - 2u^{24} + \cdots - 16u + 8$
$c_5, c_6, c_{12}$	$u^{25} + 2u^{24} + \cdots + 8u + 4$
$c_{11}$	$u^{25} - 6u^{24} + \cdots + 64u + 64$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_9$	$y^{25} + 8y^{24} + \cdots - 13y - 1$
$c_2, c_4, c_7$ $c_{10}$	$y^{25} - 12y^{24} + \cdots + 3y - 1$
$c_3, c_8$	$y^{25} + 6y^{24} + \cdots + 64y - 64$
$c_5, c_6, c_{12}$	$y^{25} - 22y^{24} + \cdots + 88y - 16$
$c_{11}$	$y^{25} + 14y^{24} + \cdots + 43008y - 4096$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.041130 + 0.234144I$		
$a = 0.008394 + 0.208390I$		
$b = -0.269928 + 1.383510I$	$3.14377 + 4.46824I$	$-1.00511 - 6.27335I$
$c = 1.348140 - 0.409095I$		
$d = 0.853442 - 0.558038I$		
$u = 1.041130 - 0.234144I$		
$a = 0.008394 - 0.208390I$		
$b = -0.269928 - 1.383510I$	$3.14377 - 4.46824I$	$-1.00511 + 6.27335I$
$c = 1.348140 + 0.409095I$		
$d = 0.853442 + 0.558038I$		
$u = -0.804646 + 0.457350I$		
$a = -0.895367 + 0.386742I$		
$b = -1.161700 + 0.803797I$	$2.41327 - 0.90505I$	$1.24488 - 0.76686I$
$c = 0.875912 - 0.274270I$		
$d = 0.214886 - 0.601608I$		
$u = -0.804646 - 0.457350I$		
$a = -0.895367 - 0.386742I$		
$b = -1.161700 - 0.803797I$	$2.41327 + 0.90505I$	$1.24488 + 0.76686I$
$c = 0.875912 + 0.274270I$		
$d = 0.214886 + 0.601608I$		
$u = -0.336133 + 1.048560I$		
$a = -0.156441 - 0.276251I$		
$b = 0.845749 + 0.298371I$	$0.70247 + 6.59785I$	$-2.96140 - 9.56947I$
$c = -0.694150 - 1.216860I$		
$d = -0.927060 + 0.554841I$		
$u = -0.336133 - 1.048560I$		
$a = -0.156441 + 0.276251I$		
$b = 0.845749 - 0.298371I$	$0.70247 - 6.59785I$	$-2.96140 + 9.56947I$
$c = -0.694150 + 1.216860I$		
$d = -0.927060 - 0.554841I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.926049 + 0.758012I$ $a = -1.42251 - 0.81155I$ $b = -0.87316 - 1.69108I$ $c = 1.62524 - 0.37230I$ $d = 1.187970 - 0.465287I$	$-7.68831 + 5.75962I$	$-10.13195 - 4.49272I$
$u = 0.926049 - 0.758012I$ $a = -1.42251 + 0.81155I$ $b = -0.87316 + 1.69108I$ $c = 1.62524 + 0.37230I$ $d = 1.187970 + 0.465287I$	$-7.68831 - 5.75962I$	$-10.13195 + 4.49272I$
$u = -0.759240 + 0.251838I$ $a = -0.264762 - 0.457484I$ $b = -0.051945 + 0.352201I$ $c = 1.384510 + 0.243604I$ $d = 0.865432 + 0.337523I$	$-2.09943 - 2.64913I$	$-8.26724 + 7.08829I$
$u = -0.759240 - 0.251838I$ $a = -0.264762 + 0.457484I$ $b = -0.051945 - 0.352201I$ $c = 1.384510 - 0.243604I$ $d = 0.865432 - 0.337523I$	$-2.09943 + 2.64913I$	$-8.26724 - 7.08829I$
$u = -0.169266 + 0.764490I$ $a = -0.128013 + 0.686745I$ $b = -0.303623 + 0.446468I$ $c = 0.734127 + 0.404802I$ $d = -0.420684 - 0.407489I$	$1.62680 - 1.08260I$	$3.35440 + 3.89731I$
$u = -0.169266 - 0.764490I$ $a = -0.128013 - 0.686745I$ $b = -0.303623 - 0.446468I$ $c = 0.734127 - 0.404802I$ $d = -0.420684 + 0.407489I$	$1.62680 + 1.08260I$	$3.35440 - 3.89731I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.096683 + 1.217070I$ $a = -0.596071 + 0.850107I$ $b = 0.883990 - 0.599145I$ $c = -0.133481 - 0.336989I$ $d = -0.646064 + 0.751814I$	$8.85704 + 0.98974I$	$4.51267 - 2.53049I$
$u = 0.096683 - 1.217070I$ $a = -0.596071 - 0.850107I$ $b = 0.883990 + 0.599145I$ $c = -0.133481 + 0.336989I$ $d = -0.646064 - 0.751814I$	$8.85704 - 0.98974I$	$4.51267 + 2.53049I$
$u = -0.661369 + 1.057320I$ $a = -0.57589 + 1.50124I$ $b = 1.36579 + 0.96216I$ $c = 0.362414 - 0.234138I$ $d = -0.212320 - 0.866068I$	$4.06909 + 6.32284I$	$1.86961 - 4.09954I$
$u = -0.661369 - 1.057320I$ $a = -0.57589 - 1.50124I$ $b = 1.36579 - 0.96216I$ $c = 0.362414 + 0.234138I$ $d = -0.212320 + 0.866068I$	$4.06909 - 6.32284I$	$1.86961 + 4.09954I$
$u = -1.024310 + 0.754591I$ $a = 1.59421 - 0.47481I$ $b = 1.76886 - 1.85122I$ $c = 1.62073 + 0.41845I$ $d = 1.188320 + 0.521494I$	$-3.22783 - 10.10170I$	$-5.60475 + 6.88322I$
$u = -1.024310 - 0.754591I$ $a = 1.59421 + 0.47481I$ $b = 1.76886 + 1.85122I$ $c = 1.62073 - 0.41845I$ $d = 1.188320 - 0.521494I$	$-3.22783 + 10.10170I$	$-5.60475 - 6.88322I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.425565 + 1.220260I$ $a = 0.635489 - 0.691012I$ $b = -0.588986 + 0.949659I$ $c = -1.004750 + 0.853367I$ $d = -1.001440 - 0.660540I$	$6.70868 - 9.75196I$	$0.64851 + 8.69449I$
$u = 0.425565 - 1.220260I$ $a = 0.635489 + 0.691012I$ $b = -0.588986 - 0.949659I$ $c = -1.004750 - 0.853367I$ $d = -1.001440 + 0.660540I$	$6.70868 + 9.75196I$	$0.64851 - 8.69449I$
$u = 0.797713 + 1.033120I$ $a = -0.52447 - 1.76199I$ $b = 1.27330 - 1.73823I$ $c = -1.87693 + 1.11019I$ $d = -1.213130 - 0.525024I$	$-6.80818 - 12.11480I$	$-8.50713 + 8.67244I$
$u = 0.797713 - 1.033120I$ $a = -0.52447 + 1.76199I$ $b = 1.27330 + 1.73823I$ $c = -1.87693 - 1.11019I$ $d = -1.213130 + 0.525024I$	$-6.80818 + 12.11480I$	$-8.50713 - 8.67244I$
$u = -0.832592 + 1.087810I$ $a = 0.39378 - 1.99462I$ $b = -2.07832 - 1.63190I$ $c = -1.88297 - 0.97500I$ $d = -1.234910 + 0.554337I$	$-2.1296 + 16.8657I$	$-4.74649 - 10.33694I$
$u = -0.832592 - 1.087810I$ $a = 0.39378 + 1.99462I$ $b = -2.07832 + 1.63190I$ $c = -1.88297 + 0.97500I$ $d = -1.234910 - 0.554337I$	$-2.1296 - 16.8657I$	$-4.74649 + 10.33694I$

	Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u =$	0.600838		
$a =$	0.863277		
$b =$	0.379944	-1.26593	-6.81200
$c =$	1.28245		
$d =$	0.691126		

$$\text{II. } I_2^u = \langle 2u^{10}a - u^{10} + \dots - 6a - 7, 10u^{10}a + 5u^{10} + \dots - 18a - 34, 2u^9a + 3u^{10} + \dots + b + 2a, 3u^{10}a + 8u^{10} + \dots + 2a^2 - 6, u^{11} - 3u^{10} + \dots - 2u + 2 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_4 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -5u^{10}a - \frac{5}{2}u^{10} + \dots + 9a + 17 \\ -2u^{10}a + u^{10} + \dots + 6a + 7 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -3u^{10}a - \frac{7}{2}u^{10} + \dots + 3a + 10 \\ -2u^{10}a + u^{10} + \dots + 6a + 7 \end{pmatrix} \\ a_1 &= \begin{pmatrix} a \\ -2u^9a - 3u^{10} + \dots - 2a - 3u \end{pmatrix} \\ a_3 &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_2 &= \begin{pmatrix} 3u^{10}a + 3u^{10} + \dots - 3a - 10 \\ 2u^{10}a - 7u^{10} + \dots - 10a - 6 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -2u^9a - 3u^{10} + \dots - 3a - 3u \\ -2u^9a - 3u^{10} + \dots - 2a - 3u \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u^{10}a + \frac{3}{2}u^{10} + \dots + 3a + 1 \\ 2u^{10}a + 5u^{10} + \dots + 6u - 9 \end{pmatrix} \\ a_6 &= \begin{pmatrix} u^9a + \frac{3}{2}u^{10} + \dots + 2a + 1 \\ u^{10}a + 3u^{10} + \dots + 3u - 3 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -u^{10}a - \frac{3}{2}u^{10} + \dots + 3a + 4 \\ -3u^{10} + 6u^9 + \dots - 3u + 3 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= 2u^{10} - 8u^9 + 10u^8 - 10u^7 + 4u^6 - 4u^5 - 14u^4 + 12u^3 - 6u^2 - 8u - 12$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_9$	$u^{22} + 11u^{21} + \cdots + 40u + 16$
$c_2, c_4, c_7$ $c_{10}$	$u^{22} - u^{21} + \cdots - 4u + 4$
$c_3, c_8$	$(u^{11} + 3u^{10} + 6u^9 + 7u^8 + 7u^7 + 3u^6 - 2u^5 - 8u^4 - 7u^3 - 5u^2 - 2u - 2)^2$
$c_5, c_6, c_{12}$	$(u^{11} + u^{10} - 5u^9 - 4u^8 + 9u^7 + 4u^6 - 5u^5 + 3u^4 - 3u^3 - 5u^2 + 3u - 1)^2$
$c_{11}$	$(u^{11} - 3u^{10} + \cdots - 16u + 4)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_9$	$y^{22} - 3y^{21} + \cdots - 544y + 256$
$c_2, c_4, c_7$ $c_{10}$	$y^{22} - 11y^{21} + \cdots - 40y + 16$
$c_3, c_8$	$(y^{11} + 3y^{10} + \cdots - 16y - 4)^2$
$c_5, c_6, c_{12}$	$(y^{11} - 11y^{10} + \cdots - y - 1)^2$
$c_{11}$	$(y^{11} + 7y^{10} + \cdots + 24y - 16)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.992754$ $a = -0.539348 + 0.169351I$ $b = -0.94293 + 1.07661I$ $c = 1.202080 - 0.374899I$ $d = 0.660661 - 0.556253I$	3.69004	0.666830
$u = -0.992754$ $a = -0.539348 - 0.169351I$ $b = -0.94293 - 1.07661I$ $c = 1.202080 + 0.374899I$ $d = 0.660661 + 0.556253I$	3.69004	0.666830
$u = 0.762686 + 0.875309I$ $a = -0.98257 - 1.33960I$ $b = -0.38116 - 2.19608I$ $c = 1.68434 - 0.30273I$ $d = 1.252300 - 0.374583I$	$-7.89368 - 2.87937I$	$-10.41286 + 3.23335I$
$u = 0.762686 + 0.875309I$ $a = -1.44491 - 1.55956I$ $b = 0.70519 - 1.74288I$ $c = -2.02916 + 1.48909I$ $d = -1.190170 - 0.436468I$	$-7.89368 - 2.87937I$	$-10.41286 + 3.23335I$
$u = 0.762686 - 0.875309I$ $a = -0.98257 + 1.33960I$ $b = -0.38116 + 2.19608I$ $c = 1.68434 + 0.30273I$ $d = 1.252300 + 0.374583I$	$-7.89368 + 2.87937I$	$-10.41286 - 3.23335I$
$u = 0.762686 - 0.875309I$ $a = -1.44491 + 1.55956I$ $b = 0.70519 + 1.74288I$ $c = -2.02916 - 1.48909I$ $d = -1.190170 + 0.436468I$	$-7.89368 + 2.87937I$	$-10.41286 - 3.23335I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.958422 + 0.661375I$ $a = -1.166710 - 0.533776I$ $b = -1.25478 - 0.98207I$ $c = 0.744407 + 0.405064I$ $d = 0.164345 + 0.807203I$	$-0.20533 + 5.20915I$	$-2.55774 - 3.72118I$
$u = 0.958422 + 0.661375I$ $a = 1.28394 + 0.64916I$ $b = 1.39078 + 2.09707I$ $c = 1.57823 - 0.38401I$ $d = 1.132380 - 0.485520I$	$-0.20533 + 5.20915I$	$-2.55774 - 3.72118I$
$u = 0.958422 - 0.661375I$ $a = -1.166710 + 0.533776I$ $b = -1.25478 + 0.98207I$ $c = 0.744407 - 0.405064I$ $d = 0.164345 - 0.807203I$	$-0.20533 - 5.20915I$	$-2.55774 + 3.72118I$
$u = 0.958422 - 0.661375I$ $a = 1.28394 - 0.64916I$ $b = 1.39078 - 2.09707I$ $c = 1.57823 + 0.38401I$ $d = 1.132380 + 0.485520I$	$-0.20533 - 5.20915I$	$-2.55774 + 3.72118I$
$u = -0.273627 + 1.210650I$ $a = 0.376337 + 1.232810I$ $b = -0.055892 - 0.873986I$ $c = -0.687715 - 0.784193I$ $d = -0.901383 + 0.672173I$	$8.10965 + 4.33574I$	$3.31243 - 3.68401I$
$u = -0.273627 + 1.210650I$ $a = -0.680000 - 0.179254I$ $b = 1.163320 + 0.588782I$ $c = 0.0243773 + 0.1172880I$ $d = -0.522674 - 0.802934I$	$8.10965 + 4.33574I$	$3.31243 - 3.68401I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.273627 - 1.210650I$ $a = 0.376337 - 1.232810I$ $b = -0.055892 + 0.873986I$ $c = -0.687715 + 0.784193I$ $d = -0.901383 - 0.672173I$	$8.10965 - 4.33574I$	$3.31243 + 3.68401I$
$u = -0.273627 - 1.210650I$ $a = -0.680000 + 0.179254I$ $b = 1.163320 - 0.588782I$ $c = 0.0243773 - 0.1172880I$ $d = -0.522674 + 0.802934I$	$8.10965 - 4.33574I$	$3.31243 + 3.68401I$
$u = 0.764438 + 1.080520I$ $a = -0.29279 - 1.73056I$ $b = 1.42979 - 1.08893I$ $c = 0.371944 + 0.333066I$ $d = -0.163987 + 0.927905I$	$1.11929 - 11.51290I$	$-1.55919 + 7.44023I$
$u = 0.764438 + 1.080520I$ $a = 0.80955 + 1.63996I$ $b = -1.82005 + 1.63929I$ $c = -1.76532 + 1.05251I$ $d = -1.196120 - 0.553243I$	$1.11929 - 11.51290I$	$-1.55919 + 7.44023I$
$u = 0.764438 - 1.080520I$ $a = -0.29279 + 1.73056I$ $b = 1.42979 + 1.08893I$ $c = 0.371944 - 0.333066I$ $d = -0.163987 - 0.927905I$	$1.11929 + 11.51290I$	$-1.55919 - 7.44023I$
$u = 0.764438 - 1.080520I$ $a = 0.80955 - 1.63996I$ $b = -1.82005 - 1.63929I$ $c = -1.76532 - 1.05251I$ $d = -1.196120 + 0.553243I$	$1.11929 + 11.51290I$	$-1.55919 - 7.44023I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.215541 + 0.601634I$		
$a = 0.704776 + 0.667690I$		
$b = 1.56963 + 1.15126I$	$-2.97495 + 0.92758I$	$-6.11605 - 7.40073I$
$c = 1.60686 + 0.07009I$		
$d = 1.140500 + 0.089613I$		
$u = -0.215541 + 0.601634I$		
$a = -0.06827 - 2.46100I$		
$b = -0.303895 + 0.345281I$	$-2.97495 + 0.92758I$	$-6.11605 - 7.40073I$
$c = 1.26996 - 3.35470I$		
$d = -0.875845 + 0.206022I$		
$u = -0.215541 - 0.601634I$		
$a = 0.704776 - 0.667690I$		
$b = 1.56963 - 1.15126I$	$-2.97495 - 0.92758I$	$-6.11605 + 7.40073I$
$c = 1.60686 - 0.07009I$		
$d = 1.140500 - 0.089613I$		
$u = -0.215541 - 0.601634I$		
$a = -0.06827 + 2.46100I$		
$b = -0.303895 - 0.345281I$	$-2.97495 - 0.92758I$	$-6.11605 + 7.40073I$
$c = 1.26996 + 3.35470I$		
$d = -0.875845 - 0.206022I$		

$$\text{III. } I_3^u = \langle -u^7 - u^5 - 2u^3 + d - u, -u^7 - 2u^5 - 2u^3 + c - 2u, u^8a + 25u^8 + \dots - 28a + 13, -u^8 - 2u^7 + \dots + a^2 + a, u^9 + u^8 + \dots + u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_4 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u^7 + 2u^5 + 2u^3 + 2u \\ u^7 + u^5 + 2u^3 + u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u^5 + u \\ u^7 + u^5 + 2u^3 + u \end{pmatrix} \\ a_1 &= \begin{pmatrix} a \\ -0.0322581au^8 - 0.806452u^8 + \dots + 0.903226a - 0.419355 \end{pmatrix} \\ a_3 &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_2 &= \begin{pmatrix} 0.225806au^8 - 0.354839u^8 + \dots + 0.677419a - 0.0645161 \\ -0.225806au^8 - 1.64516u^8 + \dots + 0.322581a - 0.935484 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -0.0322581au^8 - 0.806452u^8 + \dots - 0.0967742a - 0.419355 \\ -0.0322581au^8 - 0.806452u^8 + \dots + 0.903226a - 0.419355 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u^3 \\ -u^5 - u^3 - u \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0.451613au^8 + 1.29032u^8 + \dots + 0.354839a + 0.870968 \\ 0.387097au^8 + 0.677419u^8 + \dots - 0.838710a + 0.0322581 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-4u^7 - 4u^6 - 4u^5 - 4u^4 - 8u^3 - 4u^2 - 6$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{18} + 13u^{17} + \cdots + 12u + 1$
$c_2, c_4, c_5$ $c_6, c_{12}$	$u^{18} + u^{17} + \cdots - 2u - 1$
$c_3, c_8$	$(u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1)^2$
$c_7, c_{10}$	$(u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1)^2$
$c_9$	$(u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1)^2$
$c_{11}$	$(u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{18} - 17y^{17} + \dots - 156y + 1$
$c_2, c_4, c_5$ $c_6, c_{12}$	$y^{18} - 13y^{17} + \dots - 12y + 1$
$c_3, c_8$	$(y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)^2$
$c_7, c_{10}$	$(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)^2$
$c_9$	$(y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1)^2$
$c_{11}$	$(y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.140343 + 0.966856I$		
$a = -0.085582 + 0.757267I$		
$b = 0.418870 + 0.086291I$	$1.78344 - 2.09337I$	$0.51499 + 4.16283I$
$c = -0.045155 + 1.125270I$		
$d = -0.772920 - 0.510351I$		
$u = 0.140343 + 0.966856I$		
$a = -0.27999 - 2.96236I$		
$b = 0.70313 + 1.42788I$	$1.78344 - 2.09337I$	$0.51499 + 4.16283I$
$c = -0.045155 + 1.125270I$		
$d = -0.772920 - 0.510351I$		
$u = 0.140343 - 0.966856I$		
$a = -0.085582 - 0.757267I$		
$b = 0.418870 - 0.086291I$	$1.78344 + 2.09337I$	$0.51499 - 4.16283I$
$c = -0.045155 - 1.125270I$		
$d = -0.772920 + 0.510351I$		
$u = 0.140343 - 0.966856I$		
$a = -0.27999 + 2.96236I$		
$b = 0.70313 - 1.42788I$	$1.78344 + 2.09337I$	$0.51499 - 4.16283I$
$c = -0.045155 - 1.125270I$		
$d = -0.772920 + 0.510351I$		
$u = 0.628449 + 0.875112I$		
$a = -0.739935 - 0.923677I$		
$b = -0.747999 - 1.130940I$	$-0.61694 - 2.45442I$	$-2.32792 + 2.91298I$
$c = 0.527060 + 0.163673I$		
$d = -0.141484 + 0.739668I$		
$u = 0.628449 + 0.875112I$		
$a = -1.14609 - 1.92647I$		
$b = 1.17043 - 0.94478I$	$-0.61694 - 2.45442I$	$-2.32792 + 2.91298I$
$c = 0.527060 + 0.163673I$		
$d = -0.141484 + 0.739668I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.628449 - 0.875112I$		
$a = -0.739935 + 0.923677I$		
$b = -0.747999 + 1.130940I$	$-0.61694 + 2.45442I$	$-2.32792 - 2.91298I$
$c = 0.527060 - 0.163673I$		
$d = -0.141484 - 0.739668I$		
$u = 0.628449 - 0.875112I$		
$a = -1.14609 + 1.92647I$		
$b = 1.17043 + 0.94478I$	$-0.61694 + 2.45442I$	$-2.32792 - 2.91298I$
$c = 0.527060 - 0.163673I$		
$d = -0.141484 - 0.739668I$		
$u = -0.796005 + 0.733148I$		
$a = -0.978726 + 0.854864I$		
$b = -0.42218 + 1.69219I$	$-4.37135 - 1.33617I$	$-7.28409 + 0.70175I$
$c = 1.61946 + 0.31131I$		
$d = 1.173910 + 0.391555I$		
$u = -0.796005 + 0.733148I$		
$a = 1.47462 - 1.15398I$		
$b = 1.71904 - 2.73838I$	$-4.37135 - 1.33617I$	$-7.28409 + 0.70175I$
$c = 1.61946 + 0.31131I$		
$d = 1.173910 + 0.391555I$		
$u = -0.796005 - 0.733148I$		
$a = -0.978726 - 0.854864I$		
$b = -0.42218 - 1.69219I$	$-4.37135 + 1.33617I$	$-7.28409 - 0.70175I$
$c = 1.61946 - 0.31131I$		
$d = 1.173910 - 0.391555I$		
$u = -0.796005 - 0.733148I$		
$a = 1.47462 + 1.15398I$		
$b = 1.71904 + 2.73838I$	$-4.37135 + 1.33617I$	$-7.28409 - 0.70175I$
$c = 1.61946 - 0.31131I$		
$d = 1.173910 - 0.391555I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.728966 + 0.986295I$ $a = -0.78241 + 1.38542I$ $b = 1.05246 + 1.54480I$ $c = -1.78816 - 1.28587I$ $d = -1.172470 + 0.500383I$	$-3.59813 + 7.08493I$	$-5.57680 - 5.91335I$
$u = -0.728966 + 0.986295I$ $a = 1.68173 - 1.92006I$ $b = -1.66387 - 1.99378I$ $c = -1.78816 - 1.28587I$ $d = -1.172470 + 0.500383I$	$-3.59813 + 7.08493I$	$-5.57680 - 5.91335I$
$u = -0.728966 - 0.986295I$ $a = -0.78241 - 1.38542I$ $b = 1.05246 - 1.54480I$ $c = -1.78816 + 1.28587I$ $d = -1.172470 - 0.500383I$	$-3.59813 - 7.08493I$	$-5.57680 + 5.91335I$
$u = -0.728966 - 0.986295I$ $a = 1.68173 + 1.92006I$ $b = -1.66387 + 1.99378I$ $c = -1.78816 + 1.28587I$ $d = -1.172470 - 0.500383I$	$-3.59813 - 7.08493I$	$-5.57680 + 5.91335I$
$u = 0.512358$ $a = 0.516084$ $b = 0.492057$ $c = 1.37360$ $d = 0.825933$	$-1.19845$	$-8.65230$
$u = 0.512358$ $a = -2.80331$ $b = -5.95180$ $c = 1.37360$ $d = 0.825933$	$-1.19845$	$-8.65230$

$$\text{IV. } I_4^u = \langle u^8c + 5u^8 + \dots - 27c + 10, \ 2u^8c - 2u^8 + \dots + 2c - 4, \ -u^2 + b, \ -u^2 + a - 1, \ u^9 + u^8 + \dots + u - 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_4 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} c \\ -0.0344828cu^8 - 0.172414u^8 + \dots + 0.931034c - 0.344828 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0.0344828cu^8 + 0.172414u^8 + \dots + 0.0689655c + 0.344828 \\ -0.0344828cu^8 - 0.172414u^8 + \dots + 0.931034c - 0.344828 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_2 &= \begin{pmatrix} u^6 + u^4 + 2u^2 + 1 \\ u^8 + 2u^6 + 2u^4 + 2u^2 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u^4 - u^2 - 1 \\ -u^4 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -0.172414cu^8 + 0.137931u^8 + \dots - 0.344828c + 0.275862 \\ -0.206897cu^8 - 0.0344828u^8 + \dots - 0.413793c - 0.0689655 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0.0344828cu^8 + 0.172414u^8 + \dots + 0.0689655c + 0.344828 \\ 0.0344828cu^8 + 0.172414u^8 + \dots - 0.931034c + 0.344828 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -0.758621cu^8 + 0.206897u^8 + \dots + 1.48276c - 0.586207 \\ -0.586207cu^8 + 0.0689655u^8 + \dots + 1.82759c - 0.862069 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-4u^7 - 4u^6 - 4u^5 - 4u^4 - 4u^3 - 8u^2 - 6$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$(u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1)^2$
$c_2, c_4$	$(u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1)^2$
$c_3, c_8$	$(u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1)^2$
$c_5, c_6, c_7$ $c_{10}, c_{12}$	$u^{18} + u^{17} + \dots - 2u - 1$
$c_9$	$u^{18} + 13u^{17} + \dots + 12u + 1$
$c_{11}$	$(u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1)^2$
$c_2, c_4$	$(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)^2$
$c_3, c_8$	$(y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)^2$
$c_5, c_6, c_7$ $c_{10}, c_{12}$	$y^{18} - 13y^{17} + \dots - 12y + 1$
$c_9$	$y^{18} - 17y^{17} + \dots - 156y + 1$
$c_{11}$	$(y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.140343 + 0.966856I$		
$a = 0.084886 + 0.271383I$		
$b = -0.915114 + 0.271383I$	$1.78344 - 2.09337I$	$0.51499 + 4.16283I$
$c = 0.312641 - 0.476170I$		
$d = -0.535620 + 0.576021I$		
$u = 0.140343 + 0.966856I$		
$a = 0.084886 + 0.271383I$		
$b = -0.915114 + 0.271383I$	$1.78344 - 2.09337I$	$0.51499 + 4.16283I$
$c = 1.74136 - 0.05336I$		
$d = 1.308540 - 0.065670I$		
$u = 0.140343 - 0.966856I$		
$a = 0.084886 - 0.271383I$		
$b = -0.915114 - 0.271383I$	$1.78344 + 2.09337I$	$0.51499 - 4.16283I$
$c = 0.312641 + 0.476170I$		
$d = -0.535620 - 0.576021I$		
$u = 0.140343 - 0.966856I$		
$a = 0.084886 - 0.271383I$		
$b = -0.915114 - 0.271383I$	$1.78344 + 2.09337I$	$0.51499 - 4.16283I$
$c = 1.74136 + 0.05336I$		
$d = 1.308540 + 0.065670I$		
$u = 0.628449 + 0.875112I$		
$a = 0.629127 + 1.099930I$		
$b = -0.370873 + 1.099930I$	$-0.61694 - 2.45442I$	$-2.32792 + 2.91298I$
$c = 1.68962 - 0.24481I$		
$d = 1.253840 - 0.303492I$		
$u = 0.628449 + 0.875112I$		
$a = 0.629127 + 1.099930I$		
$b = -0.370873 + 1.099930I$	$-0.61694 - 2.45442I$	$-2.32792 + 2.91298I$
$c = -1.66618 + 1.71382I$		
$d = -1.112360 - 0.436175I$		

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.628449 - 0.875112I$		
$a = 0.629127 - 1.099930I$		
$b = -0.370873 - 1.099930I$	$-0.61694 + 2.45442I$	$-2.32792 - 2.91298I$
$c = 1.68962 + 0.24481I$		
$d = 1.253840 + 0.303492I$		
$u = 0.628449 - 0.875112I$		
$a = 0.629127 - 1.099930I$		
$b = -0.370873 - 1.099930I$	$-0.61694 + 2.45442I$	$-2.32792 - 2.91298I$
$c = -1.66618 - 1.71382I$		
$d = -1.112360 + 0.436175I$		
$u = -0.796005 + 0.733148I$		
$a = 1.09612 - 1.16718I$		
$b = 0.096118 - 1.167180I$	$-4.37135 - 1.33617I$	$-7.28409 + 0.70175I$
$c = 0.669579 - 0.290859I$		
$d = 0.035822 - 0.749326I$		
$u = -0.796005 + 0.733148I$		
$a = 1.09612 - 1.16718I$		
$b = 0.096118 - 1.167180I$	$-4.37135 - 1.33617I$	$-7.28409 + 0.70175I$
$c = -2.42920 - 1.72243I$		
$d = -1.209730 + 0.357771I$		
$u = -0.796005 - 0.733148I$		
$a = 1.09612 + 1.16718I$		
$b = 0.096118 + 1.167180I$	$-4.37135 + 1.33617I$	$-7.28409 - 0.70175I$
$c = 0.669579 + 0.290859I$		
$d = 0.035822 + 0.749326I$		
$u = -0.796005 - 0.733148I$		
$a = 1.09612 + 1.16718I$		
$b = 0.096118 + 1.167180I$	$-4.37135 + 1.33617I$	$-7.28409 - 0.70175I$
$c = -2.42920 + 1.72243I$		
$d = -1.209730 - 0.357771I$		

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.728966 + 0.986295I$		
$a = 0.55861 - 1.43795I$		
$b = -0.44139 - 1.43795I$	$-3.59813 + 7.08493I$	$-5.57680 - 5.91335I$
$c = 0.444675 - 0.276867I$		
$d = -0.138557 - 0.857281I$		
$u = -0.728966 + 0.986295I$		
$a = 0.55861 - 1.43795I$		
$b = -0.44139 - 1.43795I$	$-3.59813 + 7.08493I$	$-5.57680 - 5.91335I$
$c = 1.73366 + 0.29163I$		
$d = 1.311030 + 0.356898I$		
$u = -0.728966 - 0.986295I$		
$a = 0.55861 + 1.43795I$		
$b = -0.44139 + 1.43795I$	$-3.59813 - 7.08493I$	$-5.57680 + 5.91335I$
$c = 0.444675 + 0.276867I$		
$d = -0.138557 + 0.857281I$		
$u = -0.728966 - 0.986295I$		
$a = 0.55861 + 1.43795I$		
$b = -0.44139 + 1.43795I$	$-3.59813 - 7.08493I$	$-5.57680 + 5.91335I$
$c = 1.73366 - 0.29163I$		
$d = 1.311030 - 0.356898I$		
$u = 0.512358$		
$a = 1.26251$		
$b = 0.262511$	$-1.19845$	$-8.65230$
$c = 1.06355$		
$d = 0.285873$		
$u = 0.512358$		
$a = 1.26251$		
$b = 0.262511$	$-1.19845$	$-8.65230$
$c = -10.0559$		
$d = -1.11181$		

$$\mathbf{V} \cdot I_5^u = \langle -u^7 - u^5 - 2u^3 + d - u, -u^7 - 2u^5 - 2u^3 + c - 2u, -u^2 + b, -u^2 + a - 1, u^9 + u^8 + \dots + u - 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_4 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u^7 + 2u^5 + 2u^3 + 2u \\ u^7 + u^5 + 2u^3 + u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u^5 + u \\ u^7 + u^5 + 2u^3 + u \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_2 &= \begin{pmatrix} u^6 + u^4 + 2u^2 + 1 \\ u^8 + 2u^6 + 2u^4 + 2u^2 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u^4 - u^2 - 1 \\ -u^4 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u^3 \\ -u^5 - u^3 - u \end{pmatrix} \\ a_6 &= \begin{pmatrix} -u^8 - u^6 - u^4 + 1 \\ -u^8 - u^7 - u^6 - 2u^5 - u^4 - 2u^3 - 2u + 1 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-4u^7 - 4u^6 - 4u^5 - 4u^4 - 8u^3 - 4u^2 - 6$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_9$	$u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1$
$c_2, c_4, c_5$ $c_6, c_7, c_{10}$ $c_{12}$	$u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1$
$c_3, c_8$	$u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1$
$c_{11}$	$u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_9$	$y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1$
$c_2, c_4, c_5$ $c_6, c_7, c_{10}$ $c_{12}$	$y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1$
$c_3, c_8$	$y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1$
$c_{11}$	$y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.140343 + 0.966856I$ $a = 0.084886 + 0.271383I$ $b = -0.915114 + 0.271383I$ $c = -0.045155 + 1.125270I$ $d = -0.772920 - 0.510351I$	$\sqrt{-1}(0.140343 + 0.966856I + \sqrt{-1}(0.084886 + 0.271383I)CS)$	$0.51499 + 4.16283I$
$u = 0.140343 - 0.966856I$ $a = 0.084886 - 0.271383I$ $b = -0.915114 - 0.271383I$ $c = -0.045155 - 1.125270I$ $d = -0.772920 + 0.510351I$	$\sqrt{-1}(0.140343 - 0.966856I + \sqrt{-1}(0.084886 - 0.271383I)CS)$	$0.51499 - 4.16283I$
$u = 0.628449 + 0.875112I$ $a = 0.629127 + 1.099930I$ $b = -0.370873 + 1.099930I$ $c = 0.527060 + 0.163673I$ $d = -0.141484 + 0.739668I$	$\sqrt{-1}(0.628449 + 0.875112I + \sqrt{-1}(0.629127 + 1.099930I)CS)$	$-2.32792 + 2.91298I$
$u = 0.628449 - 0.875112I$ $a = 0.629127 - 1.099930I$ $b = -0.370873 - 1.099930I$ $c = 0.527060 - 0.163673I$ $d = -0.141484 - 0.739668I$	$\sqrt{-1}(0.628449 - 0.875112I + \sqrt{-1}(0.629127 - 1.099930I)CS)$	$-2.32792 - 2.91298I$
$u = -0.796005 + 0.733148I$ $a = 1.09612 - 1.16718I$ $b = 0.096118 - 1.167180I$ $c = 1.61946 + 0.31131I$ $d = 1.173910 + 0.391555I$	$\sqrt{-1}(-0.796005 + 0.733148I + \sqrt{-1}(1.09612 - 1.16718I)CS)$	$-7.28409 + 0.70175I$
$u = -0.796005 - 0.733148I$ $a = 1.09612 + 1.16718I$ $b = 0.096118 + 1.167180I$ $c = 1.61946 - 0.31131I$ $d = 1.173910 - 0.391555I$	$\sqrt{-1}(-0.796005 - 0.733148I + \sqrt{-1}(1.09612 + 1.16718I)CS)$	$-7.28409 - 0.70175I$

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.728966 + 0.986295I$		
$a = 0.55861 - 1.43795I$		
$b = -0.44139 - 1.43795I$	$-3.59813 + 7.08493I$	$-5.57680 - 5.91335I$
$c = -1.78816 - 1.28587I$		
$d = -1.172470 + 0.500383I$		
$u = -0.728966 - 0.986295I$		
$a = 0.55861 + 1.43795I$		
$b = -0.44139 + 1.43795I$	$-3.59813 - 7.08493I$	$-5.57680 + 5.91335I$
$c = -1.78816 + 1.28587I$		
$d = -1.172470 - 0.500383I$		
$u = 0.512358$		
$a = 1.26251$		
$b = 0.262511$	$-1.19845$	$-8.65230$
$c = 1.37360$		
$d = 0.825933$		

$$\text{VI. } I_1^v = \langle a, d-1, c-a-1, b-1, v+1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -12

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_7$ $c_9$	$u - 1$
$c_3, c_5, c_6$ $c_8, c_{11}, c_{12}$	$u$
$c_4, c_{10}$	$u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_7, c_9, c_{10}$	$y - 1$
$c_3, c_5, c_6$ $c_8, c_{11}, c_{12}$	$y$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -1.00000$		
$a = 0$		
$b = 1.00000$	-3.28987	-12.0000
$c = 1.00000$		
$d = 1.00000$		

$$\text{VII. } I_2^v = \langle a, d, c - 1, b + 1, v - 1 \rangle$$

(i) **Arc colorings**

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes = 0**

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_{12}$	$u - 1$
$c_3, c_7, c_8$ $c_9, c_{10}, c_{11}$	$u$
$c_4, c_5, c_6$	$u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_5, c_6, c_{12}$	$y - 1$
$c_3, c_7, c_8$ $c_9, c_{10}, c_{11}$	$y$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 1.00000$		
$a = 0$		
$b = -1.00000$	0	0
$c = 1.00000$		
$d = 0$		

$$\text{VIII. } I_3^v = \langle c, d-1, b, a-1, v-1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_8, c_{11}$	$u$
$c_5, c_6, c_7$ $c_9$	$u - 1$
$c_{10}, c_{12}$	$u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_8, c_{11}$	$y$
$c_5, c_6, c_7$ $c_9, c_{10}, c_{12}$	$y - 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 1.00000$		
$a = 1.00000$		
$b = 0$	0	0
$c = 0$		
$d = 1.00000$		

$$\text{IX. } I_4^v = \langle c, d - 1, av + c - v - 1, bv + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a \\ -a + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a + v \\ -a + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -a \\ a - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} a + 1 \\ -a \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $a^2 + v^2 - 2a - 7$

(iv) u-Polynomials at the component : It cannot be defined for a positive dimension component.

(v) Riley Polynomials at the component : It cannot be defined for a positive dimension component.

**(iv) Complex Volumes and Cusp Shapes**

Solution to $I_4^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = \dots$		
$a = \dots$		
$b = \dots$	-1.64493	$-6.78092 + 0.05196I$
$c = \dots$		
$d = \dots$		

## X. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_9$	$u(u-1)^2(u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1)^3$ $\cdot (u^{18} + 13u^{17} + \dots + 12u + 1)(u^{22} + 11u^{21} + \dots + 40u + 16)$ $\cdot (u^{25} + 12u^{24} + \dots + 3u + 1)$
$c_2, c_7$	$u(u-1)^2(u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1)^3$ $\cdot (u^{18} + u^{17} + \dots - 2u - 1)(u^{22} - u^{21} + \dots - 4u + 4)$ $\cdot (u^{25} - 2u^{24} + \dots - u + 1)$
$c_3, c_8$	$u^3(u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1)^5$ $\cdot (u^{11} + 3u^{10} + 6u^9 + 7u^8 + 7u^7 + 3u^6 - 2u^5 - 8u^4 - 7u^3 - 5u^2 - 2u - 2)^2$ $\cdot (u^{25} - 2u^{24} + \dots - 16u + 8)$
$c_4, c_{10}$	$u(u+1)^2(u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1)^3$ $\cdot (u^{18} + u^{17} + \dots - 2u - 1)(u^{22} - u^{21} + \dots - 4u + 4)$ $\cdot (u^{25} - 2u^{24} + \dots - u + 1)$
$c_5, c_6, c_{12}$	$u(u-1)(u+1)(u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1)$ $\cdot (u^{11} + u^{10} - 5u^9 - 4u^8 + 9u^7 + 4u^6 - 5u^5 + 3u^4 - 3u^3 - 5u^2 + 3u - 1)^2$ $\cdot ((u^{18} + u^{17} + \dots - 2u - 1)^2)(u^{25} + 2u^{24} + \dots + 8u + 4)$
$c_{11}$	$u^3(u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1)^5$ $\cdot ((u^{11} - 3u^{10} + \dots - 16u + 4)^2)(u^{25} - 6u^{24} + \dots + 64u + 64)$

## XI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_9$	$y(y - 1)^2(y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1)^3$ $\cdot (y^{18} - 17y^{17} + \dots - 156y + 1)(y^{22} - 3y^{21} + \dots - 544y + 256)$ $\cdot (y^{25} + 8y^{24} + \dots - 13y - 1)$
$c_2, c_4, c_7$ $c_{10}$	$y(y - 1)^2(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)^3$ $\cdot (y^{18} - 13y^{17} + \dots - 12y + 1)(y^{22} - 11y^{21} + \dots - 40y + 16)$ $\cdot (y^{25} - 12y^{24} + \dots + 3y - 1)$
$c_3, c_8$	$y^3(y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)^5$ $\cdot ((y^{11} + 3y^{10} + \dots - 16y - 4)^2)(y^{25} + 6y^{24} + \dots + 64y - 64)$
$c_5, c_6, c_{12}$	$y(y - 1)^2(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)$ $\cdot ((y^{11} - 11y^{10} + \dots - y - 1)^2)(y^{18} - 13y^{17} + \dots - 12y + 1)^2$ $\cdot (y^{25} - 22y^{24} + \dots + 88y - 16)$
$c_{11}$	$y^3(y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1)^5$ $\cdot ((y^{11} + 7y^{10} + \dots + 24y - 16)^2)(y^{25} + 14y^{24} + \dots + 43008y - 4096)$