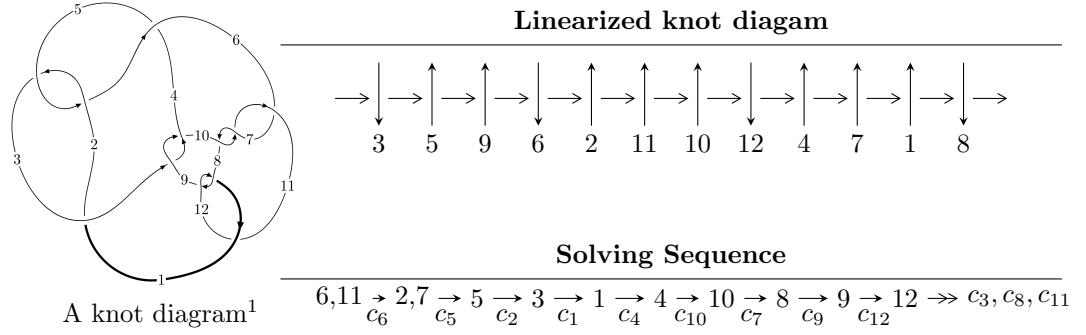


## $12a_{0177}$ ( $K12a_{0177}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle 7.32498 \times 10^{64}u^{73} + 8.66991 \times 10^{64}u^{72} + \dots + 6.16277 \times 10^{65}b - 4.73818 \times 10^{66}, \\
 &\quad - 1.00235 \times 10^{67}u^{73} - 1.65925 \times 10^{67}u^{72} + \dots + 2.09534 \times 10^{67}a + 3.92221 \times 10^{68}, \\
 &\quad u^{74} + 3u^{73} + \dots + 241u + 34 \rangle \\
 I_2^u &= \langle -u^{12} - 4u^{10} + 2u^9 - 6u^8 + 6u^7 - 6u^6 + 6u^5 - 5u^4 + 2u^3 - 2u^2 + b, \\
 &\quad u^{10} + 3u^8 - 2u^7 + 4u^6 - 4u^5 + 5u^4 - 4u^3 + 3u^2 + a - 2u + 1, u^{27} + 9u^{25} + \dots + u - 1 \rangle \\
 I_3^u &= \langle u^2a + u^2 + b + a + 1, 2u^3a + 4u^2a + 5u^3 + 4a^2 + 6au + 6u^2 + 14a + 13u + 15, u^4 + u^3 + 3u^2 + 2u + 1 \rangle \\
 I_4^u &= \langle -a^2 - 2au + b + 2a + 2u - 1, a^4 + 3a^3u - 4a^3 - 9a^2u + 5a^2 + 11au - 2a - 5u + 1, u^2 + 1 \rangle
 \end{aligned}$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 117 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 7.32 \times 10^{64} u^{73} + 8.67 \times 10^{64} u^{72} + \dots + 6.16 \times 10^{65} b - 4.74 \times 10^{66}, -1.00 \times 10^{67} u^{73} - 1.66 \times 10^{67} u^{72} + \dots + 2.10 \times 10^{67} a + 3.92 \times 10^{68}, u^{74} + 3u^{73} + \dots + 241u + 34 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} 0.478370u^{73} + 0.791874u^{72} + \dots - 33.3429u - 18.7187 \\ -0.118859u^{73} - 0.140682u^{72} + \dots + 21.7836u + 7.68839 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -1.54482u^{73} - 3.80613u^{72} + \dots - 519.075u - 88.4779 \\ 0.760024u^{73} + 1.86639u^{72} + \dots + 269.188u + 47.8263 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0.570211u^{73} + 1.31506u^{72} + \dots + 144.190u + 26.0532 \\ 0.0702357u^{73} + 0.201359u^{72} + \dots - 19.1668u - 9.42275 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 0.737803u^{73} + 1.93511u^{72} + \dots + 256.366u + 47.4633 \\ 0.565372u^{73} + 1.35960u^{72} + \dots + 138.390u + 21.9622 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -0.784791u^{73} - 1.93974u^{72} + \dots - 249.887u - 40.6516 \\ 0.760024u^{73} + 1.86639u^{72} + \dots + 269.188u + 47.8263 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u \\ u^3 + u \end{pmatrix} \\ a_8 &= \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1.26077u^{73} + 3.03039u^{72} + \dots + 376.302u + 61.5916 \\ -1.04521u^{73} - 2.74727u^{72} + \dots - 382.989u - 69.8736 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 1.61959u^{73} + 4.23678u^{72} + \dots + 593.454u + 111.477 \\ 0.435515u^{73} + 0.883326u^{72} + \dots + 44.5571u + 0.814681 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $0.202194u^{73} + 0.134817u^{72} + \dots - 112.657u - 17.5239$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^{74} + 24u^{73} + \cdots - 225u + 16$
$c_2, c_5$	$u^{74} + 4u^{73} + \cdots + 35u + 4$
$c_3, c_9$	$u^{74} - 2u^{73} + \cdots - 2560u + 2048$
$c_6, c_7, c_{10}$	$u^{74} + 3u^{73} + \cdots + 241u + 34$
$c_8, c_{12}$	$u^{74} + 3u^{73} + \cdots + 243u + 34$
$c_{11}$	$u^{74} - 31u^{73} + \cdots - 29555u + 1156$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{74} + 56y^{73} + \cdots + 227743y + 256$
$c_2, c_5$	$y^{74} + 24y^{73} + \cdots - 225y + 16$
$c_3, c_9$	$y^{74} - 40y^{73} + \cdots - 36438016y + 4194304$
$c_6, c_7, c_{10}$	$y^{74} + 75y^{73} + \cdots + 36099y + 1156$
$c_8, c_{12}$	$y^{74} + 31y^{73} + \cdots + 29555y + 1156$
$c_{11}$	$y^{74} + 35y^{73} + \cdots + 11195711y + 1336336$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.944775 + 0.259860I$		
$a = 2.05390 - 0.30574I$	$5.92126 - 12.56140I$	0
$b = -0.743584 + 1.028880I$		
$u = -0.944775 - 0.259860I$		
$a = 2.05390 + 0.30574I$	$5.92126 + 12.56140I$	0
$b = -0.743584 - 1.028880I$		
$u = -0.921296 + 0.218016I$		
$a = 1.35216 + 1.03131I$	$6.95372 - 6.59603I$	0
$b = -0.857448 - 0.692852I$		
$u = -0.921296 - 0.218016I$		
$a = 1.35216 - 1.03131I$	$6.95372 + 6.59603I$	0
$b = -0.857448 + 0.692852I$		
$u = 0.701992 + 0.812926I$		
$a = 0.745443 - 0.467058I$	$2.32200 - 1.76357I$	0
$b = -0.711125 + 0.915757I$		
$u = 0.701992 - 0.812926I$		
$a = 0.745443 + 0.467058I$	$2.32200 + 1.76357I$	0
$b = -0.711125 - 0.915757I$		
$u = 0.633453 + 0.888233I$		
$a = 1.49188 - 0.19124I$	$2.61817 + 3.75049I$	0
$b = -0.734625 - 0.820944I$		
$u = 0.633453 - 0.888233I$		
$a = 1.49188 + 0.19124I$	$2.61817 - 3.75049I$	0
$b = -0.734625 + 0.820944I$		
$u = -0.784151 + 0.296355I$		
$a = -0.632018 + 0.069860I$	$-0.13573 - 6.54057I$	$4.00000 + 8.07439I$
$b = 0.190621 - 1.095890I$		
$u = -0.784151 - 0.296355I$		
$a = -0.632018 - 0.069860I$	$-0.13573 + 6.54057I$	$4.00000 - 8.07439I$
$b = 0.190621 + 1.095890I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.672265 + 0.482118I$	$-1.54681 + 2.12225I$	$0. - 3.10049I$
$a = 1.222840 + 0.018497I$		
$b = -0.042473 - 0.877998I$		
$u = 0.672265 - 0.482118I$	$-1.54681 - 2.12225I$	$0. + 3.10049I$
$a = 1.222840 - 0.018497I$		
$b = -0.042473 + 0.877998I$		
$u = -0.126360 + 1.199890I$	$6.07360 + 1.90106I$	$0$
$a = 1.040200 + 0.208918I$		
$b = -0.877658 - 0.958922I$		
$u = -0.126360 - 1.199890I$	$6.07360 - 1.90106I$	$0$
$a = 1.040200 - 0.208918I$		
$b = -0.877658 + 0.958922I$		
$u = 0.114557 + 0.782746I$	$-1.59283 + 1.64325I$	$-3.33878 - 4.86673I$
$a = 0.659521 + 0.464671I$		
$b = 0.177178 + 0.779440I$		
$u = 0.114557 - 0.782746I$	$-1.59283 - 1.64325I$	$-3.33878 + 4.86673I$
$a = 0.659521 - 0.464671I$		
$b = 0.177178 - 0.779440I$		
$u = -0.164572 + 1.204940I$	$6.31241 - 4.67571I$	$0$
$a = 1.227960 - 0.069637I$		
$b = -0.910018 + 0.882320I$		
$u = -0.164572 - 1.204940I$	$6.31241 + 4.67571I$	$0$
$a = 1.227960 + 0.069637I$		
$b = -0.910018 - 0.882320I$		
$u = 0.742648 + 0.206519I$	$2.97428 + 6.29652I$	$7.50844 - 6.68334I$
$a = -2.53072 - 1.14776I$		
$b = 0.716663 + 0.940041I$		
$u = 0.742648 - 0.206519I$	$2.97428 - 6.29652I$	$7.50844 + 6.68334I$
$a = -2.53072 + 1.14776I$		
$b = 0.716663 - 0.940041I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.717121 + 0.158800I$		
$a = -1.225590 + 0.380080I$	$3.98068 - 3.64075I$	$11.59299 + 4.80389I$
$b = 0.731356 - 0.145206I$		
$u = -0.717121 - 0.158800I$		
$a = -1.225590 - 0.380080I$	$3.98068 + 3.64075I$	$11.59299 - 4.80389I$
$b = 0.731356 + 0.145206I$		
$u = 0.668164 + 0.154518I$		
$a = -2.39850 + 1.57549I$	$3.43591 + 0.73188I$	$9.08233 - 1.08851I$
$b = 0.744333 - 0.790073I$		
$u = 0.668164 - 0.154518I$		
$a = -2.39850 - 1.57549I$	$3.43591 - 0.73188I$	$9.08233 + 1.08851I$
$b = 0.744333 + 0.790073I$		
$u = -0.129344 + 1.322690I$		
$a = -0.479899 - 0.769382I$	$-3.18435 + 0.63847I$	0
$b = 0.779061 + 0.657588I$		
$u = -0.129344 - 1.322690I$		
$a = -0.479899 + 0.769382I$	$-3.18435 - 0.63847I$	0
$b = 0.779061 - 0.657588I$		
$u = 0.168573 + 1.321110I$		
$a = -0.405207 + 0.035030I$	$-2.90837 + 2.42803I$	0
$b = 0.761529 + 0.328332I$		
$u = 0.168573 - 1.321110I$		
$a = -0.405207 - 0.035030I$	$-2.90837 - 2.42803I$	0
$b = 0.761529 - 0.328332I$		
$u = -0.619119 + 0.176034I$		
$a = 0.73745 + 1.54337I$	$9.31962 + 1.94114I$	$12.61811 - 2.00223I$
$b = -0.846329 - 0.820584I$		
$u = -0.619119 - 0.176034I$		
$a = 0.73745 - 1.54337I$	$9.31962 - 1.94114I$	$12.61811 + 2.00223I$
$b = -0.846329 + 0.820584I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.080972 + 1.372850I$		
$a = -0.741831 - 0.900405I$	$-5.16943 - 2.42403I$	0
$b = 0.543374 - 1.089860I$		
$u = 0.080972 - 1.372850I$		
$a = -0.741831 + 0.900405I$	$-5.16943 + 2.42403I$	0
$b = 0.543374 + 1.089860I$		
$u = -0.195770 + 1.365850I$		
$a = -1.82469 - 0.71360I$	$-4.22851 - 4.92303I$	0
$b = 0.693804 - 1.006320I$		
$u = -0.195770 - 1.365850I$		
$a = -1.82469 + 0.71360I$	$-4.22851 + 4.92303I$	0
$b = 0.693804 + 1.006320I$		
$u = 0.264758 + 1.357650I$		
$a = -0.734404 + 0.940199I$	$-1.35573 + 4.11982I$	0
$b = 0.834563 - 0.756749I$		
$u = 0.264758 - 1.357650I$		
$a = -0.734404 - 0.940199I$	$-1.35573 - 4.11982I$	0
$b = 0.834563 + 0.756749I$		
$u = -0.287291 + 1.361710I$		
$a = -0.635754 - 0.259327I$	$-0.83655 - 7.27459I$	0
$b = 0.855562 - 0.209147I$		
$u = -0.287291 - 1.361710I$		
$a = -0.635754 + 0.259327I$	$-0.83655 + 7.27459I$	0
$b = 0.855562 + 0.209147I$		
$u = -0.221792 + 1.376420I$		
$a = -0.337020 + 0.630518I$	$-3.81286 - 2.52146I$	0
$b = 0.469813 + 1.138480I$		
$u = -0.221792 - 1.376420I$		
$a = -0.337020 - 0.630518I$	$-3.81286 + 2.52146I$	0
$b = 0.469813 - 1.138480I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.545845 + 0.228098I$		
$a = 2.57811 + 0.51294I$	$8.90634 - 4.18645I$	$12.18887 + 3.45540I$
$b = -0.800509 + 0.954675I$		
$u = -0.545845 - 0.228098I$		
$a = 2.57811 - 0.51294I$	$8.90634 + 4.18645I$	$12.18887 - 3.45540I$
$b = -0.800509 - 0.954675I$		
$u = -0.545719 + 0.215154I$		
$a = -1.73543 - 0.37199I$	$1.244170 + 0.336310I$	$9.44086 + 1.14384I$
$b = 0.421570 + 1.033690I$		
$u = -0.545719 - 0.215154I$		
$a = -1.73543 + 0.37199I$	$1.244170 - 0.336310I$	$9.44086 - 1.14384I$
$b = 0.421570 - 1.033690I$		
$u = 0.29962 + 1.38522I$		
$a = -1.98098 + 0.41163I$	$-2.08327 + 10.07100I$	0
$b = 0.755945 + 0.990941I$		
$u = 0.29962 - 1.38522I$		
$a = -1.98098 - 0.41163I$	$-2.08327 - 10.07100I$	0
$b = 0.755945 - 0.990941I$		
$u = 0.07395 + 1.42707I$		
$a = 0.701838 - 0.037664I$	$-5.46924 + 2.64105I$	0
$b = -0.569204 + 0.123347I$		
$u = 0.07395 - 1.42707I$		
$a = 0.701838 + 0.037664I$	$-5.46924 - 2.64105I$	0
$b = -0.569204 - 0.123347I$		
$u = 0.21382 + 1.43929I$		
$a = -0.487788 + 1.212470I$	$-7.79078 + 4.88573I$	0
$b = 0.120316 + 1.133060I$		
$u = 0.21382 - 1.43929I$		
$a = -0.487788 - 1.212470I$	$-7.79078 - 4.88573I$	0
$b = 0.120316 - 1.133060I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.31083 + 1.42891I$		
$a = -0.828824 - 0.998794I$	$-5.64512 - 10.50590I$	0
$b = 0.177740 - 1.175180I$		
$u = -0.31083 - 1.42891I$		
$a = -0.828824 + 0.998794I$	$-5.64512 + 10.50590I$	0
$b = 0.177740 + 1.175180I$		
$u = 0.33404 + 1.42646I$		
$a = 0.275691 - 0.575217I$	$-1.11669 + 5.57868I$	0
$b = -0.839583 + 0.641379I$		
$u = 0.33404 - 1.42646I$		
$a = 0.275691 + 0.575217I$	$-1.11669 - 5.57868I$	0
$b = -0.839583 - 0.641379I$		
$u = 0.343987 + 0.408307I$		
$a = 1.259340 - 0.200200I$	$0.438180 + 1.277440I$	$4.77216 - 5.31124I$
$b = -0.164430 + 0.105291I$		
$u = 0.343987 - 0.408307I$		
$a = 1.259340 + 0.200200I$	$0.438180 - 1.277440I$	$4.77216 + 5.31124I$
$b = -0.164430 - 0.105291I$		
$u = -0.38671 + 1.41560I$		
$a = 0.358467 + 0.797877I$	$1.77264 - 11.28690I$	0
$b = -0.900022 - 0.655211I$		
$u = -0.38671 - 1.41560I$		
$a = 0.358467 - 0.797877I$	$1.77264 + 11.28690I$	0
$b = -0.900022 + 0.655211I$		
$u = -0.39335 + 1.44216I$		
$a = 1.78767 + 0.81460I$	$0.5121 - 17.3690I$	0
$b = -0.744553 + 1.062820I$		
$u = -0.39335 - 1.44216I$		
$a = 1.78767 - 0.81460I$	$0.5121 + 17.3690I$	0
$b = -0.744553 - 1.062820I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.07337 + 1.49652I$		
$a = 0.689010 + 1.074630I$	$-9.15376 + 0.69582I$	0
$b = -0.098684 + 1.018160I$		
$u = -0.07337 - 1.49652I$		
$a = 0.689010 - 1.074630I$	$-9.15376 - 0.69582I$	0
$b = -0.098684 - 1.018160I$		
$u = 0.33300 + 1.47174I$		
$a = 1.55926 - 0.90181I$	$-2.33369 + 11.39850I$	0
$b = -0.717365 - 1.043070I$		
$u = 0.33300 - 1.47174I$		
$a = 1.55926 + 0.90181I$	$-2.33369 - 11.39850I$	0
$b = -0.717365 + 1.043070I$		
$u = 0.20232 + 1.50188I$		
$a = 1.013920 - 0.861496I$	$-8.06757 + 5.26507I$	0
$b = -0.197794 - 0.951591I$		
$u = 0.20232 - 1.50188I$		
$a = 1.013920 + 0.861496I$	$-8.06757 - 5.26507I$	0
$b = -0.197794 + 0.951591I$		
$u = -0.152162 + 0.459797I$		
$a = -3.15294 + 1.05533I$	$0.28773 - 2.82692I$	$5.81058 - 1.66051I$
$b = 0.535113 - 0.935355I$		
$u = -0.152162 - 0.459797I$		
$a = -3.15294 - 1.05533I$	$0.28773 + 2.82692I$	$5.81058 + 1.66051I$
$b = 0.535113 + 0.935355I$		
$u = 0.04801 + 1.62342I$		
$a = 0.686356 - 0.660507I$	$-6.42773 + 5.85172I$	0
$b = -0.622151 - 0.909091I$		
$u = 0.04801 - 1.62342I$		
$a = 0.686356 + 0.660507I$	$-6.42773 - 5.85172I$	0
$b = -0.622151 + 0.909091I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.11130 + 1.62165I$		
$a = 0.478526 + 0.438391I$	$-6.20432 + 1.00932I$	0
$b = -0.614683 + 0.843469I$		
$u = 0.11130 - 1.62165I$		
$a = 0.478526 - 0.438391I$	$-6.20432 - 1.00932I$	0
$b = -0.614683 - 0.843469I$		
$u = 0.012155 + 0.262876I$		
$a = -2.05266 - 4.00172I$	$1.18616 + 1.37603I$	$10.47248 - 4.16898I$
$b = 0.483697 + 0.622554I$		
$u = 0.012155 - 0.262876I$		
$a = -2.05266 + 4.00172I$	$1.18616 - 1.37603I$	$10.47248 + 4.16898I$
$b = 0.483697 - 0.622554I$		

II.

$$I_2^u = \langle -u^{12} - 4u^{10} + \dots - 2u^2 + b, u^{10} + 3u^8 + \dots + a + 1, u^{27} + 9u^{25} + \dots + u - 1 \rangle$$

(i) **Arc colorings**

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^{10} - 3u^8 + 2u^7 - 4u^6 + 4u^5 - 5u^4 + 4u^3 - 3u^2 + 2u - 1 \\ u^{12} + 4u^{10} - 2u^9 + 6u^8 - 6u^7 + 6u^6 - 6u^5 + 5u^4 - 2u^3 + 2u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^{22} - 7u^{20} + \dots - 2u^2 + 1 \\ u^{24} + 8u^{22} + \dots - 8u^5 + 4u^4 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^{21} + 8u^{19} + \dots + 6u^3 - u \\ -u^{21} - 7u^{19} + \dots - u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^{24} + 7u^{22} + \dots - 2u^2 + 1 \\ u^{24} + 8u^{22} + \dots - 8u^5 + 4u^4 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^4 - u^2 - 1 \\ u^6 + 2u^4 + u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^3 \\ -u^5 - u^3 + u \end{pmatrix}$$

(ii) **Obstruction class** = -1

$$(iii) \textbf{Cusp Shapes} = 4u^{24} + 32u^{22} - 20u^{21} + 112u^{20} - 140u^{19} + 268u^{18} - 420u^{17} + 544u^{16} - 744u^{15} + 884u^{14} - 920u^{13} + 1000u^{12} - 860u^{11} + 724u^{10} - 556u^9 + 316u^8 - 168u^7 + 60u^6 + 28u^5 - 24u^4 + 24u^3 - 16u^2 + 10$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$(u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1)^3$
$c_2, c_5$	$(u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1)^3$
$c_3, c_9$	$(u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1)^3$
$c_6, c_7, c_8$ $c_{10}, c_{12}$	$u^{27} + 9u^{25} + \cdots + u - 1$
$c_{11}$	$u^{27} - 18u^{26} + \cdots + 5u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$(y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1)^3$
$c_2, c_5$	$(y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)^3$
$c_3, c_9$	$(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)^3$
$c_6, c_7, c_8$ $c_{10}, c_{12}$	$y^{27} + 18y^{26} + \cdots + 5y - 1$
$c_{11}$	$y^{27} - 18y^{26} + \cdots + 25y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.269474 + 1.004760I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.82716 + 1.96998I$	$0.61694 - 2.45442I$	$2.32792 + 2.91298I$
$b = 0.628449 - 0.875112I$		
$u = 0.269474 - 1.004760I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.82716 - 1.96998I$	$0.61694 + 2.45442I$	$2.32792 - 2.91298I$
$b = 0.628449 + 0.875112I$		
$u = 0.861055 + 0.381086I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 1.96932 + 0.07622I$	$3.59813 + 7.08493I$	$5.57680 - 5.91335I$
$b = -0.728966 - 0.986295I$		
$u = 0.861055 - 0.381086I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 1.96932 - 0.07622I$	$3.59813 - 7.08493I$	$5.57680 + 5.91335I$
$b = -0.728966 + 0.986295I$		
$u = -0.457598 + 0.805344I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.921794 + 0.293449I$	$-1.78344 + 2.09337I$	$-0.51499 - 4.16283I$
$b = 0.140343 + 0.966856I$		
$u = -0.457598 - 0.805344I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.921794 - 0.293449I$	$-1.78344 - 2.09337I$	$-0.51499 + 4.16283I$
$b = 0.140343 - 0.966856I$		
$u = 0.846765 + 0.300344I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 1.11197 - 0.96313I$	$4.37135 + 1.33617I$	$7.28409 - 0.70175I$
$b = -0.796005 + 0.733148I$		
$u = 0.846765 - 0.300344I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 1.11197 + 0.96313I$	$4.37135 - 1.33617I$	$7.28409 + 0.70175I$
$b = -0.796005 - 0.733148I$		
$u = -0.265891 + 1.100950I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.098685 - 0.826899I$	$1.19845$	$8.65235 + 0.I$
$b = 0.512358$		
$u = -0.265891 - 1.100950I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.098685 + 0.826899I$	$1.19845$	$8.65235 + 0.I$
$b = 0.512358$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.186213 + 1.135090I$		
$a = -3.15403 + 1.36709I$	$0.61694 + 2.45442I$	$2.32792 - 2.91298I$
$b = 0.628449 + 0.875112I$		
$u = 0.186213 - 1.135090I$		
$a = -3.15403 - 1.36709I$	$0.61694 - 2.45442I$	$2.32792 + 2.91298I$
$b = 0.628449 - 0.875112I$		
$u = -0.632288 + 1.029230I$		
$a = 0.789222 + 0.418020I$	$3.59813 + 7.08493I$	$5.57680 - 5.91335I$
$b = -0.728966 - 0.986295I$		
$u = -0.632288 - 1.029230I$		
$a = 0.789222 - 0.418020I$	$3.59813 - 7.08493I$	$5.57680 + 5.91335I$
$b = -0.728966 + 0.986295I$		
$u = -0.579410 + 1.072300I$		
$a = 1.46542 + 0.12702I$	$4.37135 + 1.33617I$	$7.28409 - 0.70175I$
$b = -0.796005 + 0.733148I$		
$u = -0.579410 - 1.072300I$		
$a = 1.46542 - 0.12702I$	$4.37135 - 1.33617I$	$7.28409 + 0.70175I$
$b = -0.796005 - 0.733148I$		
$u = 0.543809 + 0.474736I$		
$a = -0.277099 + 0.364720I$	$-1.78344 + 2.09337I$	$-0.51499 - 4.16283I$
$b = 0.140343 + 0.966856I$		
$u = 0.543809 - 0.474736I$		
$a = -0.277099 - 0.364720I$	$-1.78344 - 2.09337I$	$-0.51499 + 4.16283I$
$b = 0.140343 - 0.966856I$		
$u = -0.086211 + 1.280080I$		
$a = -0.09642 - 2.48041I$	$-1.78344 - 2.09337I$	$-0.51499 + 4.16283I$
$b = 0.140343 - 0.966856I$		
$u = -0.086211 - 1.280080I$		
$a = -0.09642 + 2.48041I$	$-1.78344 + 2.09337I$	$-0.51499 - 4.16283I$
$b = 0.140343 + 0.966856I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.267354 + 1.372650I$		
$a = -0.193595 + 0.403575I$	$4.37135 - 1.33617I$	$7.28409 + 0.70175I$
$b = -0.796005 - 0.733148I$		
$u = -0.267354 - 1.372650I$		
$a = -0.193595 - 0.403575I$	$4.37135 + 1.33617I$	$7.28409 - 0.70175I$
$b = -0.796005 + 0.733148I$		
$u = -0.22877 + 1.41032I$		
$a = 1.32551 + 1.36940I$	$3.59813 - 7.08493I$	$5.57680 + 5.91335I$
$b = -0.728966 + 0.986295I$		
$u = -0.22877 - 1.41032I$		
$a = 1.32551 - 1.36940I$	$3.59813 + 7.08493I$	$5.57680 - 5.91335I$
$b = -0.728966 - 0.986295I$		
$u = 0.531781$		
$a = -0.500428$	1.19845	8.65230
$b = 0.512358$		
$u = -0.455687 + 0.130328I$		
$a = -2.88341 + 1.31485I$	$0.61694 - 2.45442I$	$2.32792 + 2.91298I$
$b = 0.628449 - 0.875112I$		
$u = -0.455687 - 0.130328I$		
$a = -2.88341 - 1.31485I$	$0.61694 + 2.45442I$	$2.32792 - 2.91298I$
$b = 0.628449 + 0.875112I$		

### III.

$$I_3^u = \langle u^2a + u^2 + b + a + 1, \ 2u^3a + 5u^3 + \dots + 14a + 15, \ u^4 + u^3 + 3u^2 + 2u + 1 \rangle$$

(i) **Arc colorings**

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a \\ -u^2a - u^2 - a - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^2a + \frac{1}{2}u^3 + 2u^2 + 2a + \frac{3}{2}u + \frac{9}{2} \\ -u^2a - u^2 - a - 2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} \frac{1}{2}u^3 + u^2 + a + \frac{3}{2}u + \frac{5}{2} \\ -u^2a - u^2 - a - 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} \frac{1}{2}u^3 + u^2 + a + \frac{3}{2}u + \frac{5}{2} \\ -u^2a - u^2 - a - 2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^2 + 1 \\ u^3 + u^2 + 2u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ u \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $-\frac{7}{2}u^3a + u^2a + \frac{3}{2}u^3 - \frac{11}{2}au + 7u^2 + \frac{7}{2}a + \frac{15}{2}u + \frac{27}{2}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_4, c_5$	$(u^2 - u + 1)^4$
$c_2$	$(u^2 + u + 1)^4$
$c_3, c_9$	$u^8$
$c_6, c_7, c_{11}$	$(u^4 + u^3 + 3u^2 + 2u + 1)^2$
$c_8$	$(u^4 + u^3 + u^2 + 1)^2$
$c_{10}$	$(u^4 - u^3 + 3u^2 - 2u + 1)^2$
$c_{12}$	$(u^4 - u^3 + u^2 + 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_5$	$(y^2 + y + 1)^4$
$c_3, c_9$	$y^8$
$c_6, c_7, c_{10}$ $c_{11}$	$(y^4 + 5y^3 + 7y^2 + 2y + 1)^2$
$c_8, c_{12}$	$(y^4 + y^3 + 3y^2 + 2y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.395123 + 0.506844I$		
$a = -1.10603 - 1.01030I$	$0.211005 + 0.614778I$	$1.372162 + 0.328352I$
$b = 0.500000 + 0.866025I$		
$u = -0.395123 + 0.506844I$		
$a = -1.82193 + 0.59697I$	$0.21101 - 3.44499I$	$3.71851 + 10.46973I$
$b = 0.500000 - 0.866025I$		
$u = -0.395123 - 0.506844I$		
$a = -1.10603 + 1.01030I$	$0.211005 - 0.614778I$	$1.372162 - 0.328352I$
$b = 0.500000 - 0.866025I$		
$u = -0.395123 - 0.506844I$		
$a = -1.82193 - 0.59697I$	$0.21101 + 3.44499I$	$3.71851 - 10.46973I$
$b = 0.500000 + 0.866025I$		
$u = -0.10488 + 1.55249I$		
$a = -0.797662 - 0.666019I$	$-6.79074 - 5.19385I$	$0.529613 + 1.243149I$
$b = 0.500000 - 0.866025I$		
$u = -0.10488 + 1.55249I$		
$a = -0.524380 + 0.508239I$	$-6.79074 - 1.13408I$	$-4.49529 + 1.20873I$
$b = 0.500000 + 0.866025I$		
$u = -0.10488 - 1.55249I$		
$a = -0.797662 + 0.666019I$	$-6.79074 + 5.19385I$	$0.529613 - 1.243149I$
$b = 0.500000 + 0.866025I$		
$u = -0.10488 - 1.55249I$		
$a = -0.524380 - 0.508239I$	$-6.79074 + 1.13408I$	$-4.49529 - 1.20873I$
$b = 0.500000 - 0.866025I$		

$$\text{IV. } I_4^u = \langle -a^2 - 2au + b + 2a + 2u - 1, \ 3a^3u - 9a^2u + \dots - 2a + 1, \ u^2 + 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a \\ a^2 + 2au - 2a - 2u + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a^3 + 2a^2u - 2a^2 - 2au + a + 1 \\ a^3u - 3a^2u - 3a^2 + au + 6a + u - 4 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a^3u - 4a^2u - 2a^2 + 5au + 6a - 3u - 4 \\ -a^3u + 3a^2u + 4a^2 - 8a - 2u + 6 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -au + u + 2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a^3u + a^3 - a^2u - 5a^2 - au + 7a + u - 3 \\ a^3u - 3a^2u - 3a^2 + au + 6a + u - 4 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ a + 2u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ -au + 2u + 2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-4a^3u + 12a^2u + 8a^2 - 12au - 16a + 4u + 16$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$(u^4 - u^3 + 3u^2 - 2u + 1)^2$
$c_2$	$(u^4 - u^3 + u^2 + 1)^2$
$c_3, c_9$	$u^8 - 5u^6 + 7u^4 - 2u^2 + 1$
$c_5$	$(u^4 + u^3 + u^2 + 1)^2$
$c_6, c_7, c_8$ $c_{10}, c_{12}$	$(u^2 + 1)^4$
$c_{11}$	$(u + 1)^8$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$(y^4 + 5y^3 + 7y^2 + 2y + 1)^2$
$c_2, c_5$	$(y^4 + y^3 + 3y^2 + 2y + 1)^2$
$c_3, c_9$	$(y^4 - 5y^3 + 7y^2 - 2y + 1)^2$
$c_6, c_7, c_8$ $c_{10}, c_{12}$	$(y + 1)^8$
$c_{11}$	$(y - 1)^8$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.000000I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.674360 + 0.399232I$	$6.79074 + 3.16396I$	$7.82674 - 2.56480I$
$b = -0.851808 - 0.911292I$		
$u = 1.000000I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 1.325640 + 0.399232I$	$6.79074 - 3.16396I$	$7.82674 + 2.56480I$
$b = -0.851808 + 0.911292I$		
$u = 1.000000I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.59947 - 1.89923I$	$-0.21101 + 1.41510I$	$4.17326 - 4.90874I$
$b = 0.351808 + 0.720342I$		
$u = 1.000000I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 1.40053 - 1.89923I$	$-0.21101 - 1.41510I$	$4.17326 + 4.90874I$
$b = 0.351808 - 0.720342I$		
$u = -1.000000I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.674360 - 0.399232I$	$6.79074 - 3.16396I$	$7.82674 + 2.56480I$
$b = -0.851808 + 0.911292I$		
$u = -1.000000I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 1.325640 - 0.399232I$	$6.79074 + 3.16396I$	$7.82674 - 2.56480I$
$b = -0.851808 - 0.911292I$		
$u = -1.000000I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.59947 + 1.89923I$	$-0.21101 - 1.41510I$	$4.17326 + 4.90874I$
$b = 0.351808 - 0.720342I$		
$u = -1.000000I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 1.40053 + 1.89923I$	$-0.21101 + 1.41510I$	$4.17326 - 4.90874I$
$b = 0.351808 + 0.720342I$		

## V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$(u^2 - u + 1)^4(u^4 - u^3 + 3u^2 - 2u + 1)^2 \\ \cdot (u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1)^3 \\ \cdot (u^{74} + 24u^{73} + \dots - 225u + 16)$
$c_2$	$(u^2 + u + 1)^4(u^4 - u^3 + u^2 + 1)^2 \\ \cdot (u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1)^3 \\ \cdot (u^{74} + 4u^{73} + \dots + 35u + 4)$
$c_3, c_9$	$u^8(u^8 - 5u^6 + 7u^4 - 2u^2 + 1) \\ \cdot (u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1)^3 \\ \cdot (u^{74} - 2u^{73} + \dots - 2560u + 2048)$
$c_5$	$(u^2 - u + 1)^4(u^4 + u^3 + u^2 + 1)^2 \\ \cdot (u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1)^3 \\ \cdot (u^{74} + 4u^{73} + \dots + 35u + 4)$
$c_6, c_7$	$((u^2 + 1)^4)(u^4 + u^3 + 3u^2 + 2u + 1)^2(u^{27} + 9u^{25} + \dots + u - 1) \\ \cdot (u^{74} + 3u^{73} + \dots + 241u + 34)$
$c_8$	$((u^2 + 1)^4)(u^4 + u^3 + u^2 + 1)^2(u^{27} + 9u^{25} + \dots + u - 1) \\ \cdot (u^{74} + 3u^{73} + \dots + 243u + 34)$
$c_{10}$	$((u^2 + 1)^4)(u^4 - u^3 + 3u^2 - 2u + 1)^2(u^{27} + 9u^{25} + \dots + u - 1) \\ \cdot (u^{74} + 3u^{73} + \dots + 241u + 34)$
$c_{11}$	$((u + 1)^8)(u^4 + u^3 + 3u^2 + 2u + 1)^2(u^{27} - 18u^{26} + \dots + 5u + 1) \\ \cdot (u^{74} - 31u^{73} + \dots - 29555u + 1156)$
$c_{12}$	$((u^2 + 1)^4)(u^4 - u^3 + u^2 + 1)^2(u^{27} + 9u^{25} + \dots + u - 1) \\ \cdot (u^{74} + 3u^{73} + \dots + 243u + 34)$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$(y^2 + y + 1)^4(y^4 + 5y^3 + 7y^2 + 2y + 1)^2 \\ \cdot (y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1)^3 \\ \cdot (y^{74} + 56y^{73} + \dots + 227743y + 256)$
$c_2, c_5$	$(y^2 + y + 1)^4(y^4 + y^3 + 3y^2 + 2y + 1)^2 \\ \cdot (y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)^3 \\ \cdot (y^{74} + 24y^{73} + \dots - 225y + 16)$
$c_3, c_9$	$y^8(y^4 - 5y^3 + 7y^2 - 2y + 1)^2 \\ \cdot (y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)^3 \\ \cdot (y^{74} - 40y^{73} + \dots - 36438016y + 4194304)$
$c_6, c_7, c_{10}$	$((y + 1)^8)(y^4 + 5y^3 + \dots + 2y + 1)^2(y^{27} + 18y^{26} + \dots + 5y - 1) \\ \cdot (y^{74} + 75y^{73} + \dots + 36099y + 1156)$
$c_8, c_{12}$	$((y + 1)^8)(y^4 + y^3 + 3y^2 + 2y + 1)^2(y^{27} + 18y^{26} + \dots + 5y - 1) \\ \cdot (y^{74} + 31y^{73} + \dots + 29555y + 1156)$
$c_{11}$	$((y - 1)^8)(y^4 + 5y^3 + \dots + 2y + 1)^2(y^{27} - 18y^{26} + \dots + 25y - 1) \\ \cdot (y^{74} + 35y^{73} + \dots + 11195711y + 1336336)$