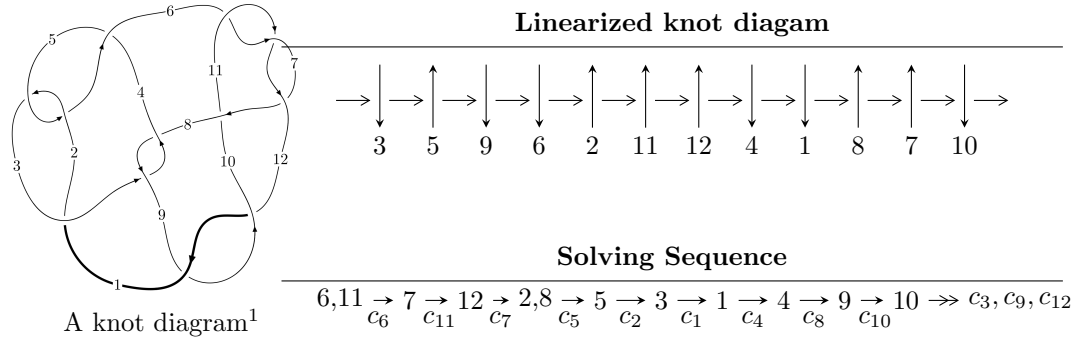


12a<sub>0178</sub> (K12a<sub>0178</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle u^{76} - u^{75} + \dots + 2b - 5u, 2u^{78} - 4u^{77} + \dots + 2a - 1, u^{79} - 3u^{78} + \dots + u - 1 \rangle$$

$$I_2^u = \langle u^3a + u^3 - au + b - a - u - 1, -u^3a - u^4 + a^2 + 2au + 2u^2 + 2a, u^5 - u^4 - 2u^3 + u^2 + u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 89 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle u^{76} - u^{75} + \dots + 2b - 5u, 2u^{78} - 4u^{77} + \dots + 2a - 1, u^{79} - 3u^{78} + \dots + u - 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^{78} + 2u^{77} + \dots - \frac{3}{2}u + \frac{1}{2} \\ -\frac{1}{2}u^{76} + \frac{1}{2}u^{75} + \dots - \frac{11}{2}u^2 + \frac{5}{2}u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -2u^{78} + 4u^{77} + \dots + 5u - \frac{1}{2} \\ 3u^{78} - 5u^{77} + \dots + \frac{3}{2}u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -5u^{78} + 8u^{77} + \dots + \frac{17}{2}u - \frac{5}{2} \\ 5u^{78} - 8u^{77} + \dots + \frac{3}{2}u + 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^9 - 4u^7 + 5u^5 - 2u^3 + u \\ -u^{11} + 5u^9 - 8u^7 + 3u^5 + u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^{78} - u^{77} + \dots + \frac{13}{2}u + \frac{1}{2} \\ 3u^{78} - 5u^{77} + \dots + \frac{3}{2}u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^{13} - 6u^{11} + 13u^9 - 12u^7 + 6u^5 - 4u^3 + u \\ -u^{15} + 7u^{13} - 18u^{11} + 19u^9 - 6u^7 + 2u^5 - 4u^3 - u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^5 + 2u^3 - u \\ u^7 - 3u^5 + 2u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $\frac{11}{2}u^{78} - \frac{19}{2}u^{77} + \dots - 22u + \frac{3}{2}$

(iv) u-Polynomials at the component

| Crossings          | u-Polynomials at each crossing           |
|--------------------|--|
| $c_1, c_4$         | $u^{79} + 24u^{78} + \dots - 14u - 1$    |
| $c_2, c_5$         | $u^{79} + 6u^{78} + \dots + 2u + 1$      |
| $c_3, c_8$         | $u^{79} + u^{78} + \dots - 2048u - 1024$ |
| $c_6, c_7, c_{11}$ | $u^{79} - 3u^{78} + \dots + u - 1$       |
| $c_9, c_{12}$      | $u^{79} - 11u^{78} + \dots - 117u - 73$  |
| $c_{10}$           | $u^{79} + 9u^{78} + \dots - 2487u + 851$ |

(v) Riley Polynomials at the component

| Crossings          | Riley Polynomials at each crossing               |
|--------------------|--|
| $c_1, c_4$         | $y^{79} + 68y^{78} + \dots + 270y - 1$           |
| $c_2, c_5$         | $y^{79} + 24y^{78} + \dots - 14y - 1$            |
| $c_3, c_8$         | $y^{79} + 55y^{78} + \dots - 9437184y - 1048576$ |
| $c_6, c_7, c_{11}$ | $y^{79} - 75y^{78} + \dots - 23y - 1$            |
| $c_9, c_{12}$      | $y^{79} + 73y^{78} + \dots - 70115y - 5329$      |
| $c_{10}$           | $y^{79} - 31y^{78} + \dots - 2637999y - 724201$  |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---|---------------------------------------|----------------------|
| $u = 0.960687 + 0.153679I$<br>$a = 0.507114 + 0.208480I$<br>$b = -0.750208 + 0.893053I$   | $4.67325 - 2.88323I$                  | 0                    |
| $u = 0.960687 - 0.153679I$<br>$a = 0.507114 - 0.208480I$<br>$b = -0.750208 - 0.893053I$   | $4.67325 + 2.88323I$                  | 0                    |
| $u = 0.827370 + 0.170912I$<br>$a = 0.960753 - 0.367241I$<br>$b = -0.764781 - 0.869204I$   | $4.74752 + 2.85194I$                  | $5.96777 - 3.55563I$ |
| $u = 0.827370 - 0.170912I$<br>$a = 0.960753 + 0.367241I$<br>$b = -0.764781 + 0.869204I$   | $4.74752 - 2.85194I$                  | $5.96777 + 3.55563I$ |
| $u = -0.431098 + 0.703014I$<br>$a = -0.011403 + 1.045270I$<br>$b = -0.906120 - 0.737961I$ | $9.87956 - 5.56873I$                  | $5.48276 + 3.81380I$ |
| $u = -0.431098 - 0.703014I$<br>$a = -0.011403 - 1.045270I$<br>$b = -0.906120 + 0.737961I$ | $9.87956 + 5.56873I$                  | $5.48276 - 3.81380I$ |
| $u = -0.417770 + 0.709165I$<br>$a = 2.06985 + 1.21835I$<br>$b = -0.786589 + 1.032560I$    | $8.9584 - 11.8257I$                   | $3.97751 + 8.54937I$ |
| $u = -0.417770 - 0.709165I$<br>$a = 2.06985 - 1.21835I$<br>$b = -0.786589 - 1.032560I$    | $8.9584 + 11.8257I$                   | $3.97751 - 8.54937I$ |
| $u = -0.541357 + 0.617925I$<br>$a = 1.260830 + 0.092818I$<br>$b = -0.902271 + 0.758090I$  | $10.28590 + 1.15255I$                 | $6.41028 + 2.08924I$ |
| $u = -0.541357 - 0.617925I$<br>$a = 1.260830 - 0.092818I$<br>$b = -0.902271 - 0.758090I$  | $10.28590 - 1.15255I$                 | $6.41028 - 2.08924I$ |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|--|---------------------------------------|----------------------|
| $u = -0.554854 + 0.602818I$<br>$a = 0.818220 + 0.193142I$<br>$b = -0.794943 - 1.020680I$ | $9.46345 + 7.42771I$                  | $5.21274 - 2.74453I$ |
| $u = -0.554854 - 0.602818I$<br>$a = 0.818220 - 0.193142I$<br>$b = -0.794943 + 1.020680I$ | $9.46345 - 7.42771I$                  | $5.21274 + 2.74453I$ |
| $u = -0.460232 + 0.639959I$<br>$a = -0.538335 - 0.631341I$<br>$b = 0.819242 - 0.023424I$ | $5.68856 - 2.11060I$                  | $6.83378 + 3.31832I$ |
| $u = -0.460232 - 0.639959I$<br>$a = -0.538335 + 0.631341I$<br>$b = 0.819242 + 0.023424I$ | $5.68856 + 2.11060I$                  | $6.83378 - 3.31832I$ |
| $u = 0.446094 + 0.644815I$<br>$a = -2.25296 + 0.31798I$<br>$b = 0.776837 + 0.897829I$    | $4.79648 + 5.02800I$                  | $3.77738 - 5.92269I$ |
| $u = 0.446094 - 0.644815I$<br>$a = -2.25296 - 0.31798I$<br>$b = 0.776837 - 0.897829I$    | $4.79648 - 5.02800I$                  | $3.77738 + 5.92269I$ |
| $u = 1.211160 + 0.128664I$<br>$a = 1.28344 - 1.04569I$<br>$b = 0.018725 - 0.877436I$     | $0.410093 + 0.569090I$                | 0                    |
| $u = 1.211160 - 0.128664I$<br>$a = 1.28344 + 1.04569I$<br>$b = 0.018725 + 0.877436I$     | $0.410093 - 0.569090I$                | 0                    |
| $u = 0.465338 + 0.625622I$<br>$a = -0.819821 + 1.071380I$<br>$b = 0.783132 - 0.871429I$  | $4.87790 - 0.84564I$                  | $4.12547 - 0.52207I$ |
| $u = 0.465338 - 0.625622I$<br>$a = -0.819821 - 1.071380I$<br>$b = 0.783132 + 0.871429I$  | $4.87790 + 0.84564I$                  | $4.12547 + 0.52207I$ |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = -0.416187 + 0.649698I$<br>$a = -1.47061 - 1.27515I$<br>$b = 0.281669 - 1.127160I$   | $1.81369 - 5.81158I$                  | $1.46444 + 7.37025I$  |
| $u = -0.416187 - 0.649698I$<br>$a = -1.47061 + 1.27515I$<br>$b = 0.281669 + 1.127160I$   | $1.81369 + 5.81158I$                  | $1.46444 - 7.37025I$  |
| $u = -0.467486 + 0.588976I$<br>$a = 0.271507 + 0.612178I$<br>$b = 0.318145 + 1.112630I$  | $2.05435 + 1.75127I$                  | $2.62331 - 0.74126I$  |
| $u = -0.467486 - 0.588976I$<br>$a = 0.271507 - 0.612178I$<br>$b = 0.318145 - 1.112630I$  | $2.05435 - 1.75127I$                  | $2.62331 + 0.74126I$  |
| $u = 1.26366$<br>$a = 0.931332$<br>$b = -0.238856$                                       | $2.75626$                             | $0$                   |
| $u = 0.174701 + 0.686237I$<br>$a = -0.699194 + 0.373449I$<br>$b = -0.764897 + 0.812003I$ | $2.54707 + 0.60070I$                  | $2.16281 - 1.57893I$  |
| $u = 0.174701 - 0.686237I$<br>$a = -0.699194 - 0.373449I$<br>$b = -0.764897 - 0.812003I$ | $2.54707 - 0.60070I$                  | $2.16281 + 1.57893I$  |
| $u = 0.140244 + 0.692618I$<br>$a = 0.66990 - 1.89405I$<br>$b = -0.742698 - 0.939246I$    | $2.15562 + 6.31590I$                  | $0.72997 - 6.99064I$  |
| $u = 0.140244 - 0.692618I$<br>$a = 0.66990 + 1.89405I$<br>$b = -0.742698 + 0.939246I$    | $2.15562 - 6.31590I$                  | $0.72997 + 6.99064I$  |
| $u = 0.331444 + 0.619754I$<br>$a = 1.70156 - 0.90801I$<br>$b = -0.146875 - 0.718790I$    | $-0.39859 + 2.41679I$                 | $-2.51815 - 2.50379I$ |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = 0.331444 - 0.619754I$<br>$a = 1.70156 + 0.90801I$<br>$b = -0.146875 + 0.718790I$    | $-0.39859 - 2.41679I$                 | $-2.51815 + 2.50379I$ |
| $u = -1.284980 + 0.179165I$<br>$a = -0.74042 - 1.23710I$<br>$b = 0.156711 - 1.014790I$   | $1.15848 - 4.83085I$                  | 0                     |
| $u = -1.284980 - 0.179165I$<br>$a = -0.74042 + 1.23710I$<br>$b = 0.156711 + 1.014790I$   | $1.15848 + 4.83085I$                  | 0                     |
| $u = -1.300270 + 0.074806I$<br>$a = -0.754795 + 0.685987I$<br>$b = 0.494882 + 1.001490I$ | $3.08759 + 1.25662I$                  | 0                     |
| $u = -1.300270 - 0.074806I$<br>$a = -0.754795 - 0.685987I$<br>$b = 0.494882 - 1.001490I$ | $3.08759 - 1.25662I$                  | 0                     |
| $u = -1.311810 + 0.262394I$<br>$a = 1.97615 + 0.97895I$<br>$b = -0.742423 + 0.968481I$   | $6.68975 - 9.77430I$                  | 0                     |
| $u = -1.311810 - 0.262394I$<br>$a = 1.97615 - 0.97895I$<br>$b = -0.742423 - 0.968481I$   | $6.68975 + 9.77430I$                  | 0                     |
| $u = 1.330220 + 0.148111I$<br>$a = -2.77349 + 0.42700I$<br>$b = 0.643454 + 0.948330I$    | $4.02017 + 5.12137I$                  | 0                     |
| $u = 1.330220 - 0.148111I$<br>$a = -2.77349 - 0.42700I$<br>$b = 0.643454 - 0.948330I$    | $4.02017 - 5.12137I$                  | 0                     |
| $u = 1.345390 + 0.105400I$<br>$a = -0.77119 + 1.72286I$<br>$b = 0.672238 - 0.709217I$    | $4.74837 + 0.02263I$                  | 0                     |



| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = 1.345390 - 0.105400I$<br>$a = -0.77119 - 1.72286I$<br>$b = 0.672238 + 0.709217I$    | $4.74837 - 0.02263I$                  | 0                     |
| $u = -1.354000 + 0.125122I$<br>$a = -0.577117 + 0.093747I$<br>$b = 0.589160 - 0.295718I$ | $5.02105 - 2.84369I$                  | 0                     |
| $u = -1.354000 - 0.125122I$<br>$a = -0.577117 - 0.093747I$<br>$b = 0.589160 + 0.295718I$ | $5.02105 + 2.84369I$                  | 0                     |
| $u = -1.336080 + 0.257261I$<br>$a = 0.095226 + 0.877787I$<br>$b = -0.779371 - 0.771197I$ | $7.28961 - 4.01466I$                  | 0                     |
| $u = -1.336080 - 0.257261I$<br>$a = 0.095226 - 0.877787I$<br>$b = -0.779371 + 0.771197I$ | $7.28961 + 4.01466I$                  | 0                     |
| $u = 0.055935 + 0.584888I$<br>$a = 0.34048 + 2.64860I$<br>$b = 0.118978 + 0.935231I$     | $-2.96390 + 2.06663I$                 | $-7.76438 - 4.75095I$ |
| $u = 0.055935 - 0.584888I$<br>$a = 0.34048 - 2.64860I$<br>$b = 0.118978 - 0.935231I$     | $-2.96390 - 2.06663I$                 | $-7.76438 + 4.75095I$ |
| $u = 0.372135 + 0.444695I$<br>$a = 0.571797 + 0.154582I$<br>$b = -0.064395 + 0.528805I$  | $0.152685 + 0.966028I$                | $0.58728 - 4.99432I$  |
| $u = 0.372135 - 0.444695I$<br>$a = 0.571797 - 0.154582I$<br>$b = -0.064395 - 0.528805I$  | $0.152685 - 0.966028I$                | $0.58728 + 4.99432I$  |
| $u = -1.42465 + 0.19612I$<br>$a = 0.757172 + 0.386330I$<br>$b = -0.274557 - 0.523897I$   | $5.85268 - 3.48752I$                  | 0                     |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------|
| $u = -1.42465 - 0.19612I$<br>$a = 0.757172 - 0.386330I$<br>$b = -0.274557 + 0.523897I$ | $5.85268 + 3.48752I$                  | 0          |
| $u = -1.42914 + 0.23677I$<br>$a = 1.75980 + 0.17758I$<br>$b = -0.210954 + 0.737939I$   | $5.24909 - 5.55916I$                  | 0          |
| $u = -1.42914 - 0.23677I$<br>$a = 1.75980 - 0.17758I$<br>$b = -0.210954 - 0.737939I$   | $5.24909 + 5.55916I$                  | 0          |
| $u = -1.45767 + 0.01095I$<br>$a = 1.81232 - 0.84748I$<br>$b = -0.830455 + 0.896981I$   | $11.59420 - 3.09088I$                 | 0          |
| $u = -1.45767 - 0.01095I$<br>$a = 1.81232 + 0.84748I$<br>$b = -0.830455 - 0.896981I$   | $11.59420 + 3.09088I$                 | 0          |
| $u = 1.46442 + 0.23981I$<br>$a = -1.64516 + 0.18165I$<br>$b = 0.275942 + 1.152230I$    | $7.87641 + 9.06816I$                  | 0          |
| $u = 1.46442 - 0.23981I$<br>$a = -1.64516 - 0.18165I$<br>$b = 0.275942 - 1.152230I$    | $7.87641 - 9.06816I$                  | 0          |
| $u = 1.46930 + 0.21252I$<br>$a = -0.105941 + 0.396384I$<br>$b = 0.341084 - 1.138020I$  | $8.28626 + 1.18360I$                  | 0          |
| $u = 1.46930 - 0.21252I$<br>$a = -0.105941 - 0.396384I$<br>$b = 0.341084 + 1.138020I$  | $8.28626 - 1.18360I$                  | 0          |
| $u = -1.47358 + 0.23322I$<br>$a = -2.85449 + 0.44307I$<br>$b = 0.790272 - 0.913410I$   | $10.99410 - 8.23765I$                 | 0          |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------|
| $u = -1.47358 - 0.23322I$<br>$a = -2.85449 - 0.44307I$<br>$b = 0.790272 + 0.913410I$ | $10.99410 + 8.23765I$                 | 0          |
| $u = -1.47618 + 0.22313I$<br>$a = -1.48000 - 1.76752I$<br>$b = 0.805517 + 0.864477I$ | $11.14650 - 2.25375I$                 | 0          |
| $u = -1.47618 - 0.22313I$<br>$a = -1.48000 + 1.76752I$<br>$b = 0.805517 - 0.864477I$ | $11.14650 + 2.25375I$                 | 0          |
| $u = 1.47734 + 0.22877I$<br>$a = -1.30565 + 0.55825I$<br>$b = 0.851193 + 0.043651I$  | $11.94830 + 5.28265I$                 | 0          |
| $u = 1.47734 - 0.22877I$<br>$a = -1.30565 - 0.55825I$<br>$b = 0.851193 - 0.043651I$  | $11.94830 - 5.28265I$                 | 0          |
| $u = 1.47342 + 0.26226I$<br>$a = 2.75426 - 0.27890I$<br>$b = -0.787624 - 1.043110I$  | $15.0608 + 15.3708I$                  | 0          |
| $u = 1.47342 - 0.26226I$<br>$a = 2.75426 + 0.27890I$<br>$b = -0.787624 + 1.043110I$  | $15.0608 - 15.3708I$                  | 0          |
| $u = 1.47783 + 0.25743I$<br>$a = 0.82024 - 1.67408I$<br>$b = -0.918969 + 0.728773I$  | $16.0459 + 9.0741I$                   | 0          |
| $u = 1.47783 - 0.25743I$<br>$a = 0.82024 + 1.67408I$<br>$b = -0.918969 - 0.728773I$  | $16.0459 - 9.0741I$                   | 0          |
| $u = 1.49805 + 0.19160I$<br>$a = 1.56162 - 1.06045I$<br>$b = -0.811404 + 1.021460I$  | $16.1357 - 4.5825I$                   | 0          |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = 1.49805 - 0.19160I$<br>$a = 1.56162 + 1.06045I$<br>$b = -0.811404 - 1.021460I$    | $16.1357 + 4.5825I$                   | 0                     |
| $u = 1.49830 + 0.20045I$<br>$a = 2.02683 + 0.60119I$<br>$b = -0.917511 - 0.773257I$    | $16.9160 + 1.7936I$                   | 0                     |
| $u = 1.49830 - 0.20045I$<br>$a = 2.02683 - 0.60119I$<br>$b = -0.917511 + 0.773257I$    | $16.9160 - 1.7936I$                   | 0                     |
| $u = -0.108953 + 0.459074I$<br>$a = -1.93875 - 2.39147I$<br>$b = 0.573629 - 0.929349I$ | $-0.49704 - 2.88847I$                 | $-5.04267 + 1.92432I$ |
| $u = -0.108953 - 0.459074I$<br>$a = -1.93875 + 2.39147I$<br>$b = 0.573629 + 0.929349I$ | $-0.49704 + 2.88847I$                 | $-5.04267 - 1.92432I$ |
| $u = 0.247554 + 0.377813I$<br>$a = 0.560959 + 0.199573I$<br>$b = 0.193812 + 0.327293I$ | $0.102843 + 1.008930I$                | $1.78319 - 6.38352I$  |
| $u = 0.247554 - 0.377813I$<br>$a = 0.560959 - 0.199573I$<br>$b = 0.193812 - 0.327293I$ | $0.102843 - 1.008930I$                | $1.78319 + 6.38352I$  |
| $u = -0.152462 + 0.276606I$<br>$a = 1.19363 - 1.28731I$<br>$b = 0.511852 + 0.767170I$  | $0.09111 + 1.51758I$                  | $-2.07514 - 4.93514I$ |
| $u = -0.152462 - 0.276606I$<br>$a = 1.19363 + 1.28731I$<br>$b = 0.511852 - 0.767170I$  | $0.09111 - 1.51758I$                  | $-2.07514 + 4.93514I$ |

$$\text{II. } I_2^u = \langle u^3 a + u^3 - au + b - a - u - 1, -u^3 a - u^4 + a^2 + 2au + 2u^2 + 2a, u^5 - u^4 - 2u^3 + u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a \\ -u^3 a - u^3 + au + a + u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^3 a - au + u + 1 \\ -u^3 a - u^3 + au + a + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^3 + a + 2u + 1 \\ -u^3 a - u^3 + au + a + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 + a + 2u + 1 \\ -u^3 a - u^3 + au + a + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^4 + u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = u^4 a + 4u^3 a + u^4 - 2u^2 a + u^3 - 4au - 2u^2 - 5a + 3u + 1$$

(iv) u-Polynomials at the component

| Crossings       | u-Polynomials at each crossing        |
|-----------------|---------------------------------------|
| $c_1, c_4, c_5$ | $(u^2 - u + 1)^5$                     |
| $c_2$           | $(u^2 + u + 1)^5$                     |
| $c_3, c_8$      | $u^{10}$                              |
| $c_6, c_7$      | $(u^5 - u^4 - 2u^3 + u^2 + u + 1)^2$  |
| $c_9$           | $(u^5 + u^4 + 2u^3 + u^2 + u + 1)^2$  |
| $c_{10}$        | $(u^5 - 3u^4 + 4u^3 - u^2 - u + 1)^2$ |
| $c_{11}$        | $(u^5 + u^4 - 2u^3 - u^2 + u - 1)^2$  |
| $c_{12}$        | $(u^5 - u^4 + 2u^3 - u^2 + u - 1)^2$  |

(v) Riley Polynomials at the component

| Crossings                | Riley Polynomials at each crossing     |
|--------------------------|--|
| $c_1, c_2, c_4$<br>$c_5$ | $(y^2 + y + 1)^5$                      |
| $c_3, c_8$               | $y^{10}$                               |
| $c_6, c_7, c_{11}$       | $(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^2$ |
| $c_9, c_{12}$            | $(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^2$  |
| $c_{10}$                 | $(y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1)^2$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -1.21774$              |                                       |                       |
| $a = -0.685143 + 0.545349I$ | $2.40108 + 2.02988I$                  | $0.33682 - 4.42764I$  |
| $b = 0.500000 + 0.866025I$  |                                       |                       |
| $u = -1.21774$              |                                       |                       |
| $a = -0.685143 - 0.545349I$ | $2.40108 - 2.02988I$                  | $0.33682 + 4.42764I$  |
| $b = 0.500000 - 0.866025I$  |                                       |                       |
| $u = -0.309916 + 0.549911I$ |                                       |                       |
| $a = 0.394874 + 0.200669I$  | $0.329100 + 0.499304I$                | $-0.01046 + 1.42329I$ |
| $b = 0.500000 + 0.866025I$  |                                       |                       |
| $u = -0.309916 + 0.549911I$ |                                       |                       |
| $a = -1.52365 - 1.30833I$   | $0.32910 - 3.56046I$                  | $2.49844 + 7.77102I$  |
| $b = 0.500000 - 0.866025I$  |                                       |                       |
| $u = -0.309916 - 0.549911I$ |                                       |                       |
| $a = 0.394874 - 0.200669I$  | $0.329100 - 0.499304I$                | $-0.01046 - 1.42329I$ |
| $b = 0.500000 - 0.866025I$  |                                       |                       |
| $u = -0.309916 - 0.549911I$ |                                       |                       |
| $a = -1.52365 + 1.30833I$   | $0.32910 + 3.56046I$                  | $2.49844 - 7.77102I$  |
| $b = 0.500000 + 0.866025I$  |                                       |                       |
| $u = 1.41878 + 0.21917I$    |                                       |                       |
| $a = -0.335573 + 0.598472I$ | $5.87256 + 2.37095I$                  | $4.29156 + 0.98555I$  |
| $b = 0.500000 - 0.866025I$  |                                       |                       |
| $u = 1.41878 + 0.21917I$    |                                       |                       |
| $a = -1.85051 + 0.27617I$   | $5.87256 + 6.43072I$                  | $6.88365 - 7.29164I$  |
| $b = 0.500000 + 0.866025I$  |                                       |                       |
| $u = 1.41878 - 0.21917I$    |                                       |                       |
| $a = -0.335573 - 0.598472I$ | $5.87256 - 2.37095I$                  | $4.29156 - 0.98555I$  |
| $b = 0.500000 + 0.866025I$  |                                       |                       |
| $u = 1.41878 - 0.21917I$    |                                       |                       |
| $a = -1.85051 - 0.27617I$   | $5.87256 - 6.43072I$                  | $6.88365 + 7.29164I$  |
| $b = 0.500000 - 0.866025I$  |                                       |                       |



### III. u-Polynomials

| Crossings  | u-Polynomials at each crossing  |
|------------|---|
| $c_1, c_4$ | $((u^2 - u + 1)^5)(u^{79} + 24u^{78} + \dots - 14u - 1)$                        |
| $c_2$      | $((u^2 + u + 1)^5)(u^{79} + 6u^{78} + \dots + 2u + 1)$                          |
| $c_3, c_8$ | $u^{10}(u^{79} + u^{78} + \dots - 2048u - 1024)$                                |
| $c_5$      | $((u^2 - u + 1)^5)(u^{79} + 6u^{78} + \dots + 2u + 1)$                          |
| $c_6, c_7$ | $((u^5 - u^4 - 2u^3 + u^2 + u + 1)^2)(u^{79} - 3u^{78} + \dots + u - 1)$        |
| $c_9$      | $((u^5 + u^4 + 2u^3 + u^2 + u + 1)^2)(u^{79} - 11u^{78} + \dots - 117u - 73)$   |
| $c_{10}$   | $((u^5 - 3u^4 + 4u^3 - u^2 - u + 1)^2)(u^{79} + 9u^{78} + \dots - 2487u + 851)$ |
| $c_{11}$   | $((u^5 + u^4 - 2u^3 - u^2 + u - 1)^2)(u^{79} - 3u^{78} + \dots + u - 1)$        |
| $c_{12}$   | $((u^5 - u^4 + 2u^3 - u^2 + u - 1)^2)(u^{79} - 11u^{78} + \dots - 117u - 73)$   |

#### IV. Riley Polynomials

| Crossings          | Riley Polynomials at each crossing  |
|--------------------|---|
| $c_1, c_4$         | $((y^2 + y + 1)^5)(y^{79} + 68y^{78} + \dots + 270y - 1)$   |
| $c_2, c_5$         | $((y^2 + y + 1)^5)(y^{79} + 24y^{78} + \dots - 14y - 1)$  |
| $c_3, c_8$         | $y^{10}(y^{79} + 55y^{78} + \dots - 9437184y - 1048576)$  |
| $c_6, c_7, c_{11}$ | $((y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^2)(y^{79} - 75y^{78} + \dots - 23y - 1)$                     |
| $c_9, c_{12}$      | $((y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^2)(y^{79} + 73y^{78} + \dots - 70115y - 5329)$                |
| $c_{10}$           | $(y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1)^2$<br>$\cdot (y^{79} - 31y^{78} + \dots - 2637999y - 724201)$ |