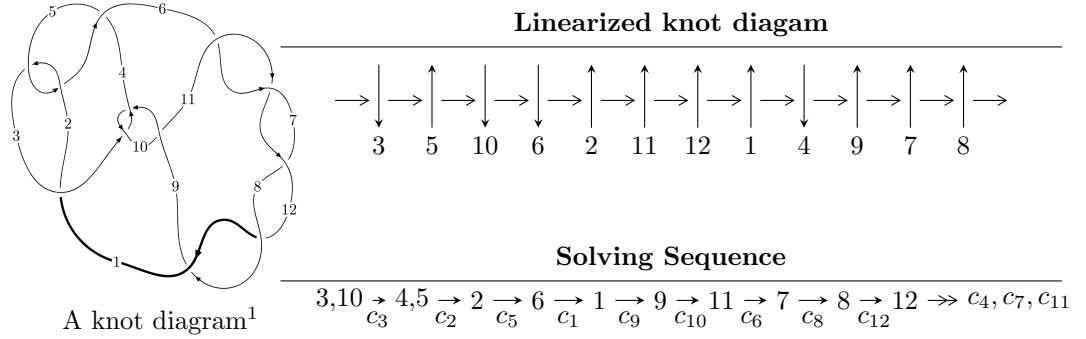


$12a_{0193}$  ( $K12a_{0193}$ )



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 1.76155 \times 10^{30} u^{55} + 2.38665 \times 10^{30} u^{54} + \dots + 1.86805 \times 10^{31} b - 5.18520 \times 10^{31}, \\ 7.54734 \times 10^{30} u^{55} - 1.06356 \times 10^{31} u^{54} + \dots + 1.86805 \times 10^{31} a + 8.01489 \times 10^{31}, u^{56} - u^{55} + \dots - 44u^2 - \dots \rangle$$

$$I_1^v = \langle a, v^3 + 2v^2 + 2b + 2v + 1, v^4 + v^3 + 2v^2 - v + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 60 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 1.76 \times 10^{30} u^{55} + 2.39 \times 10^{30} u^{54} + \dots + 1.87 \times 10^{31} b - 5.19 \times 10^{31}, \ 7.55 \times 10^{30} u^{55} - 1.06 \times 10^{31} u^{54} + \dots + 1.87 \times 10^{31} a + 8.01 \times 10^{31}, \ u^{56} - u^{55} + \dots - 44u^2 - 16 \rangle$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.404023u^{55} + 0.569343u^{54} + \dots + 4.15487u - 4.29052 \\ -0.0942991u^{55} - 0.127762u^{54} + \dots + 0.441391u + 2.77573 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.124417u^{55} - 0.0227610u^{54} + \dots + 3.42223u + 3.91486 \\ 0.197532u^{55} - 0.245618u^{54} + \dots + 1.00380u + 1.74945 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.124417u^{55} - 0.0227610u^{54} + \dots + 3.42223u + 3.91486 \\ -0.148908u^{55} + 0.254056u^{54} + \dots - 2.99446u - 4.10429 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.0731156u^{55} - 0.268379u^{54} + \dots + 4.42602u + 5.66431 \\ 0.197532u^{55} - 0.245618u^{54} + \dots + 1.00380u + 1.74945 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.113306u^{55} + 0.203193u^{54} + \dots - 3.36863u - 1.54199 \\ -0.262328u^{55} + 0.0564765u^{54} + \dots + 0.999404u + 0.529453 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.516553u^{55} + 0.486410u^{54} + \dots + 8.01784u - 2.62530 \\ -0.254069u^{55} + 0.475756u^{54} + \dots + 2.22140u - 6.56977 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.330162u^{55} + 0.368862u^{54} + \dots - 9.49132u - 8.58801 \\ -0.363570u^{55} + 0.132323u^{54} + \dots + 7.63673u + 0.248734 \end{pmatrix}$$

(ii) **Obstruction class = -1**

(iii) **Cusp Shapes** =  $-0.0743933u^{55} - 0.650973u^{54} + \dots - 12.4637u + 17.4604$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^{56} + 19u^{55} + \cdots - 20u + 1$
$c_2, c_5$	$u^{56} + 3u^{55} + \cdots + 2u + 1$
$c_3, c_9$	$u^{56} - u^{55} + \cdots - 44u^2 - 16$
$c_6, c_7, c_8$ $c_{11}, c_{12}$	$u^{56} - 3u^{55} + \cdots + 2u - 1$
$c_{10}$	$u^{56} - 25u^{55} + \cdots - 1408u + 256$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{56} + 39y^{55} + \cdots - 388y + 1$
$c_2, c_5$	$y^{56} + 19y^{55} + \cdots - 20y + 1$
$c_3, c_9$	$y^{56} + 25y^{55} + \cdots + 1408y + 256$
$c_6, c_7, c_8$ $c_{11}, c_{12}$	$y^{56} - 73y^{55} + \cdots + 16y + 1$
$c_{10}$	$y^{56} + 5y^{55} + \cdots - 925696y + 65536$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.945963 + 0.329000I$ $a = 0.700162 + 0.301248I$ $b = -0.710485 + 0.729480I$	$3.41470 + 0.08627I$	$10.40732 - 0.41249I$
$u = 0.945963 - 0.329000I$ $a = 0.700162 - 0.301248I$ $b = -0.710485 - 0.729480I$	$3.41470 - 0.08627I$	$10.40732 + 0.41249I$
$u = 0.625712 + 0.814457I$ $a = 0.889757 + 0.875058I$ $b = -0.083216 + 1.022700I$	$-3.46331 - 2.44033I$	$-1.79100 + 4.21493I$
$u = 0.625712 - 0.814457I$ $a = 0.889757 - 0.875058I$ $b = -0.083216 - 1.022700I$	$-3.46331 + 2.44033I$	$-1.79100 - 4.21493I$
$u = 0.323104 + 1.005060I$ $a = 0.642445 - 0.528510I$ $b = -0.489124 - 1.083120I$	$10.64430 + 0.45572I$	$9.98152 - 0.50436I$
$u = 0.323104 - 1.005060I$ $a = 0.642445 + 0.528510I$ $b = -0.489124 + 1.083120I$	$10.64430 - 0.45572I$	$9.98152 + 0.50436I$
$u = 0.371261 + 0.991405I$ $a = 0.781690 + 0.096007I$ $b = -0.675087 + 0.237892I$	$3.78611 - 2.97347I$	$12.77186 + 5.12067I$
$u = 0.371261 - 0.991405I$ $a = 0.781690 - 0.096007I$ $b = -0.675087 - 0.237892I$	$3.78611 + 2.97347I$	$12.77186 - 5.12067I$
$u = 0.284163 + 1.021260I$ $a = -1.11146 - 1.51595I$ $b = 0.733335 + 0.752099I$	$3.44212 + 1.17546I$	$10.25427 - 3.27090I$
$u = 0.284163 - 1.021260I$ $a = -1.11146 + 1.51595I$ $b = 0.733335 - 0.752099I$	$3.44212 - 1.17546I$	$10.25427 + 3.27090I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.661266 + 0.661352I$		
$a = 1.09003 - 0.94478I$	$-1.41938 - 0.49911I$	$2.60701 + 1.40158I$
$b = -0.000047 - 0.953461I$		
$u = -0.661266 - 0.661352I$		
$a = 1.09003 + 0.94478I$	$-1.41938 + 0.49911I$	$2.60701 - 1.40158I$
$b = -0.000047 + 0.953461I$		
$u = -0.978145 + 0.449475I$		
$a = 0.635866 + 0.398468I$	$2.70209 - 5.44166I$	$8.56320 + 6.09737I$
$b = -0.681700 + 0.964218I$		
$u = -0.978145 - 0.449475I$		
$a = 0.635866 - 0.398468I$	$2.70209 + 5.44166I$	$8.56320 - 6.09737I$
$b = -0.681700 - 0.964218I$		
$u = 0.739636 + 0.543266I$		
$a = 1.27278 + 1.20579I$	$6.95218 + 1.78242I$	$3.71796 - 0.00626I$
$b = 0.109646 + 0.952563I$		
$u = 0.739636 - 0.543266I$		
$a = 1.27278 - 1.20579I$	$6.95218 - 1.78242I$	$3.71796 + 0.00626I$
$b = 0.109646 - 0.952563I$		
$u = -0.423575 + 1.030690I$		
$a = -2.51731 + 0.08098I$	$2.80455 + 4.29067I$	$8.68297 - 2.64204I$
$b = 0.696401 + 0.959847I$		
$u = -0.423575 - 1.030690I$		
$a = -2.51731 - 0.08098I$	$2.80455 - 4.29067I$	$8.68297 + 2.64204I$
$b = 0.696401 - 0.959847I$		
$u = 0.144714 + 0.863875I$		
$a = -3.05379 + 1.22740I$	$9.78220 - 2.56986I$	$13.5531 + 4.3615I$
$b = 0.662709 - 0.878637I$		
$u = 0.144714 - 0.863875I$		
$a = -3.05379 - 1.22740I$	$9.78220 + 2.56986I$	$13.5531 - 4.3615I$
$b = 0.662709 + 0.878637I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.588153 + 0.958301I$		
$a = 0.773912 - 0.833223I$	$-0.51184 + 5.35586I$	$4.95676 - 7.14944I$
$b = -0.137469 - 1.083360I$		
$u = -0.588153 - 0.958301I$		
$a = 0.773912 + 0.833223I$	$-0.51184 - 5.35586I$	$4.95676 + 7.14944I$
$b = -0.137469 + 1.083360I$		
$u = -0.473668 + 1.064350I$		
$a = -0.68920 + 1.25309I$	$2.37111 + 2.38012I$	$7.11781 - 3.12902I$
$b = 0.770337 - 0.690812I$		
$u = -0.473668 - 1.064350I$		
$a = -0.68920 - 1.25309I$	$2.37111 - 2.38012I$	$7.11781 + 3.12902I$
$b = 0.770337 + 0.690812I$		
$u = -0.306607 + 0.768934I$		
$a = 0.677930 + 0.501746I$	$1.59907 - 1.22012I$	$10.24669 - 1.76763I$
$b = -0.495582 + 1.016170I$		
$u = -0.306607 - 0.768934I$		
$a = 0.677930 - 0.501746I$	$1.59907 + 1.22012I$	$10.24669 + 1.76763I$
$b = -0.495582 - 1.016170I$		
$u = 0.691853 + 0.442021I$		
$a = 0.666356 - 0.423245I$	$-0.47690 + 3.08931I$	$0.47513 - 3.63327I$
$b = -0.608819 - 0.951542I$		
$u = 0.691853 - 0.442021I$		
$a = 0.666356 + 0.423245I$	$-0.47690 - 3.08931I$	$0.47513 + 3.63327I$
$b = -0.608819 + 0.951542I$		
$u = -1.123100 + 0.376086I$		
$a = 0.673422 - 0.285619I$	$12.79390 - 1.04374I$	$11.13568 + 0.I$
$b = -0.777518 - 0.731848I$		
$u = -1.123100 - 0.376086I$		
$a = 0.673422 + 0.285619I$	$12.79390 + 1.04374I$	$11.13568 + 0.I$
$b = -0.777518 + 0.731848I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.031496 + 1.220130I$		
$a = -1.73190 + 0.77105I$	$9.36102 - 2.89044I$	$13.8461 + 3.0592I$
$b = 0.769526 - 0.864952I$		
$u = 0.031496 - 1.220130I$		
$a = -1.73190 - 0.77105I$	$9.36102 + 2.89044I$	$13.8461 - 3.0592I$
$b = 0.769526 + 0.864952I$		
$u = 0.568066 + 1.084730I$		
$a = -2.24565 - 0.41344I$	$1.44085 - 7.97313I$	$0. + 7.82699I$
$b = 0.703592 - 0.999172I$		
$u = 0.568066 - 1.084730I$		
$a = -2.24565 + 0.41344I$	$1.44085 + 7.97313I$	$0. - 7.82699I$
$b = 0.703592 + 0.999172I$		
$u = 0.591719 + 1.074220I$		
$a = 0.704304 + 0.824413I$	$8.62037 - 6.88650I$	$0$
$b = -0.157829 + 1.132950I$		
$u = 0.591719 - 1.074220I$		
$a = 0.704304 - 0.824413I$	$8.62037 + 6.88650I$	$0$
$b = -0.157829 - 1.132950I$		
$u = -0.422992 + 1.152020I$		
$a = 0.742663 - 0.089155I$	$13.22670 + 4.07484I$	$13.16985 + 0.I$
$b = -0.772781 - 0.231893I$		
$u = -0.422992 - 1.152020I$		
$a = 0.742663 + 0.089155I$	$13.22670 - 4.07484I$	$13.16985 + 0.I$
$b = -0.772781 + 0.231893I$		
$u = 1.127950 + 0.485672I$		
$a = 0.618155 - 0.389809I$	$12.03690 + 6.70540I$	$0$
$b = -0.718412 - 0.980360I$		
$u = 1.127950 - 0.485672I$		
$a = 0.618155 + 0.389809I$	$12.03690 - 6.70540I$	$0$
$b = -0.718412 + 0.980360I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.754125$		
$a = 0.724705$	9.83456	8.53390
$b = 0.455004$		
$u = -0.256062 + 0.665128I$		
$a = 0.904103 - 0.096717I$	$0.338686 + 0.999830I$	$6.13657 - 6.36197I$
$b = -0.397261 - 0.233187I$		
$u = -0.256062 - 0.665128I$		
$a = 0.904103 + 0.096717I$	$0.338686 - 0.999830I$	$6.13657 + 6.36197I$
$b = -0.397261 + 0.233187I$		
$u = 0.588126 + 1.170640I$		
$a = -0.617779 - 0.984152I$	6.05580 - 5.59891I	0
$b = 0.824403 + 0.669190I$		
$u = 0.588126 - 1.170640I$		
$a = -0.617779 + 0.984152I$	6.05580 + 5.59891I	0
$b = 0.824403 - 0.669190I$		
$u = -0.658056 + 1.167570I$		
$a = -1.99266 + 0.49709I$	4.97425 + 11.38970I	0
$b = 0.720138 + 1.025440I$		
$u = -0.658056 - 1.167570I$		
$a = -1.99266 - 0.49709I$	4.97425 - 11.38970I	0
$b = 0.720138 - 1.025440I$		
$u = -0.66401 + 1.25051I$		
$a = -0.594793 + 0.840724I$	15.6301 + 7.4127I	0
$b = 0.862806 - 0.659902I$		
$u = -0.66401 - 1.25051I$		
$a = -0.594793 - 0.840724I$	15.6301 - 7.4127I	0
$b = 0.862806 + 0.659902I$		
$u = 0.72488 + 1.23003I$		
$a = -1.83482 - 0.53507I$	14.4517 - 13.3499I	0
$b = 0.732388 - 1.044730I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.72488 - 1.23003I$		
$a = -1.83482 + 0.53507I$	$14.4517 + 13.3499I$	0
$b = 0.732388 + 1.044730I$		
$u = -0.520003 + 0.233894I$		
$a = 0.762531 - 0.369226I$	$0.16754 + 1.55102I$	$-0.50728 - 2.39456I$
$b = -0.544789 - 0.773570I$		
$u = -0.520003 - 0.233894I$		
$a = 0.762531 + 0.369226I$	$0.16754 - 1.55102I$	$-0.50728 + 2.39456I$
$b = -0.544789 + 0.773570I$		
$u = -0.04885 + 1.43050I$		
$a = -1.47868 - 0.48254I$	$-19.6229 + 3.0661I$	0
$b = 0.825254 + 0.886448I$		
$u = -0.04885 - 1.43050I$		
$a = -1.47868 + 0.48254I$	$-19.6229 - 3.0661I$	0
$b = 0.825254 - 0.886448I$		
$u = 0.485800$		
$a = 0.939168$	1.28164	7.41160
$b = 0.224170$		

$$\text{III. } I_1^v = \langle a, v^3 + 2v^2 + 2b + 2v + 1, v^4 + v^3 + 2v^2 - v + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ -\frac{1}{2}v^3 - v^2 - v - \frac{1}{2} \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ \frac{1}{2}v^3 + v^2 + v - \frac{1}{2} \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{1}{2}v^3 - v^2 - v - \frac{1}{2} \\ -\frac{1}{2}v^3 - v^2 - v + \frac{1}{2} \end{pmatrix}$$

$$a_1 = \begin{pmatrix} \frac{1}{2}v^3 + v^2 + v + \frac{1}{2} \\ \frac{1}{2}v^3 + v^2 + v - \frac{1}{2} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -v \\ -\frac{1}{2}v^3 - v^2 - v + \frac{1}{2} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ -\frac{1}{2}v^3 - v + \frac{1}{2} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} \frac{1}{2}v^3 + v^2 + v + \frac{1}{2} \\ \frac{1}{2}v^3 + v - \frac{1}{2} \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-3v^3 - 5v^2 - 7v + 7$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_4, c_5$	$(u^2 - u + 1)^2$
$c_2$	$(u^2 + u + 1)^2$
$c_3, c_9, c_{10}$	$u^4$
$c_6, c_7, c_8$	$(u^2 - u - 1)^2$
$c_{11}, c_{12}$	$(u^2 + u - 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_5$	$(y^2 + y + 1)^2$
$c_3, c_9, c_{10}$	$y^4$
$c_6, c_7, c_8$ $c_{11}, c_{12}$	$(y^2 - 3y + 1)^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 0.309017 + 0.535233I$		
$a = 0$	$0.98696 + 2.02988I$	$6.50000 - 5.40059I$
$b = -0.500000 - 0.866025I$		
$v = 0.309017 - 0.535233I$		
$a = 0$	$0.98696 - 2.02988I$	$6.50000 + 5.40059I$
$b = -0.500000 + 0.866025I$		
$v = -0.80902 + 1.40126I$		
$a = 0$	$8.88264 - 2.02988I$	$6.50000 + 1.52761I$
$b = -0.500000 + 0.866025I$		
$v = -0.80902 - 1.40126I$		
$a = 0$	$8.88264 + 2.02988I$	$6.50000 - 1.52761I$
$b = -0.500000 - 0.866025I$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$((u^2 - u + 1)^2)(u^{56} + 19u^{55} + \dots - 20u + 1)$
$c_2$	$((u^2 + u + 1)^2)(u^{56} + 3u^{55} + \dots + 2u + 1)$
$c_3, c_9$	$u^4(u^{56} - u^{55} + \dots - 44u^2 - 16)$
$c_5$	$((u^2 - u + 1)^2)(u^{56} + 3u^{55} + \dots + 2u + 1)$
$c_6, c_7, c_8$	$((u^2 - u - 1)^2)(u^{56} - 3u^{55} + \dots + 2u - 1)$
$c_{10}$	$u^4(u^{56} - 25u^{55} + \dots - 1408u + 256)$
$c_{11}, c_{12}$	$((u^2 + u - 1)^2)(u^{56} - 3u^{55} + \dots + 2u - 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$((y^2 + y + 1)^2)(y^{56} + 39y^{55} + \dots - 388y + 1)$
$c_2, c_5$	$((y^2 + y + 1)^2)(y^{56} + 19y^{55} + \dots - 20y + 1)$
$c_3, c_9$	$y^4(y^{56} + 25y^{55} + \dots + 1408y + 256)$
$c_6, c_7, c_8$ $c_{11}, c_{12}$	$((y^2 - 3y + 1)^2)(y^{56} - 73y^{55} + \dots + 16y + 1)$
$c_{10}$	$y^4(y^{56} + 5y^{55} + \dots - 925696y + 65536)$