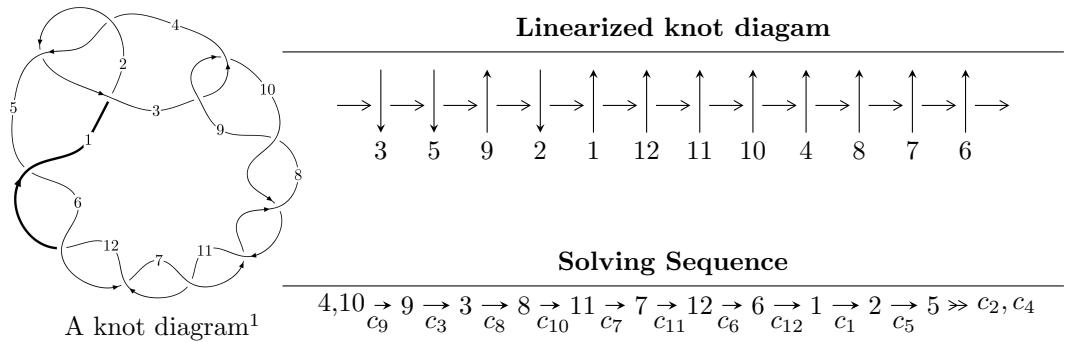


$12a_{0169}$  ( $K12a_{0169}$ )



Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$

$$I_1^u = \langle u^{24} - u^{23} + \cdots - 2u^2 + 1 \rangle$$

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 24 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle u^{24} - u^{23} + \cdots - 2u^2 + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned}
a_4 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\
a_{10} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\
a_9 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\
a_3 &= \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix} \\
a_8 &= \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix} \\
a_{11} &= \begin{pmatrix} u^4 - u^2 + 1 \\ -u^4 \end{pmatrix} \\
a_7 &= \begin{pmatrix} -u^6 + u^4 - 2u^2 + 1 \\ u^6 + u^2 \end{pmatrix} \\
a_{12} &= \begin{pmatrix} u^8 - u^6 + 3u^4 - 2u^2 + 1 \\ -u^8 - 2u^4 \end{pmatrix} \\
a_6 &= \begin{pmatrix} -u^{10} + u^8 - 4u^6 + 3u^4 - 3u^2 + 1 \\ u^{10} + 3u^6 + u^2 \end{pmatrix} \\
a_1 &= \begin{pmatrix} u^{12} - u^{10} + 5u^8 - 4u^6 + 6u^4 - 3u^2 + 1 \\ -u^{12} - 4u^8 - 3u^4 \end{pmatrix} \\
a_2 &= \begin{pmatrix} u^{16} - u^{14} + 7u^{12} - 6u^{10} + 15u^8 - 10u^6 + 10u^4 - 4u^2 + 1 \\ u^{18} - 2u^{16} + 7u^{14} - 12u^{12} + 15u^{10} - 20u^8 + 10u^6 - 8u^4 + u^2 \end{pmatrix} \\
a_5 &= \begin{pmatrix} -u^{14} + u^{12} - 6u^{10} + 5u^8 - 10u^6 + 6u^4 - 4u^2 + 1 \\ u^{14} + 5u^{10} + 6u^6 + u^2 \end{pmatrix}
\end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$\begin{aligned}
&= -4u^{23} + 8u^{21} - 4u^{20} - 44u^{19} + 4u^{18} + 72u^{17} - 32u^{16} - 176u^{15} + 28u^{14} + 228u^{13} - 88u^{12} - \\
&\quad 308u^{11} + 64u^{10} + 296u^9 - 96u^8 - 220u^7 + 52u^6 + 136u^5 - 28u^4 - 44u^3 + 4u^2 + 16u + 6
\end{aligned}$$

**(iv) u-Polynomials at the component**

| Crossings  | u-Polynomials at each crossing        |
|--|---------------------------------------|
| $c_1$  | $u^{24} + 15u^{23} + \cdots + 4u + 1$ |
| $c_2, c_4$   | $u^{24} - u^{23} + \cdots - 4u + 1$   |
| $c_3, c_9$   | $u^{24} - u^{23} + \cdots - 2u^2 + 1$ |
| $c_5, c_6, c_7$<br>$c_8, c_{10}, c_{11}$<br>$c_{12}$ | $u^{24} - 3u^{23} + \cdots - 4u + 1$  |

**(v) Riley Polynomials at the component**

| Crossings  | Riley Polynomials at each crossing     |
|--|--|
| $c_1$  | $y^{24} - 11y^{23} + \cdots - 20y + 1$ |
| $c_2, c_4$   | $y^{24} - 15y^{23} + \cdots - 4y + 1$  |
| $c_3, c_9$   | $y^{24} - 3y^{23} + \cdots - 4y + 1$   |
| $c_5, c_6, c_7$<br>$c_8, c_{10}, c_{11}$<br>$c_{12}$ | $y^{24} + 37y^{23} + \cdots + 12y + 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.818053 + 0.585237I$  | $-4.34966 + 5.76332I$                 | $-0.83619 - 8.32312I$ |
| $u = 0.818053 - 0.585237I$  | $-4.34966 - 5.76332I$                 | $-0.83619 + 8.32312I$ |
| $u = 0.629900 + 0.676291I$  | $-4.99244 - 1.16181I$                 | $-3.45696 + 0.66594I$ |
| $u = 0.629900 - 0.676291I$  | $-4.99244 + 1.16181I$                 | $-3.45696 - 0.66594I$ |
| $u = -0.703557 + 0.542696I$ | $-1.64192 - 2.01575I$                 | $2.27145 + 4.63931I$  |
| $u = -0.703557 - 0.542696I$ | $-1.64192 + 2.01575I$                 | $2.27145 - 4.63931I$  |
| $u = 0.865592 + 0.818505I$  | $-9.02499 + 3.00763I$                 | $0.51260 - 2.75465I$  |
| $u = 0.865592 - 0.818505I$  | $-9.02499 - 3.00763I$                 | $0.51260 + 2.75465I$  |
| $u = -0.748084 + 0.274295I$ | $-0.07774 - 3.02933I$                 | $5.70852 + 9.26987I$  |
| $u = -0.748084 - 0.274295I$ | $-0.07774 + 3.02933I$                 | $5.70852 - 9.26987I$  |
| $u = -0.844876 + 0.858831I$ | $-12.84350 + 1.46852I$                | $-3.16556 - 0.66920I$ |
| $u = -0.844876 - 0.858831I$ | $-12.84350 - 1.46852I$                | $-3.16556 + 0.66920I$ |
| $u = -0.908318 + 0.819726I$ | $-12.6233 - 7.6239I$                  | $-2.60069 + 6.03151I$ |
| $u = -0.908318 - 0.819726I$ | $-12.6233 + 7.6239I$                  | $-2.60069 - 6.03151I$ |
| $u = 0.662055 + 0.056751I$  | $0.927331 + 0.040320I$                | $11.54599 - 0.37990I$ |
| $u = 0.662055 - 0.056751I$  | $0.927331 - 0.040320I$                | $11.54599 + 0.37990I$ |
| $u = -0.966596 + 0.956593I$ | $18.1029 - 3.5079I$                   | $0.10153 + 2.15218I$  |
| $u = -0.966596 - 0.956593I$ | $18.1029 + 3.5079I$                   | $0.10153 - 2.15218I$  |
| $u = 0.962124 + 0.965092I$  | $14.0584 - 1.6220I$                   | $-3.03720 + 0.65264I$ |
| $u = 0.962124 - 0.965092I$  | $14.0584 + 1.6220I$                   | $-3.03720 - 0.65264I$ |
| $u = 0.975953 + 0.955750I$  | $14.1060 + 8.6639I$                   | $-2.94392 - 4.94788I$ |
| $u = 0.975953 - 0.955750I$  | $14.1060 - 8.6639I$                   | $-2.94392 + 4.94788I$ |
| $u = -0.242249 + 0.453783I$ | $-1.64107 + 0.52371I$                 | $-4.09957 - 0.43757I$ |
| $u = -0.242249 - 0.453783I$ | $-1.64107 - 0.52371I$                 | $-4.09957 + 0.43757I$ |

## II. u-Polynomials

| Crossings  | u-Polynomials at each crossing        |
|--|---------------------------------------|
| $c_1$  | $u^{24} + 15u^{23} + \cdots + 4u + 1$ |
| $c_2, c_4$   | $u^{24} - u^{23} + \cdots - 4u + 1$   |
| $c_3, c_9$   | $u^{24} - u^{23} + \cdots - 2u^2 + 1$ |
| $c_5, c_6, c_7$<br>$c_8, c_{10}, c_{11}$<br>$c_{12}$ | $u^{24} - 3u^{23} + \cdots - 4u + 1$  |

### III. Riley Polynomials

| Crossings  | Riley Polynomials at each crossing     |
|--|--|
| $c_1$  | $y^{24} - 11y^{23} + \cdots - 20y + 1$ |
| $c_2, c_4$   | $y^{24} - 15y^{23} + \cdots - 4y + 1$  |
| $c_3, c_9$   | $y^{24} - 3y^{23} + \cdots - 4y + 1$   |
| $c_5, c_6, c_7$<br>$c_8, c_{10}, c_{11}$<br>$c_{12}$ | $y^{24} + 37y^{23} + \cdots + 12y + 1$ |